

École Joliot-Curie 2015

*“Instrumentation, detection and simulation in modern nuclear physics”*

# Nuclear Structure studies using *Advanced-Gamma-Tracking* techniques

Caterina Michelagnoli

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# World-wide projects for $\gamma$ -ray spectroscopy

*Use highly segmented  
Ge detectors  
+ digital electronics to  
reconstruct the path of  $\gamma$  rays  
in the detector medium*

**GRETA**  
(Gamma-Ray  
Energy Tracking  
Array)



**AGATA** (Advanced-Gamma-Tracking Array)



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**AGATA** (Advanced-Gamma-Tracking Array)



**Grand Accelérateur National  
d'Ions Lourdes (GANIL) France  
(2014 – at present)**

**GSI, Germany (2012-2014)  
@ fragment separator**

**Legnaro National Lab. (2009-2012)  
Demostrator phase**



# Outline

*PART 1 (September 28<sup>th</sup> 2015)*

## **General Introduction: Physics Motivation**

1. Nuclear structure and  $\gamma$ -ray spectroscopy
2. Structure of neutron-rich fission fragments

## **$\gamma$ -ray tracking: Motivation and Concept**

1. In-beam  $\gamma$ -ray detection: requirements
2. From conventional germanium detector arrays to  $\gamma$ -ray tracking
3.  $\gamma$ -ray tracking (“philosophy”, approximations, open questions)

## **Pulse Shape Analysis (PSA)**

1. Principle
2. Position resolution and Compton imaging

*(be aware ... personal 😊selection of topics!)*

# Outline

*PART 2 (September 29<sup>th</sup> 2015)*

## **Pulse Shape Analysis (PSA)**

1. Signal bases calculation
2. Signal decomposition

**Some results from Ge position sensitive mode operation and  $\gamma$ -ray tracking**

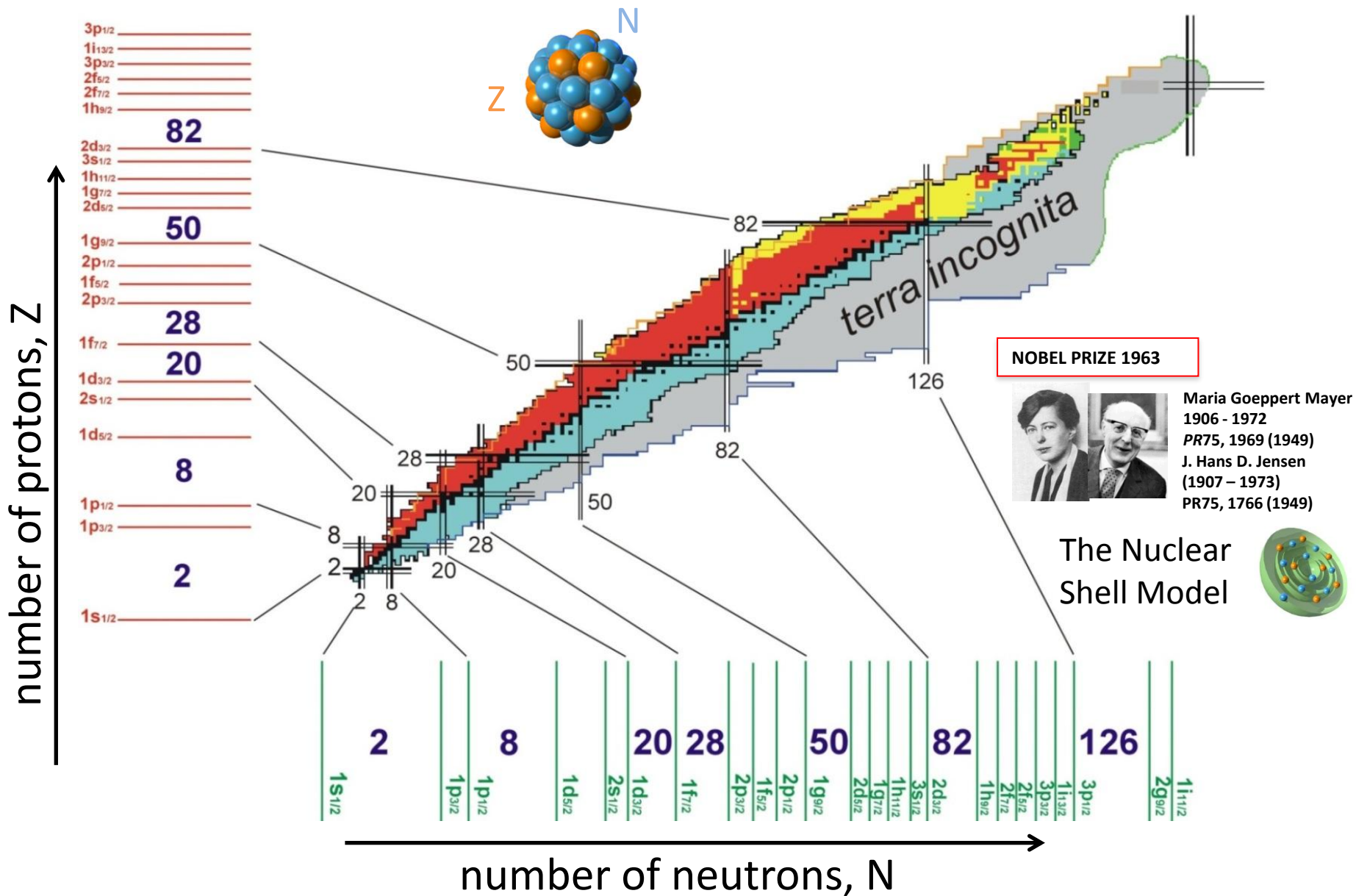
## **The AGATA array of segmented HPGe detectors**

1. Implementation of Pulse Shape Analysis and Tracking concepts
2. The AGATA detectors and preamplifiers
3. The structure of electronics and data acquisition
4. Digital signal processing (at high counting rate)
5. (AGATA data processing)

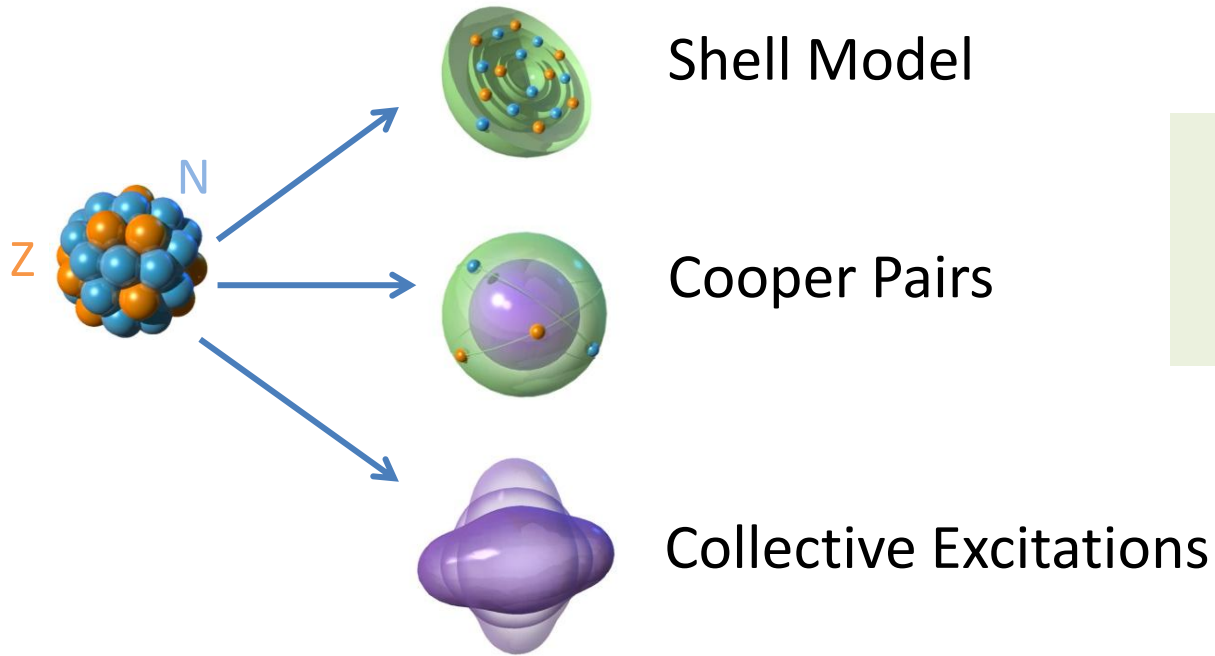
**AGATA+VAMOS (magnetic spectrometer) at GANIL**

*(be aware ... personal 😊selection of topics!)*

# The Atomic Nucleus

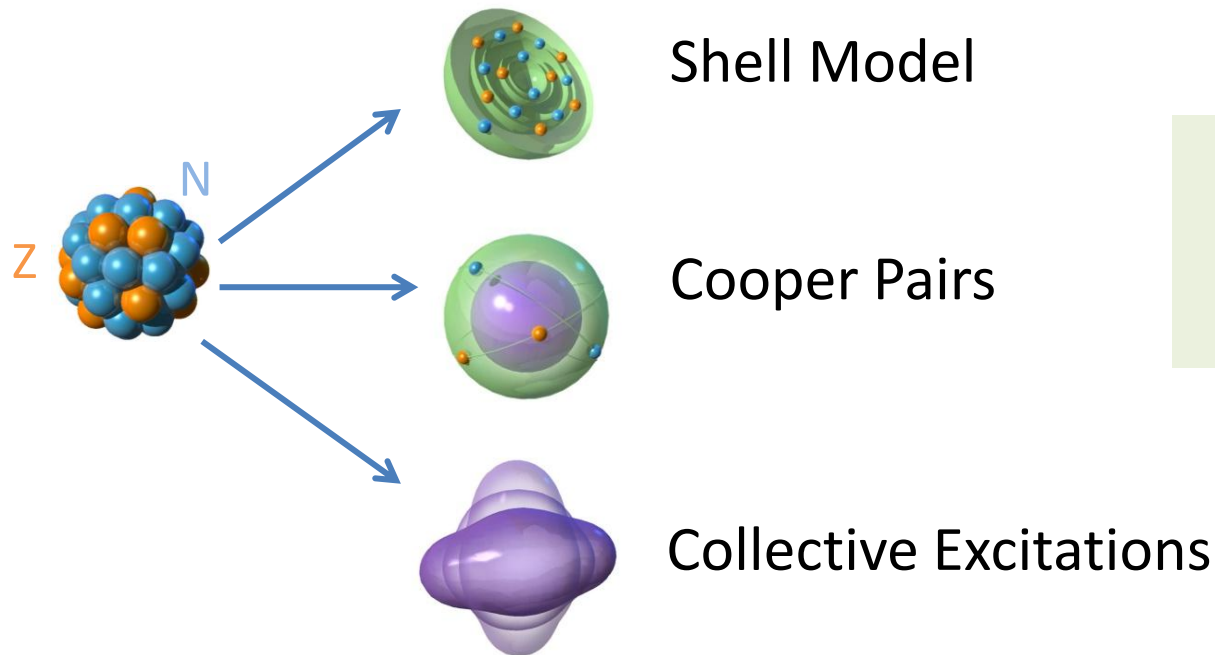


# Nuclear Excitations



Need to tune model parameters collecting nuclear experimental information

# Nuclear Excitations



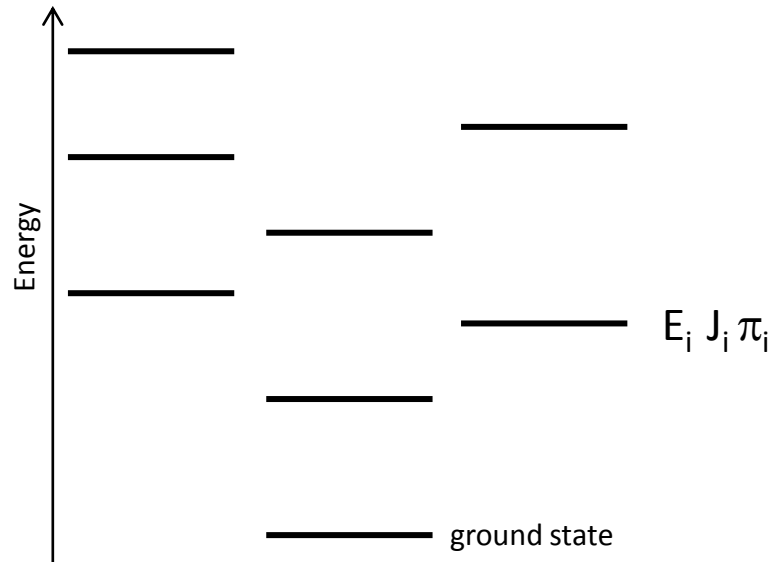
Need to tune model parameters collecting nuclear experimental information

Test of nucleon-nucleon interaction  
by comparing the experimental results to model prediction

What is the effective nucleon-nucleon interaction?  
What are the limits of existence for bound nuclei (*driplines*) ?



# The Structure of the Nucleus

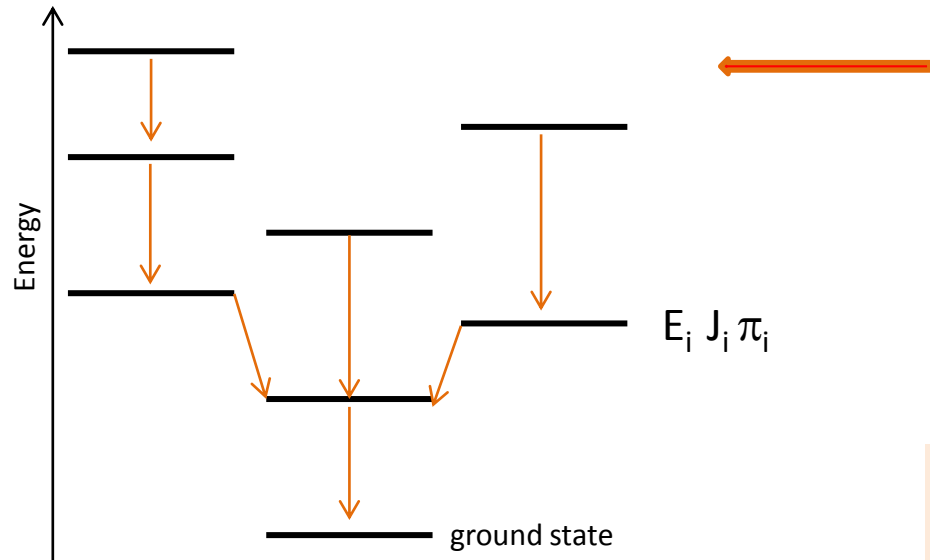


- ✓ systematics (e.g. shape transitions)
- ✓ benchmarks for nuclear models (e.g. Nuclear Shell Model)

Observables:

- ✓ energy levels ( $E_i$ )
- ✓ spin ( $J_i$ )
- ✓ parity ( $\pi_i$ )
- ✓ lifetime (transition probabilities) ( $\tau_i$ )
- ✓ nuclear moments (g-factors)

# The Structure of the Nucleus



populate in excited state(s) and observe  $\gamma$  ray de-excitation radiation

$\gamma$  ray spectroscopy is an approach for the study of nuclear structure

- ✓ systematics (e.g. shape transitions)
- ✓ benchmarks for nuclear models (e.g. Nuclear Shell Model)

Observables:

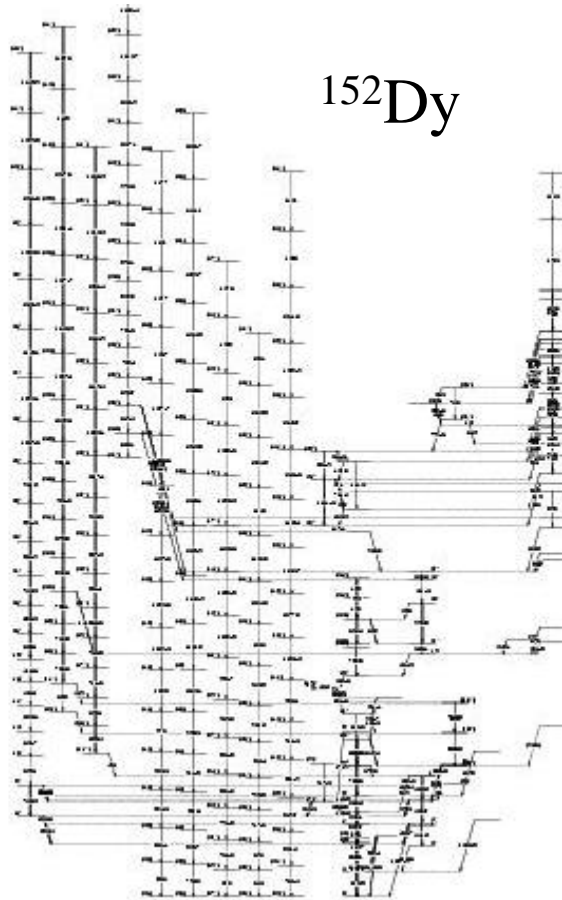
- ✓ energy levels ( $E_i$ )
- ✓ spin ( $J_i$ )
- ✓ parity ( $\pi_i$ )
- ✓ lifetime (transition probabilities) ( $\tau_i$ )
- ✓ nuclear moments (g-factors)

Measuring  $\gamma$ -ray:

- ✓ energy
- ✓ angular distribution
- ✓ linear polarization
- ✓ energy Doppler shift (for example)
- ✓ angular distribution vs t

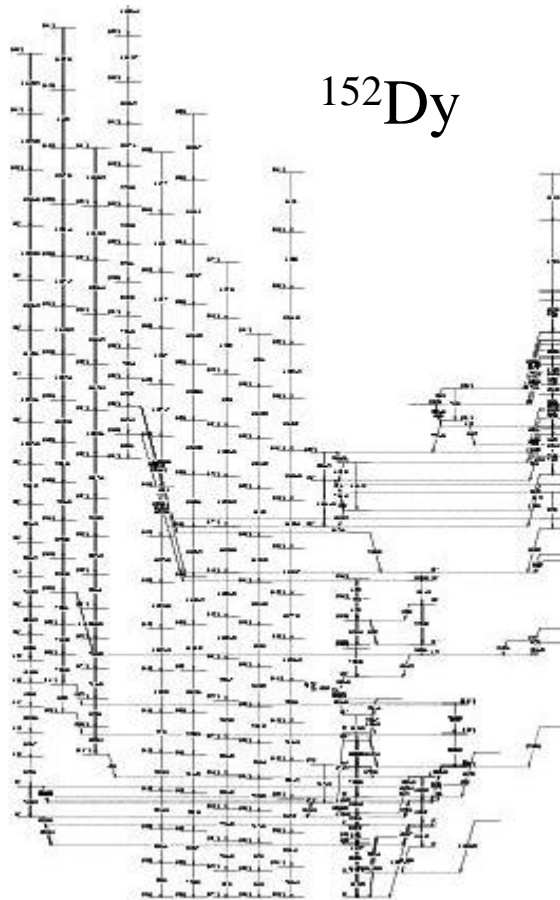
# Level schemes vs Energy spectra

What we want ...

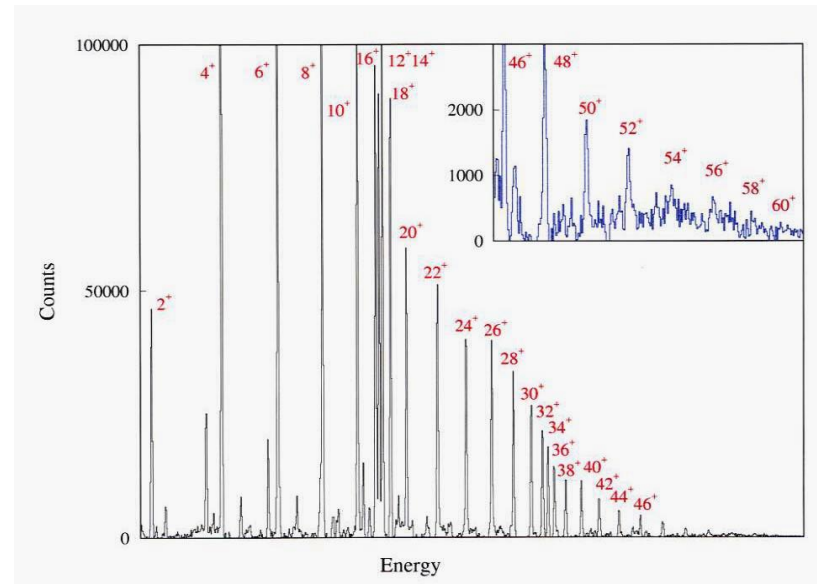


# Level schemes vs Energy spectra

What we want ...



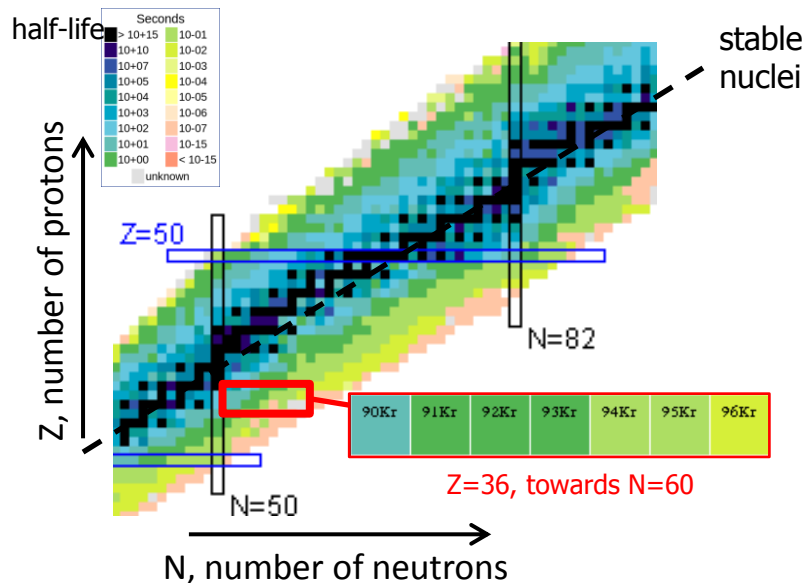
What we get ...



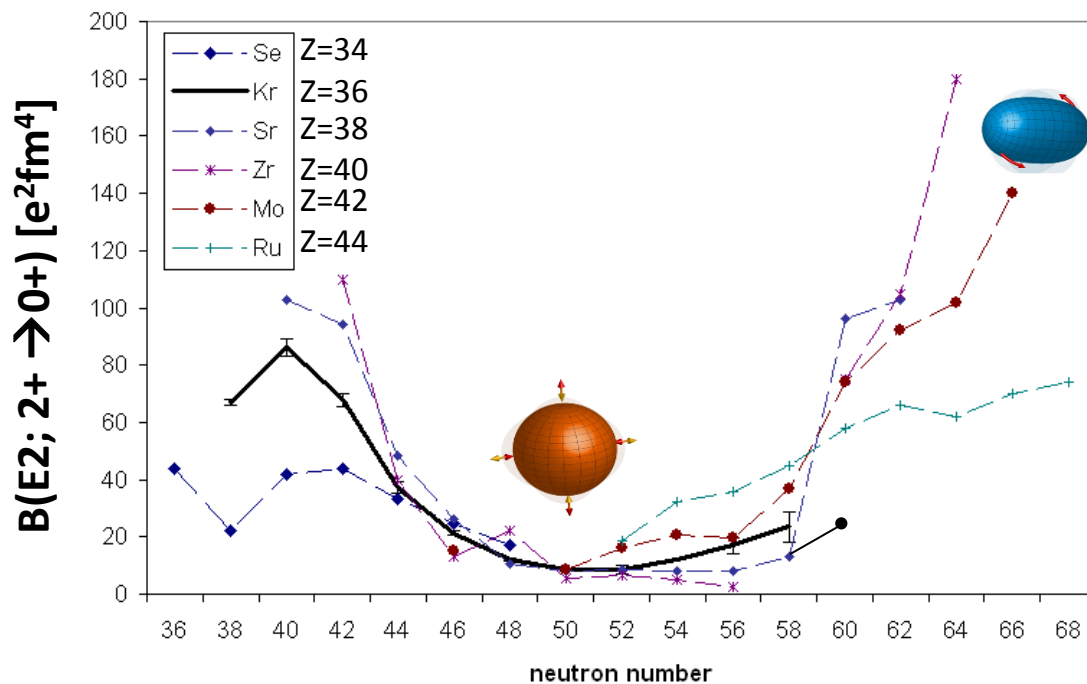
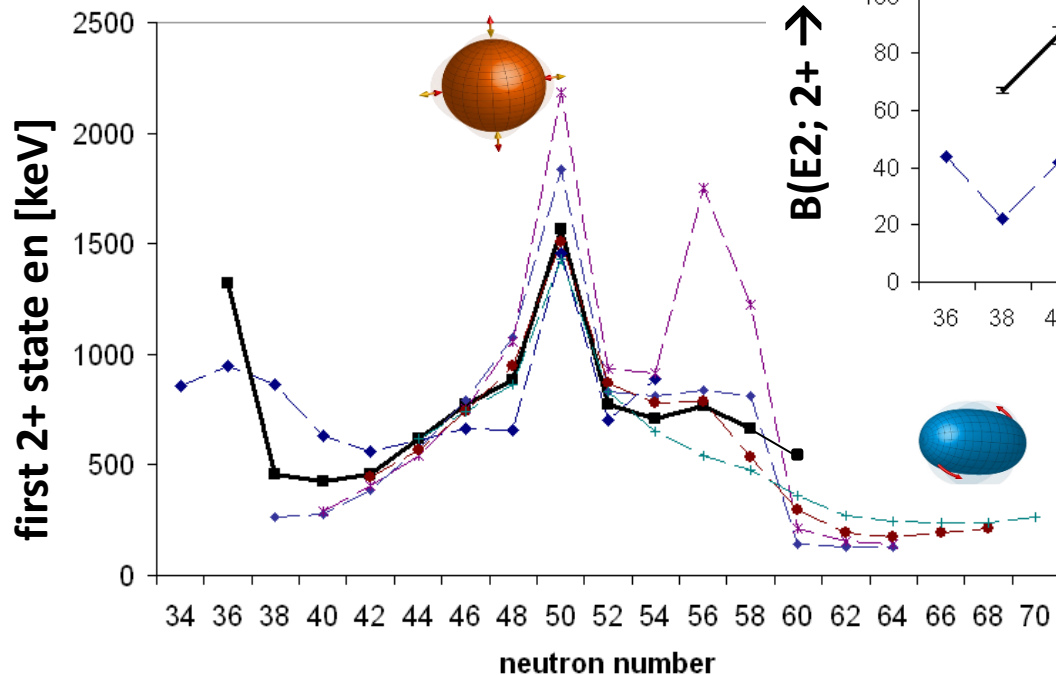
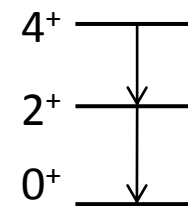
"Allegoria della pazienza"  
G. Vasari

Analysis of complex spectra  
with many lines close in energy

# Nuclear deformation in the $A \sim 100$ region

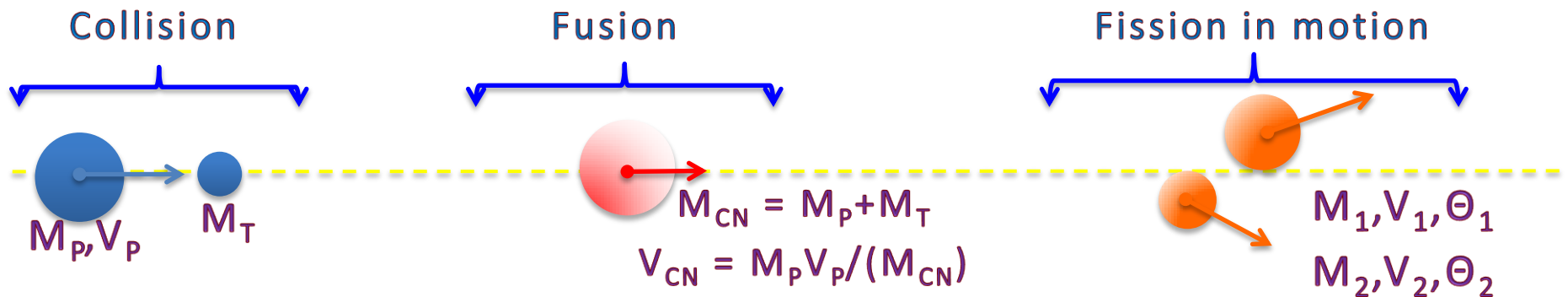


Nuclear shape evolution in the neutron-rich Kr isotopes



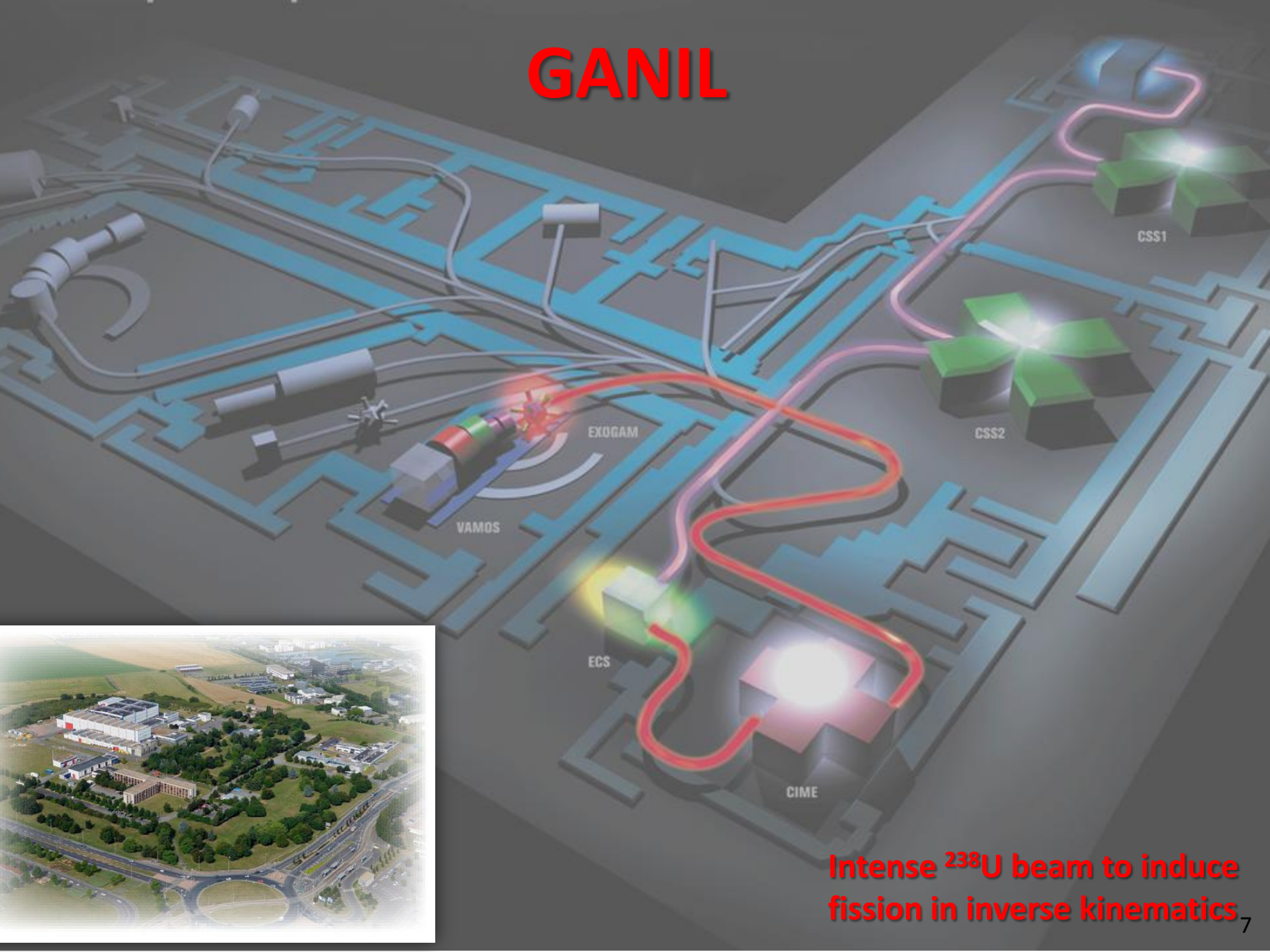
M. Albers et al., Phys. Rev. Lett. 108, 062701, "Evidence of a smooth onset of deformation in the neutron-rich Kr isotopes"

# $\gamma$ -ray spectroscopy of neutron-rich isotopically-identified fission fragments



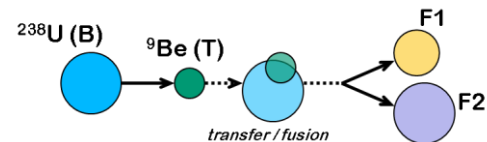
Gamma ray detector + mass spectrometer

# GANIL

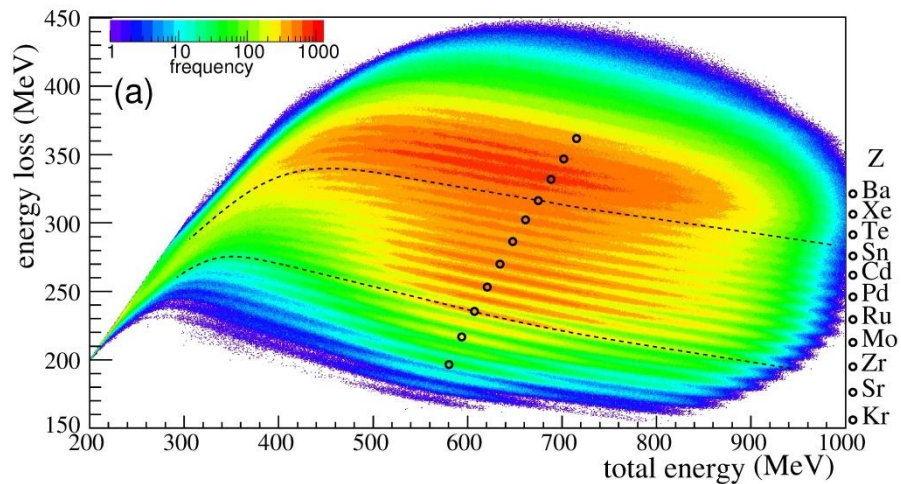


Intense  $^{238}\text{U}$  beam to induce fission in inverse kinematics

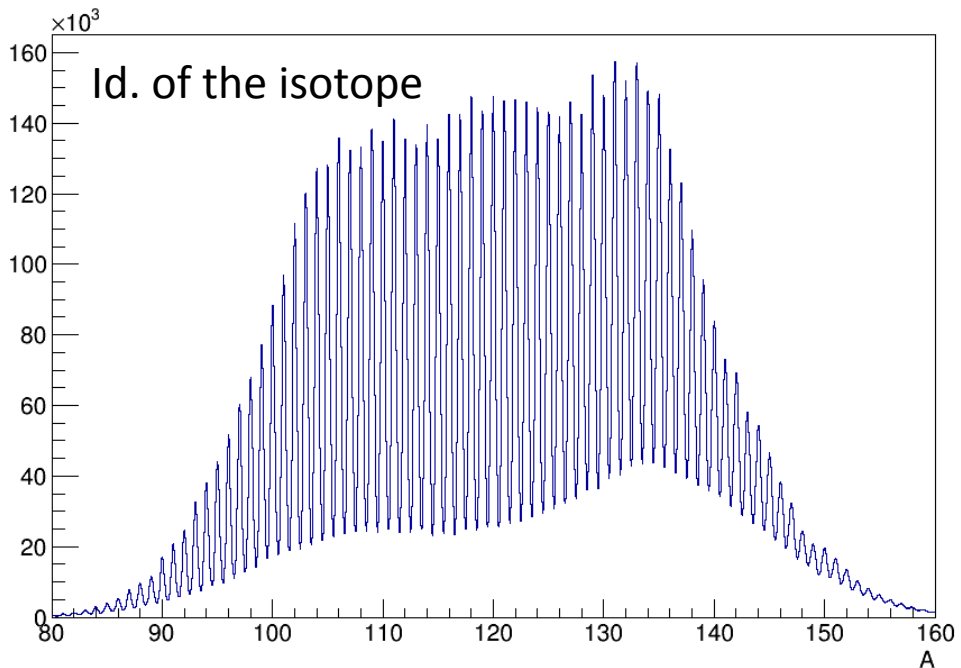
# $^{238}\text{U}$ beam (@ 6.2 MeV/A) on $^9\text{Be}$ target



Id. of the element



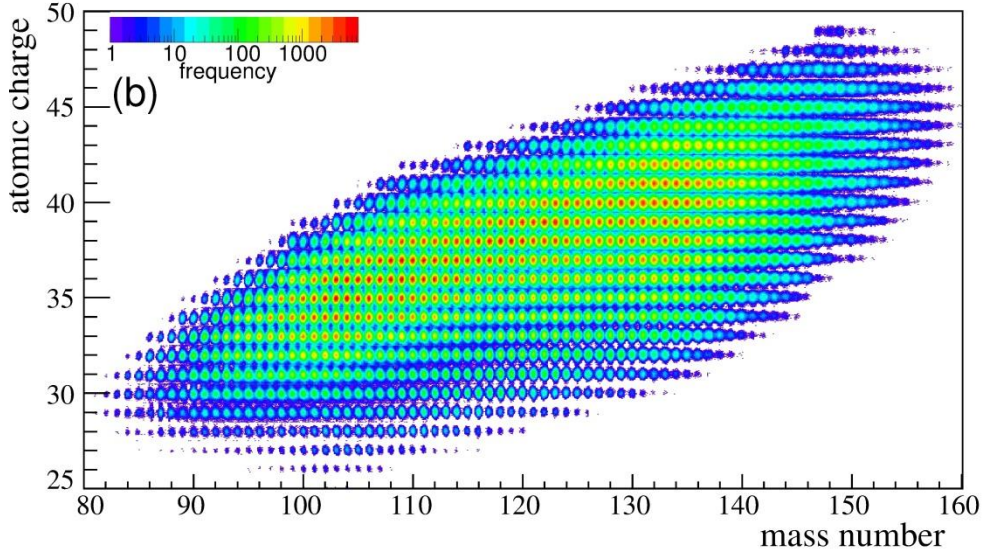
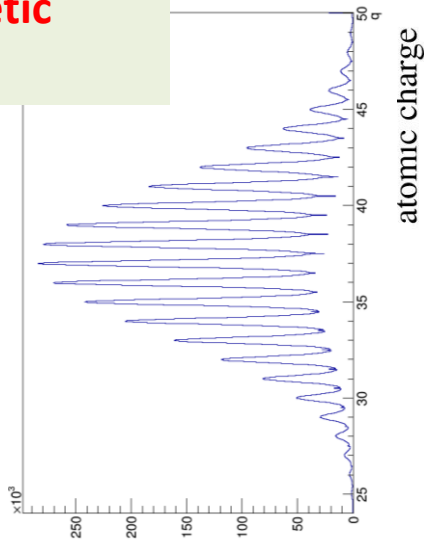
Id. of the isotope



**Isotopic identification event-by-event in the magnetic spectrometer**

A. Navin et al.,  
*Phys. Lett. B* **278**, 136 (2014)

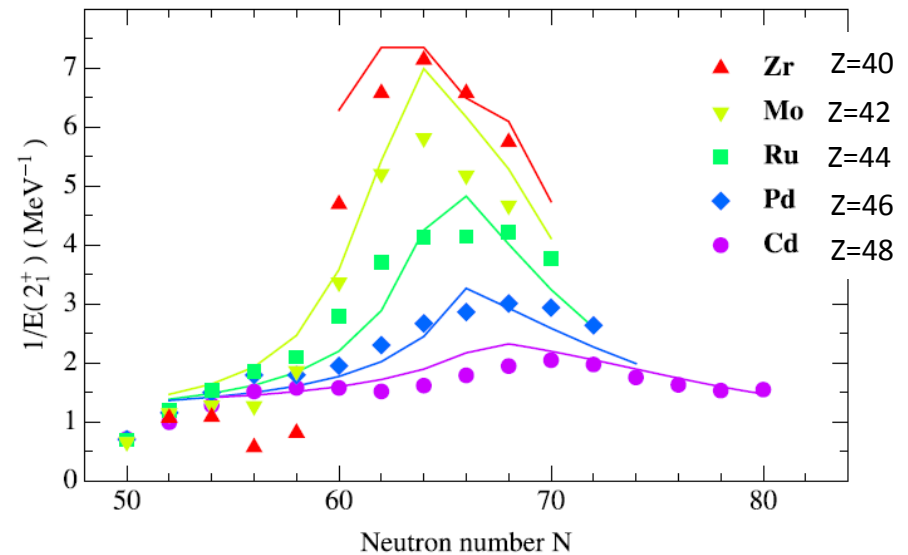
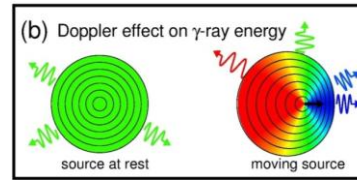
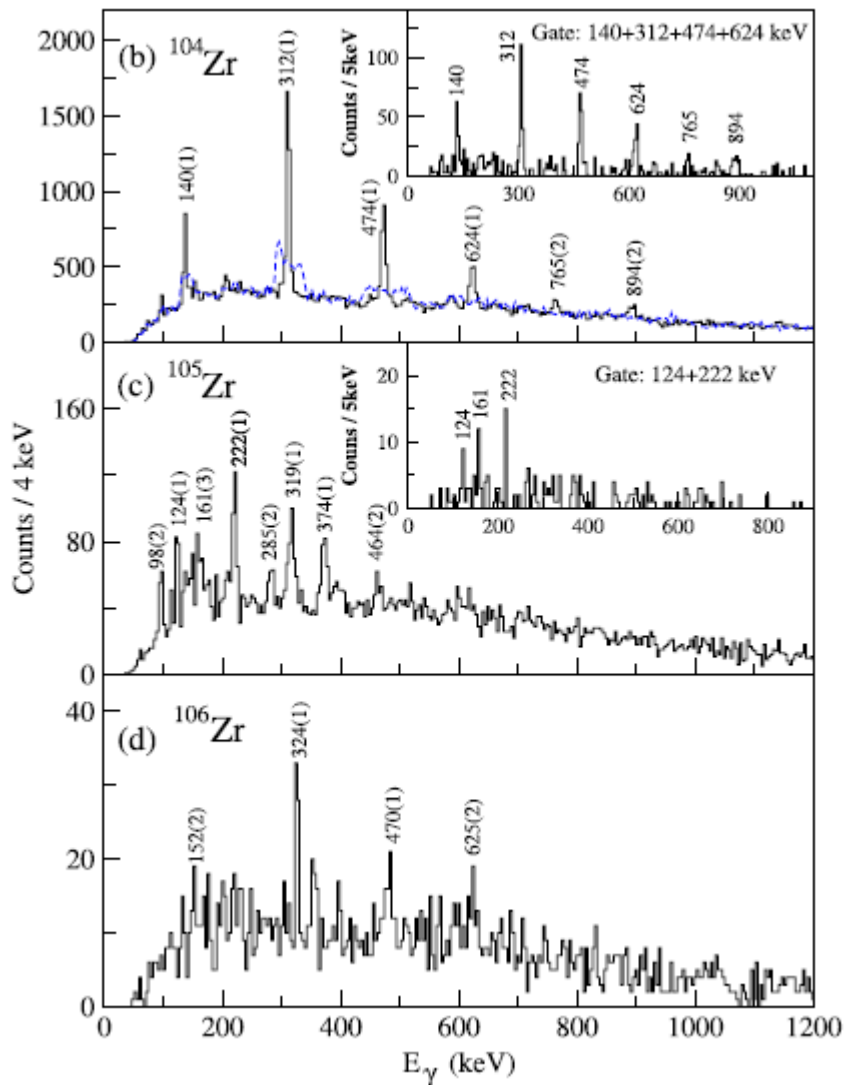
Courtesy of M. Rejmund



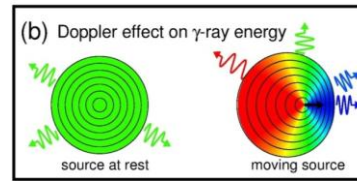
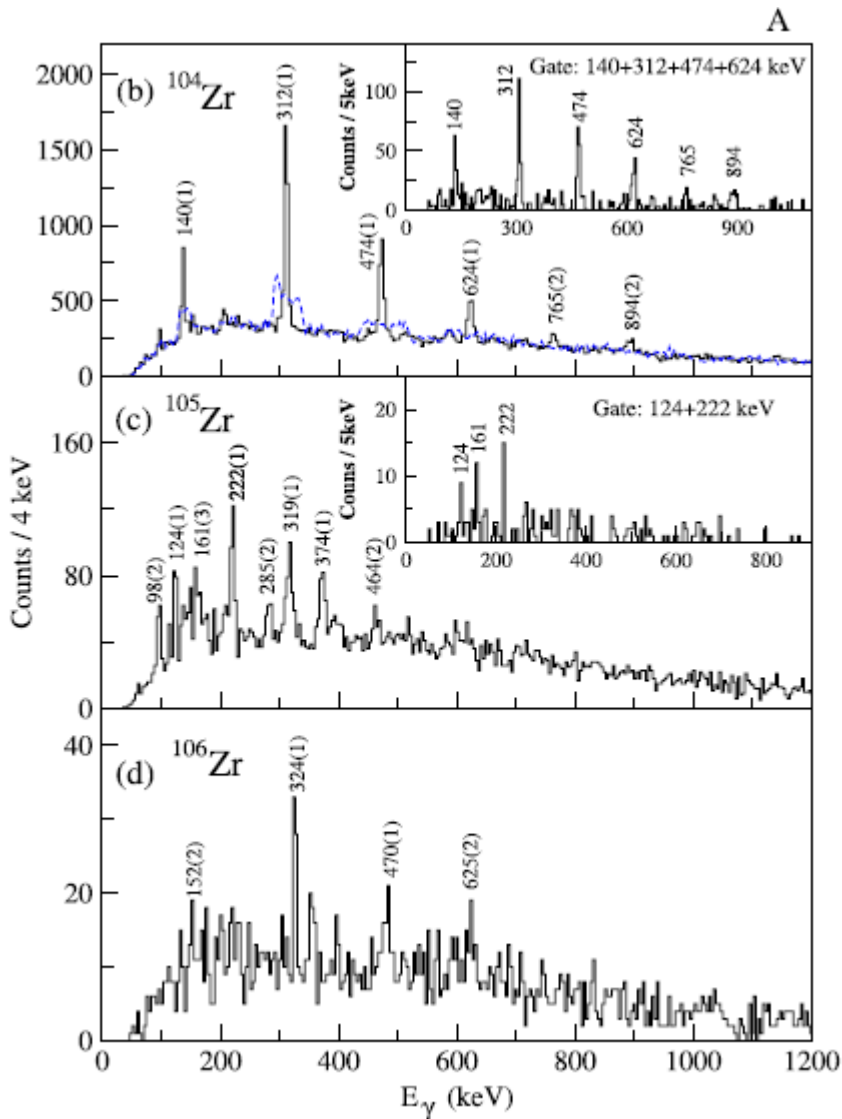


# Collectivity in neutron-rich Zr nuclei

A

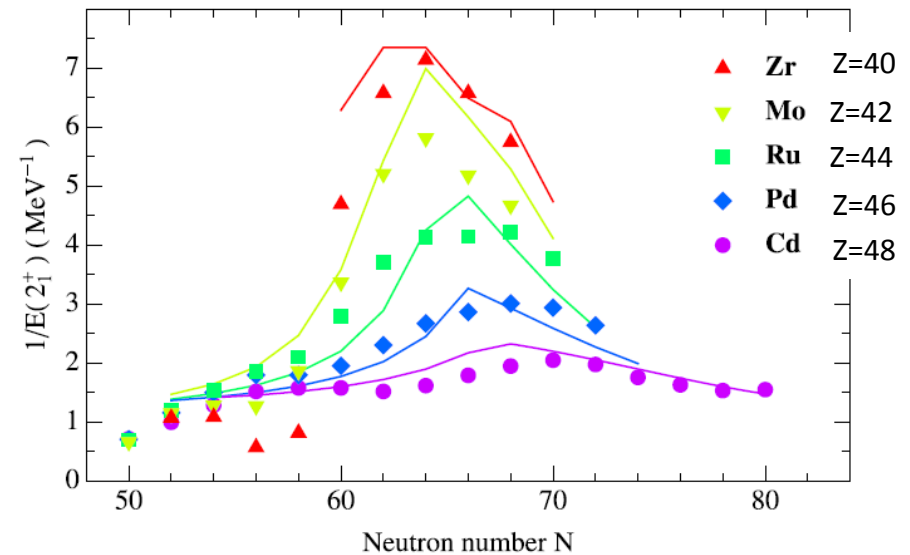


# Collectivity in neutron-rich Zr nuclei



How we can do better?

- ✓ Low energy gamma rays
- ✓ Resolution (EXOAM: 8 keV at 1.2 MeV)
- ✓ Gamma linear polarization measurements
- ✓ ...



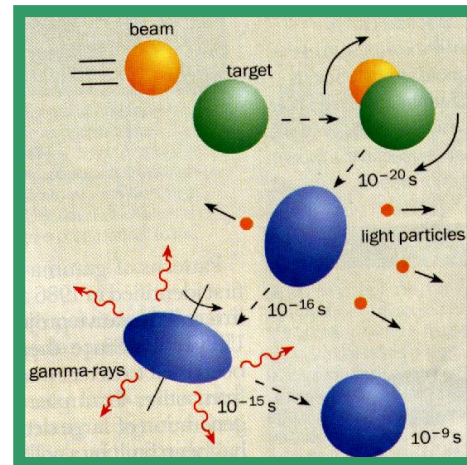
# In-beam $\gamma$ -ray spectroscopy: requirements

**Energy resolution** ( $E_\gamma \sim 10 \text{ keV} - 10 \text{ MeV}$ ),  
in order to disentangle complex spectra

→ germanium detectors

**Peak to Total ratio** (large continuous Compton background),  
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→ Compton background suppression



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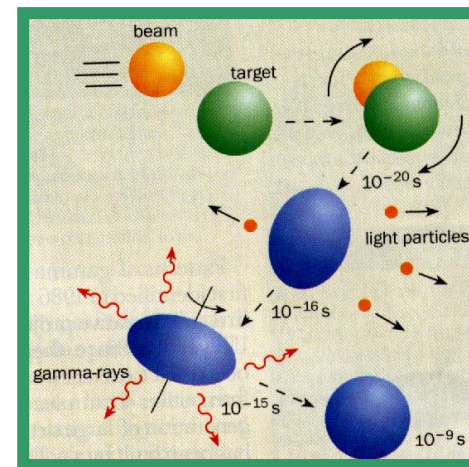
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energy resolution dominated by Doppler broadening if the velocity vector and the emission angle of the  $\gamma$ -ray are not well known ( $\beta \sim 5\text{-}10\%$ , up to 50%)



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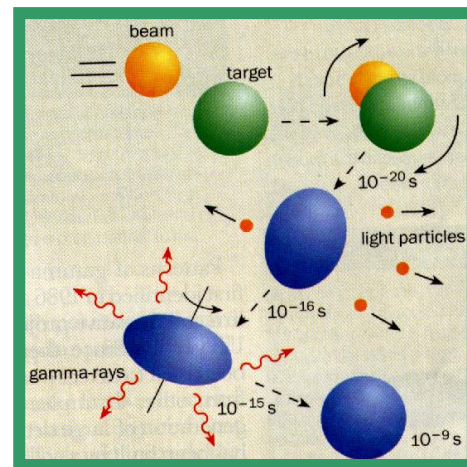
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**Good solid angle coverage** (ideally  $4\pi$ ), in order to maximize efficiency

**Good granularity ,**

in order to reduce multiple hits on the detectors for high  $\gamma$ -ray multiplicity events

**Avoid dead materials** that could absorb radiation (→ preserve low energies)



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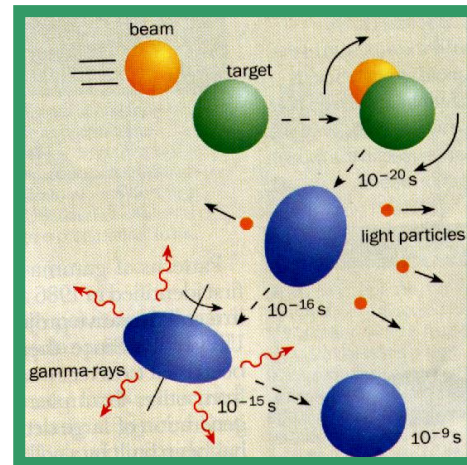
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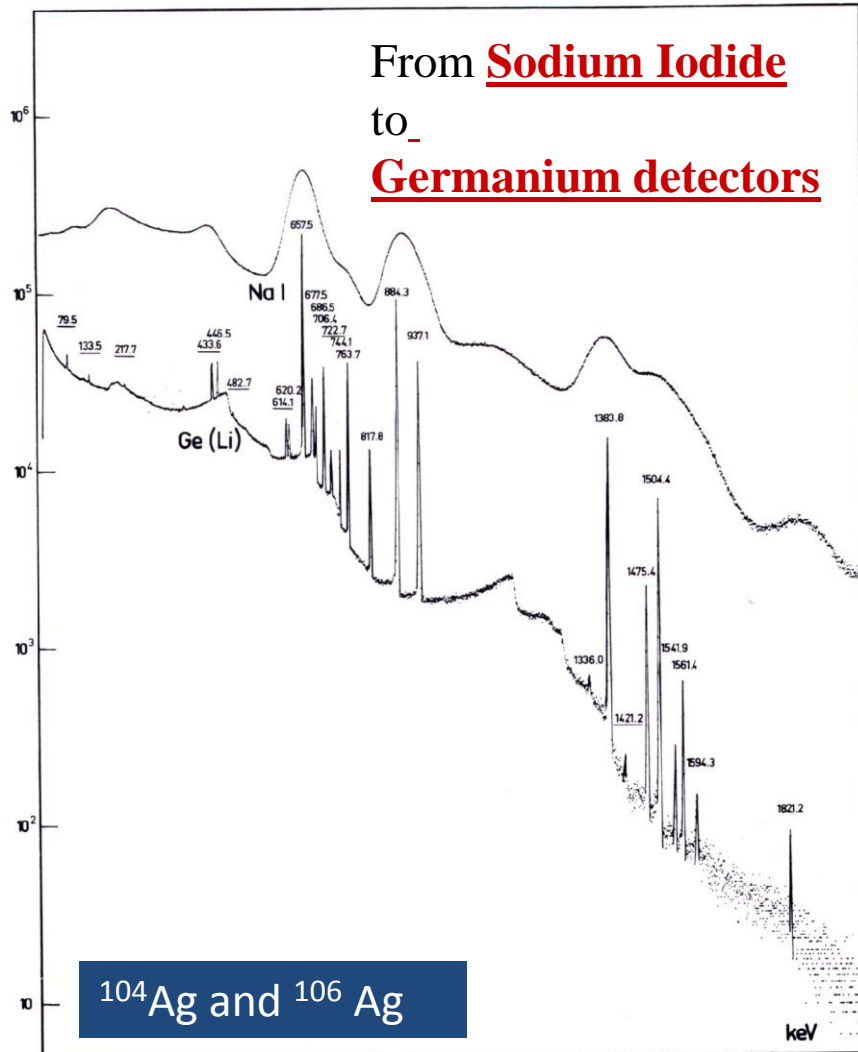
**Avoid dead materials** that could absorb radiation (→ preserve low energies)

**High counting rate capability** (frequently background much stronger than channel of interest)

**Time resolution** (prompt events selection, lifetimes)



# Energy resolution



*Response function = differential spectrum obtained with a detector when hit by monochromatic radiation*

60's → Use of Ge(Li) detectors marks the beginning of high-resolution in-beam  $\gamma$ -ray spectroscopy

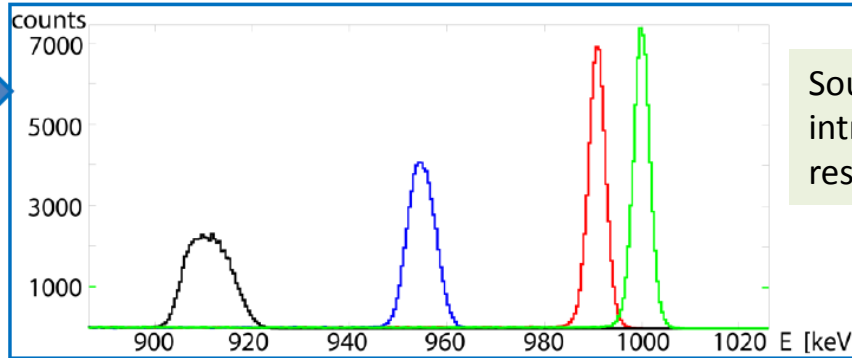
70's → Only few detectors, operated in  $\gamma$ - $\gamma$  coincidence. Development of the HP-Ge detector.

**Use of Germanium detectors = breakthrough in nuclear structure**

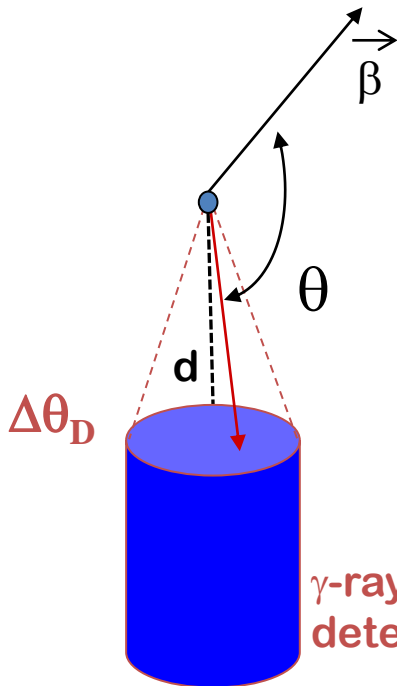
FWHM = 2 keV at 1.3 MeV

# Doppler broadening: effective energy resolution

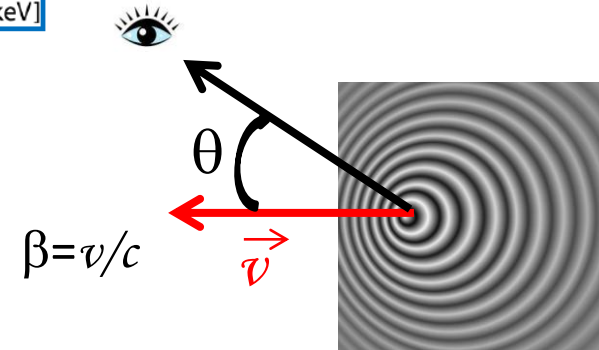
$E_0 = 1\text{MeV}$   
 $\beta = 0, 0.01, 0.05, 0.10$   
 (fixed direction)  
 $\theta = 158\text{ deg}$



Source at rest →  
intrinsic energy  
resolution



$$E_{\gamma}^{\text{Lab}}(\theta) = E_{\gamma}^{\text{CM}} \frac{\sqrt{1 - \beta^2}}{1 - \beta \cdot \cos \theta}$$

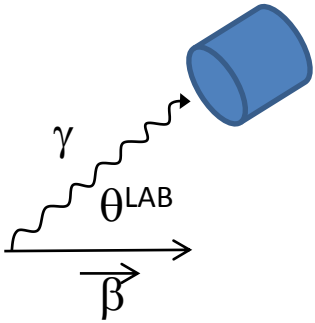


## Efficiency vs Resolution:

Small  $d$  ↔ Large  $\Omega$  ↔ High eff ↔ Poor FWHM  
 Large  $d$  ↔ Small  $\Omega$  ↔ Low eff ↔ Good FWHM



# Doppler broadening: effective energy resolution



$E_\gamma$	1 MeV	
$\Delta E_{\text{lab}}$	$v(1.2+0.003 \cdot E_{\text{lab}})$	
$\beta(\%)$	$5 \pm 0.01$	$20 \pm 0.005$
$\Delta\Theta(\text{deg})$	8	2

$$E_\gamma^{\text{Lab}} = E_\gamma^{\text{CM}} \frac{\sqrt{1 - \beta^2}}{1 - \beta \cdot \cos \theta^{\text{Lab}}}$$

$$E_\gamma^{\text{CM}} = E_\gamma^{\text{Lab}} \frac{1 - \beta \cdot \cos \theta^{\text{Lab}}}{\sqrt{1 - \beta^2}}$$

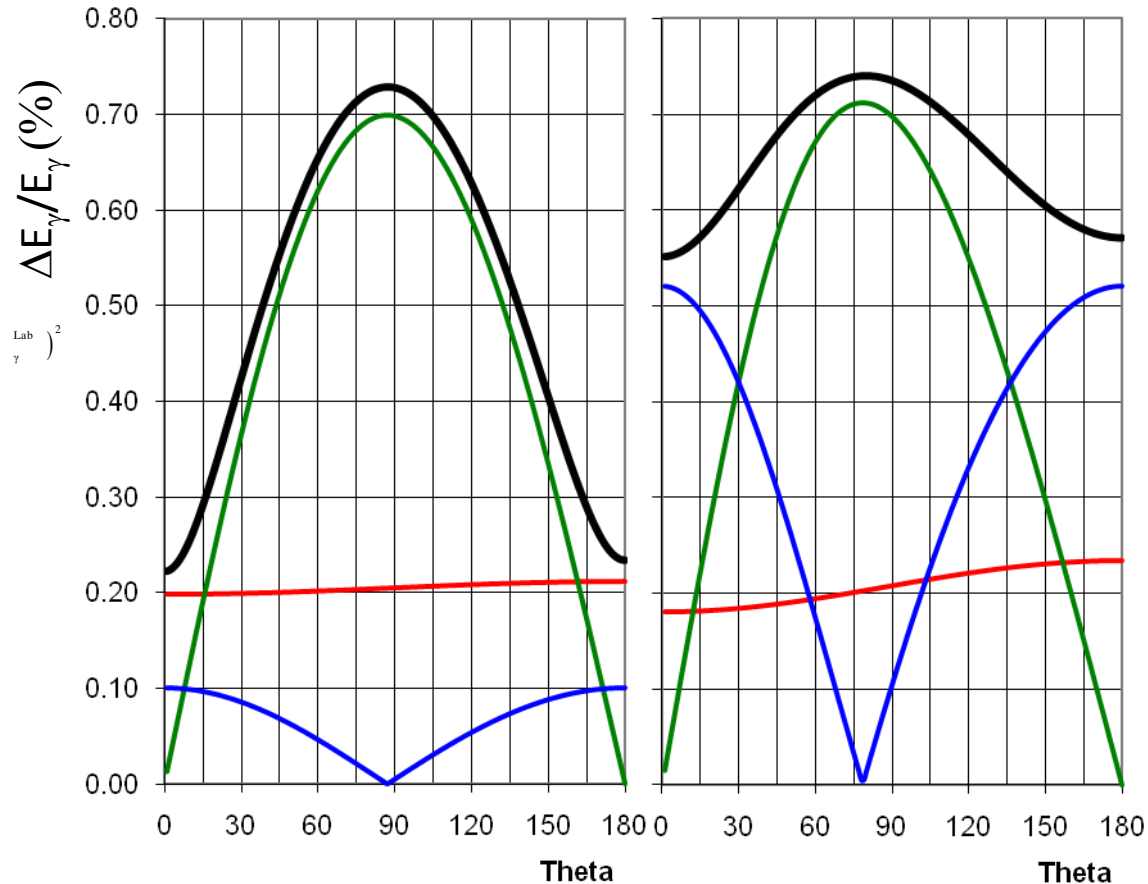
$$(\Delta E_\gamma^{\text{CM}})^2 = \left( \frac{\partial E_\gamma^{\text{CM}}}{\partial \theta^{\text{Lab}}} \right)^2 (\Delta \theta^{\text{Lab}})^2 + \left( \frac{\partial E_\gamma^{\text{CM}}}{\partial \beta} \right)^2 (\Delta \beta)^2 + \left( \frac{\partial E_\gamma^{\text{CM}}}{\partial E_\gamma^{\text{Lab}}} \right)^2 (\Delta E_\gamma^{\text{Lab}})^2$$

$$\left( \frac{\Delta E_\gamma^{\text{CM}}}{E_\gamma^{\text{CM}}} \right)^2 = \left( \frac{\beta \cdot \sin \theta^{\text{Lab}}}{1 - \beta \cdot \cos \theta^{\text{Lab}}} \right)^2 (\Delta \theta)^2 + \left( \frac{\beta - \cos \theta^{\text{Lab}}}{(1 - \beta^2)(1 - \beta \cdot \cos \theta^{\text{Lab}})} \right)^2 (\Delta \beta)^2 + \left( \frac{\Delta E_\gamma^{\text{Lab}}}{E_\gamma^{\text{Lab}}} \right)^2$$

Opening

Recoil

Intrinsic



# Photon interaction with matter

~ 100 keV

~1 MeV

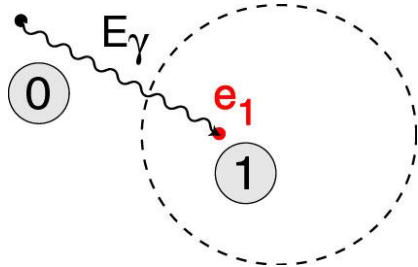
~ 10 MeV

γ ray energy

**Photoelectric**

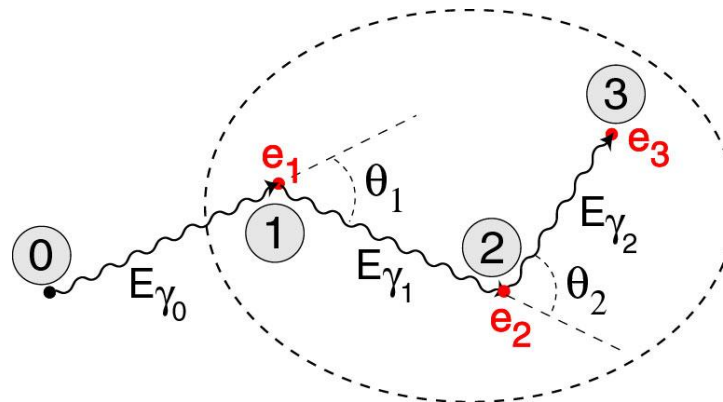
**Compton Scattering**

**Pair Production**

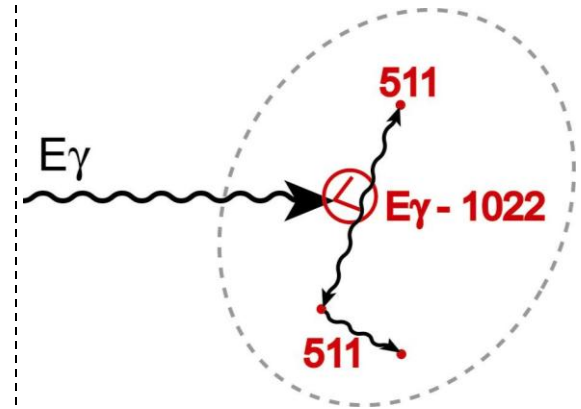


$$E_{e1} = E_{\gamma} - E_b$$

$$\sigma \propto \frac{Z^n}{E_{\gamma}^{3.5}}, \quad n \approx 4 \div 5$$



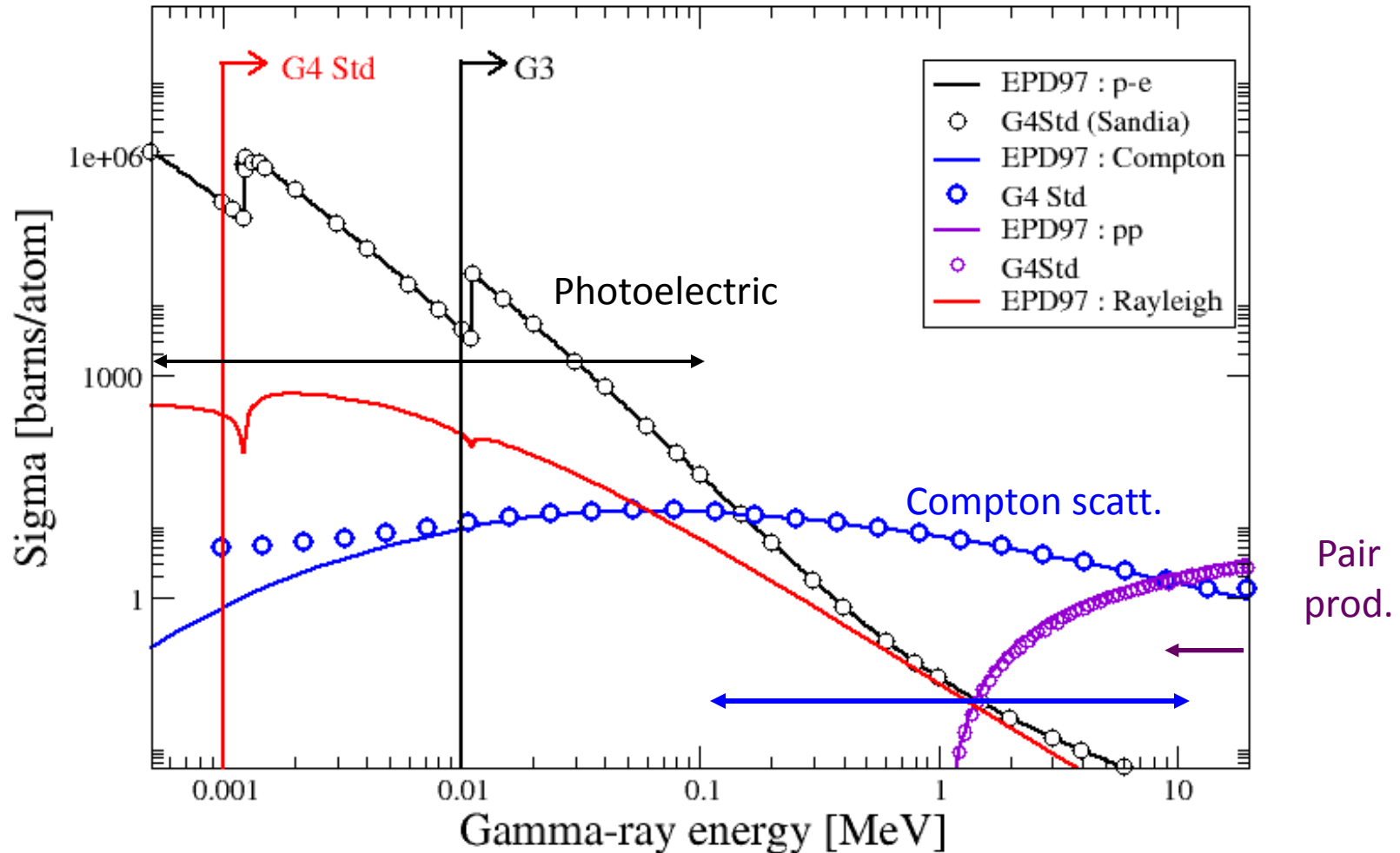
$$E_{\gamma'} = \frac{E_{\gamma}}{1 + \frac{E_{\gamma}}{m_0 c^2} (1 - \cos \theta)}$$



$$(E_{\gamma} > 2m_e c^2)$$

$$\sigma \propto Z^2$$

# Cross Sections in Germanium

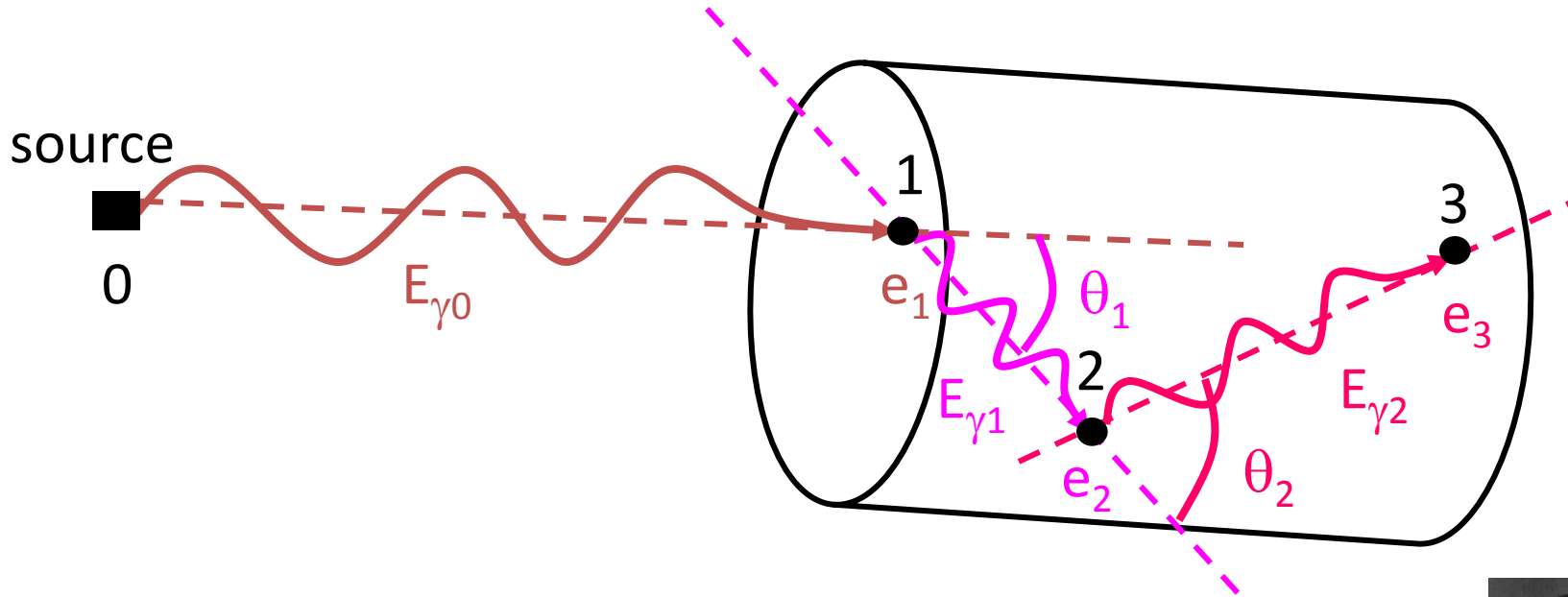


Mean free path:  $\lambda(E) = M_A / (N_{AV} \cdot \rho) \cdot 1 / \Sigma \sigma_E$

$\lambda(10 \text{ keV}) \sim 55 \text{ } \mu\text{m}$        $\lambda(100 \text{ keV}) \sim 0.3 \text{ cm}$        $\lambda(200 \text{ keV}) \sim 1.1 \text{ cm}$

$\lambda(500 \text{ keV}) \sim 2.3 \text{ cm}$        $\lambda(1 \text{ MeV}) \sim 3.3 \text{ cm}$

# Compton Scattering (1)



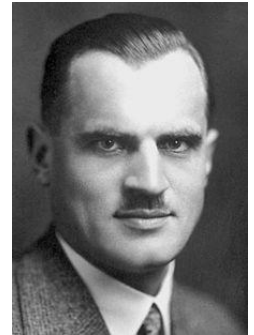
assuming that the  $e^-$  is at rest,  
from conservation of energy and momentum:

$$E_{\gamma i} = \frac{E_{\gamma i-1}}{1 + \frac{E_{\gamma i-1}}{m_0 c^2} (1 - \cos \theta_i)}$$

$$e_i = E_{\gamma i-1} - E_{\gamma i}$$

Energy of scattered  $\gamma$

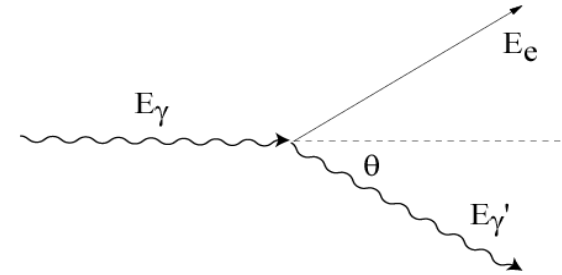
Energy of scattered  $e^-$



Arthur Holly Compton  
Nobel prize 1927

# Compton Scattering (2)

The angular distribution of the scattered photon is described by the **Klein-Nishina** formula:

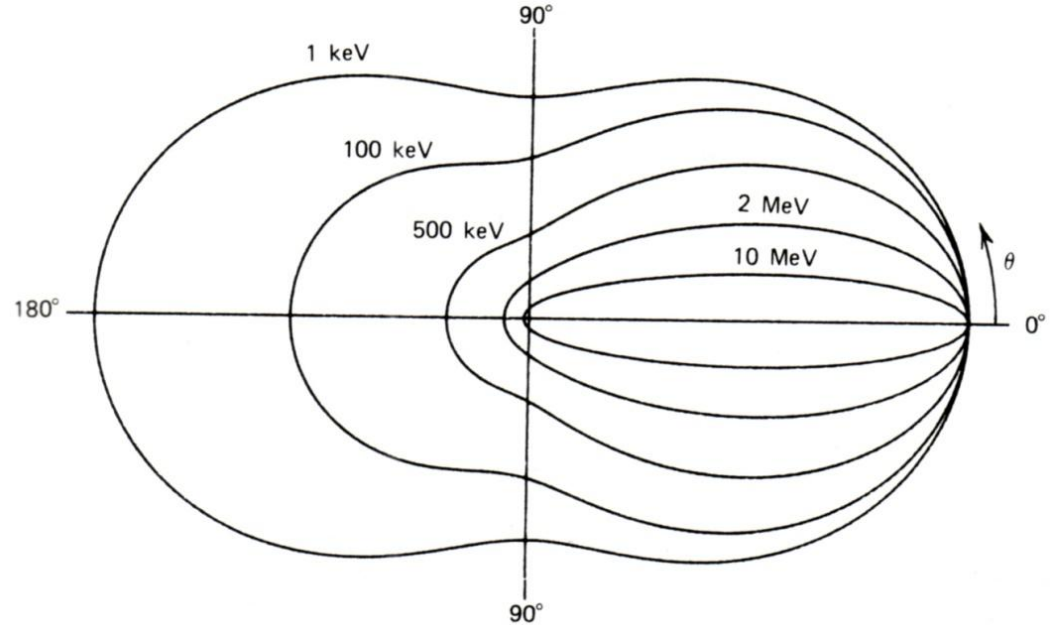


$$\frac{d\sigma}{d\Omega} = z r_e^2 \left( \frac{1}{1 + \alpha (1 - \cos \theta)} \right)^2 \left( \frac{1 + \cos^2 \theta}{2} \right) \left( 1 + \frac{\alpha^2 (1 - \cos \theta)^2}{(1 + \cos^2 \theta)[1 + \alpha (1 - \cos \theta)]} \right)$$

$$\alpha = E_\gamma / m_e c^2$$

and  $r_e$  is the classical electron radius

For  $E_\gamma >$  few 100 keVs the angular distribution is highly anisotropical and peaked to small forward angles. It strongly “focuses” with the increasing photon energy.

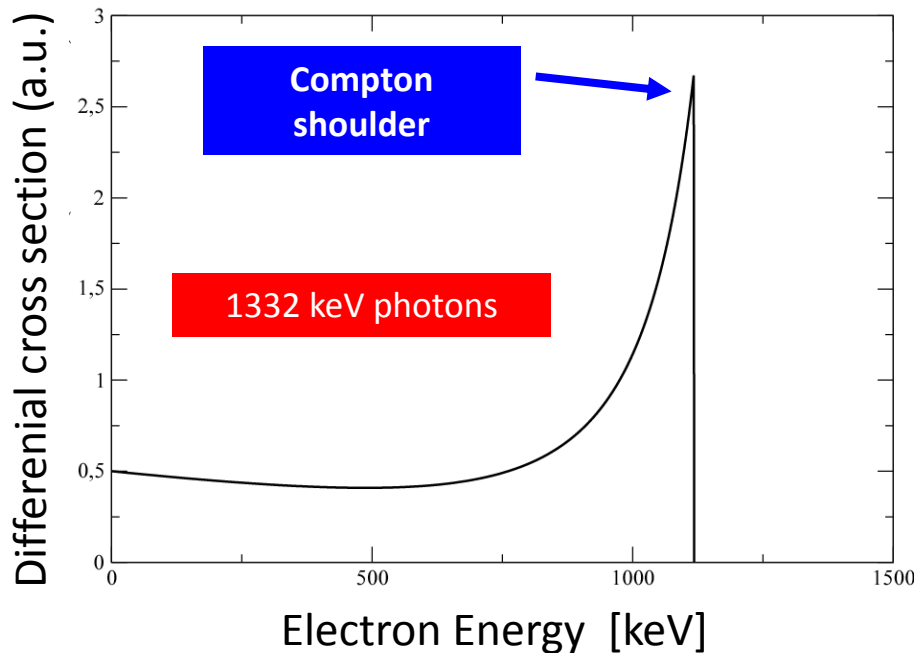


# Continuum Compton

The spectrum of the scattered electrons can be deduced from the Klein-Nishina formula:

$$\frac{dN}{dE_e} \propto \left( \frac{1 + f^2(E_e)}{2} \right) \left[ 1 + \frac{1}{1 + f^2(E_e)} \frac{E_e^2}{E_\gamma (E_\gamma - E_e)} \right]$$

$$f(E_e) = 1 - \frac{m_e c^2}{E_\gamma} \frac{E_e}{E_\gamma - E_e}$$

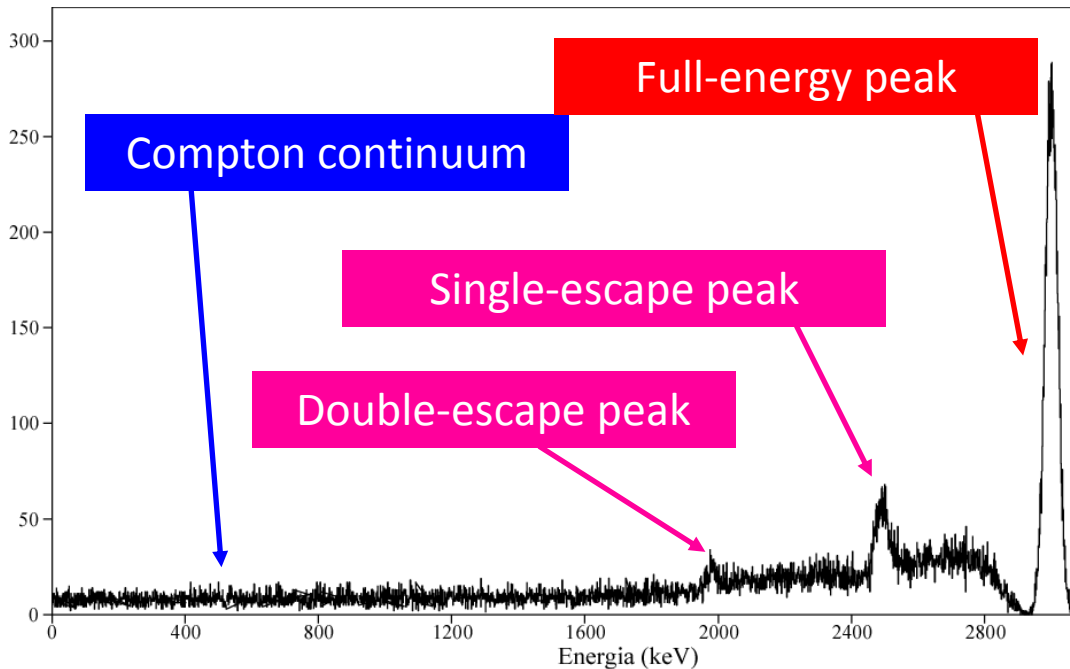


Since the actual energy deposition is performed by the electrons, photons interacting via Compton scattering will produce a continuum.

Corrections are needed since electrons are not free, rather bound in materials, producing a smoothing of the actual spectrum

(Compton profile)

# Shape of the $\gamma$ spectrum for a typical size Ge detector



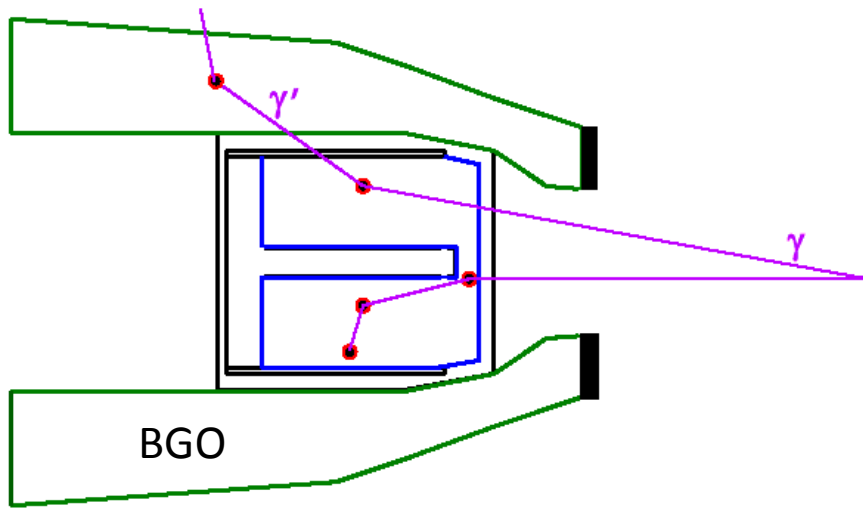
$E_\gamma = 3 \text{ MeV}$

HPGe detector used  
with the GASP array  
(LNL)



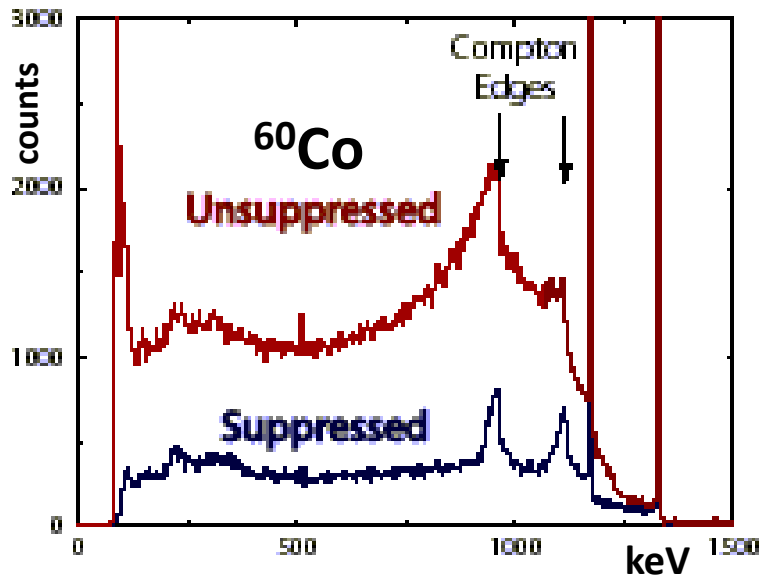
High probability that the incoming photons are only partially absorbed.  
Response function: **full-energy peak**, **continuum** generated by photons which underwent Compton scattering and, if the photon energy is larger than 1.022 MeV, peaks due to the missed detection of one or both the annihilation photons (**single and double escape peaks**).

# Escape-suppressed Ge detectors (Compton suppression)



The cross section for Compton scattering in germanium implies quite a large continuous background in the resulting spectra

For large-volume Ge crystals the Anticoincidence shield (AC) improves the PeakToTotal ratio (P/T) from  $\sim 20\%$  to  $\sim 60\%$



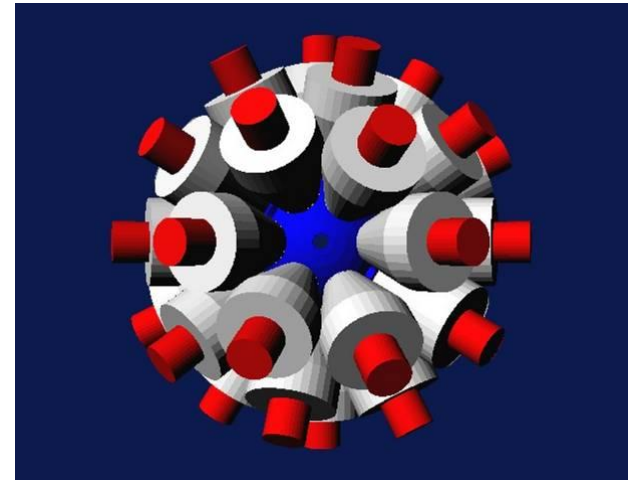
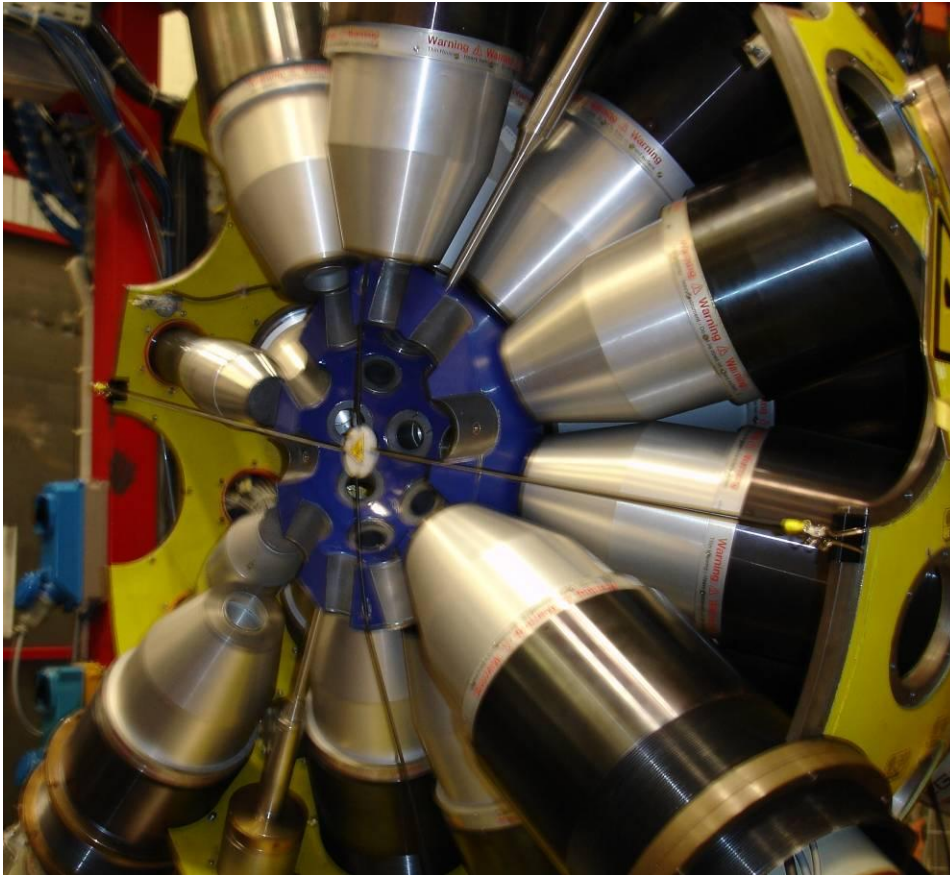
$\gamma_1 \setminus \gamma_2$	P	B
P	PP	PB
B	BP	BB

In a  $\gamma$ - $\gamma$  measurement, the fraction of useful peak-peak coincidence events grows from 4 % to 36%

For high fold (F) coincidences the fraction of useful coincidences is  $P/T^F$



# GASP @ Legnaro Nat. Lab.



- 40 HPGe + AC (config. II)
  - $d_{\text{target-det.}} = 22 \text{ cm}$
  - $\epsilon_{\text{ph}} \sim 5.8\% \text{ @ } 1332.5 \text{ keV}$
- Pb collimator (6 cm thick)
  - inner space  $R_{\text{int}} = 15 \text{ cm}$

Lifetime measurements with Doppler Shift Techniques

7 rings @  $35^\circ$ ,  $60^\circ$ ,  $72^\circ$ ,  $90^\circ$ ,  $108^\circ$ ,  $120^\circ$ ,  $145^\circ$

6    6    4    8    4    6    6

*C. Rossi-Alvarez, Nucl. Phys. News Europe 2 (1993) 10*

*D. Bazzacco, in: Proc. Conf. On Physics from Large g-ray detector arrays, 1992, p. 376*

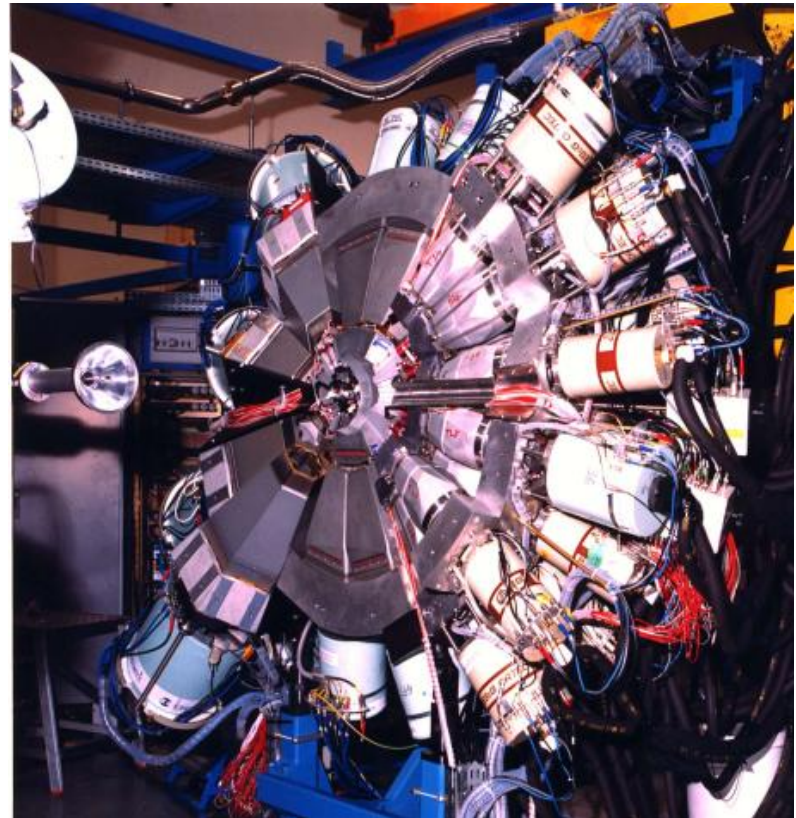
# GAMMASPHERE



up to 110 Compton-Suppressed Ge detectors

*I.Y. Lee, NPA 520 (1990) 641*

# EUROBALL



15 Clusters (7-Ge); 26 Clovers (4-Ge); 30 single Ge

71 CS-systems

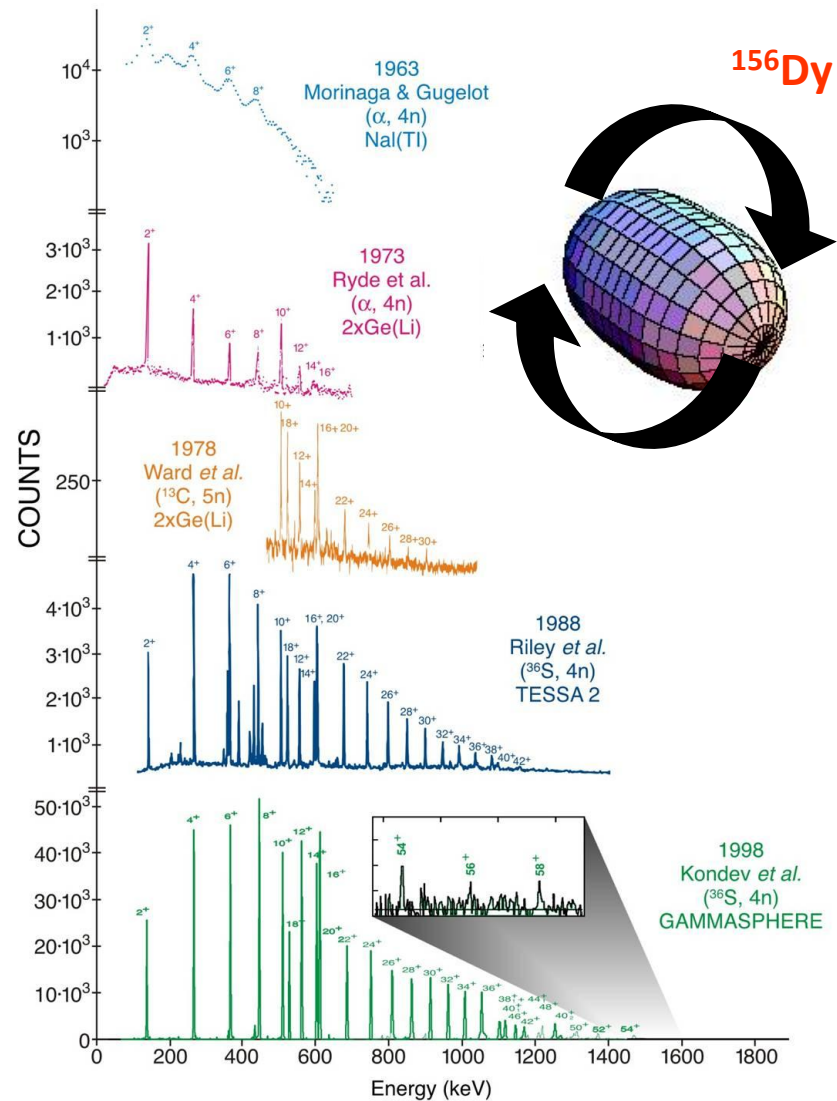
239 Ge crystals

Efficiency	$\epsilon_p \sim 10 - 5 \%$
Peak/Total	PT $\sim 55 - 40 \%$
	( $M_\gamma=1 - M_\gamma=30$ )

Solid angle covered by Ge → 40-50 %

# Spectroscopic history of $^{156}\text{Dy}$

The “spectroscopic history” of  $^{156}\text{Dy}$  is a notable example of how the progress with the acceleration and detection techniques leads to better insight on the nuclear structure.



# *The nucleus is always full of surprises*



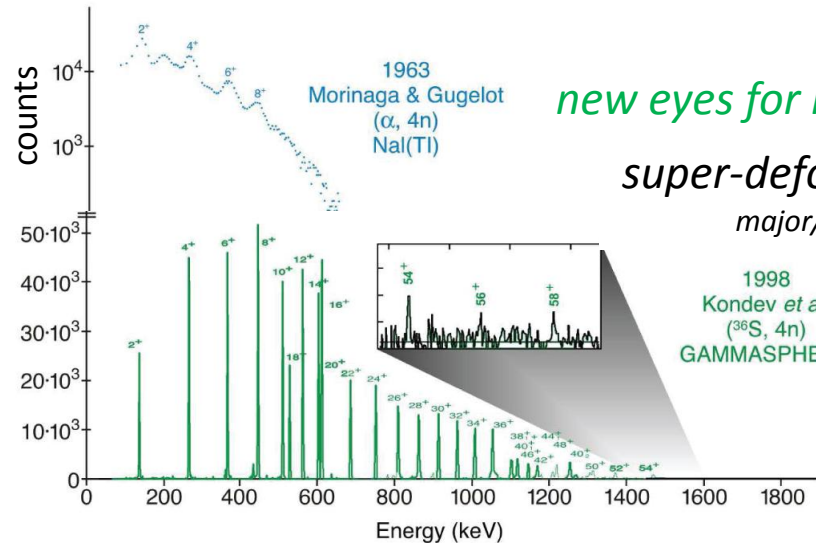
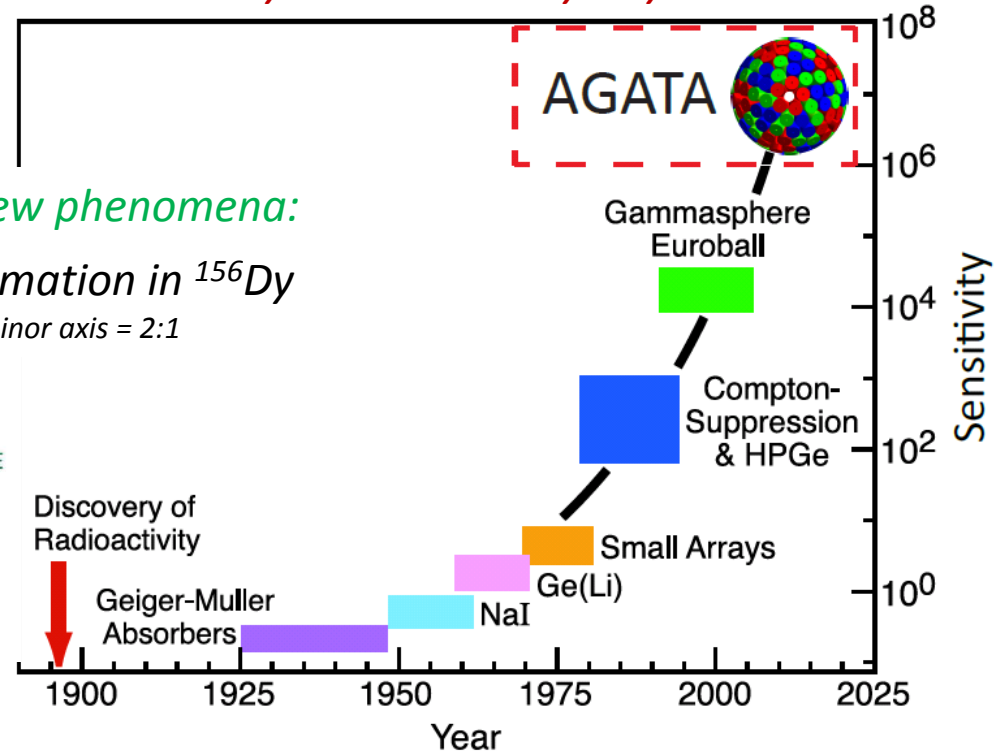
**Instrumentation advances**



**New Science**

# Advances in $\gamma$ -ray spectroscopy: sensitivity vs year

*Ge detector system sensitivity vs year*



*new eyes for new phenomena:*

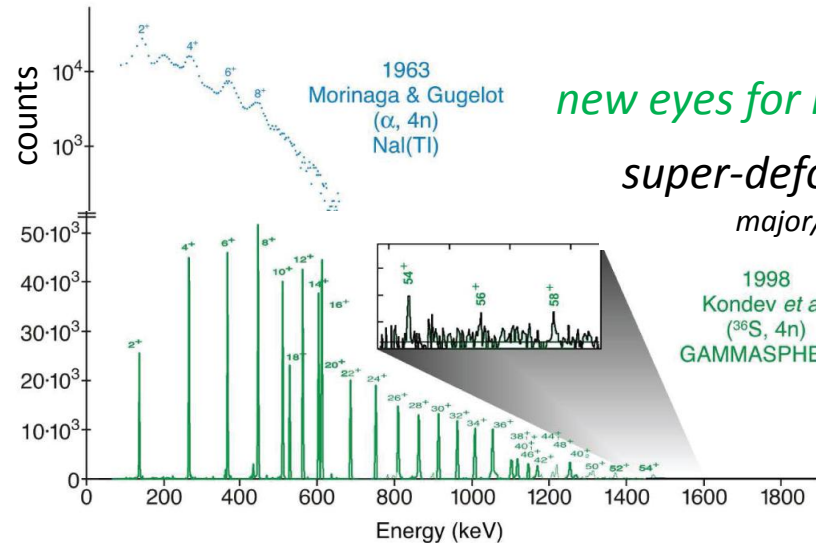
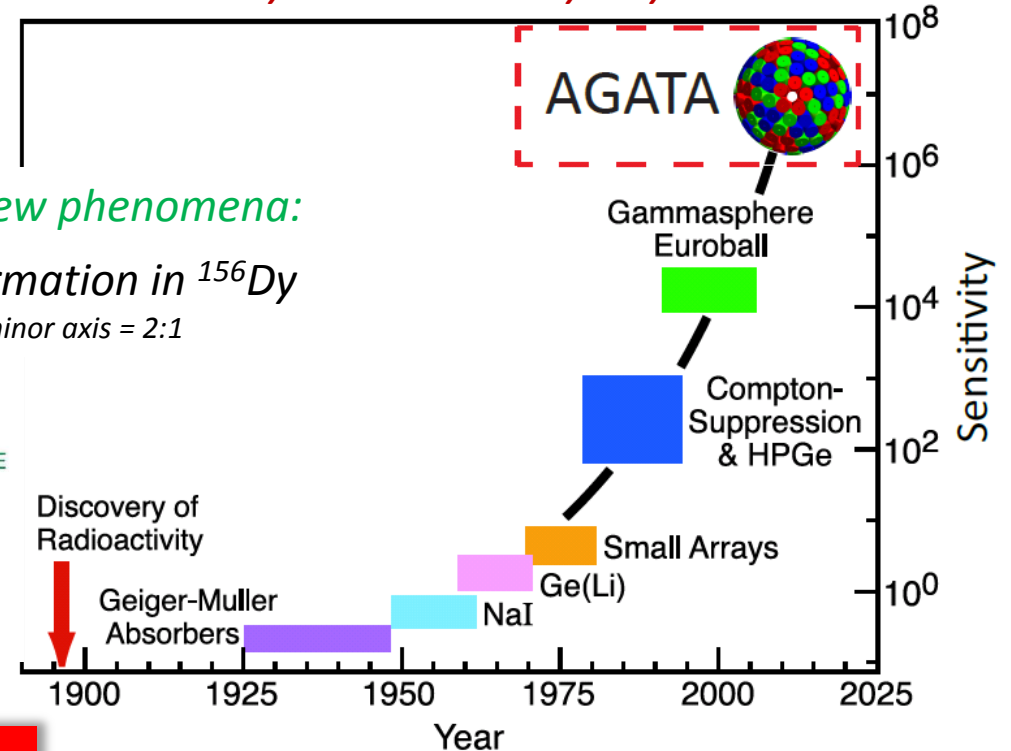
*super-deformation in  $^{156}\text{Dy}$   
major/minor axis = 2:1*

Sensitivity =

inverse of the weakest channel  
reaction cross-section that can be  
measured over total cross section

# Advances in $\gamma$ -ray spectroscopy: sensitivity vs year

*Ge detector system sensitivity vs year*



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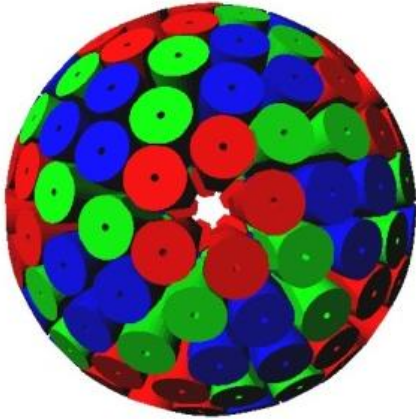
1998  
Kondev *et al.*  
( $^{36}\text{S}$ , 4n)  
GAMMASPHERE

**AGATA (EU) and GRETA (US) will allow unprecedented gamma detection sensitivity, by using the germanium detectors in *position sensitive mode* (Pulse Shape Analysis and Tracking)**

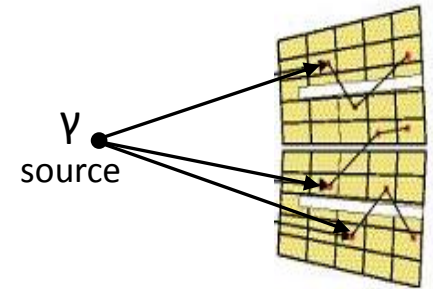
Sensitivity =  
inverse of the weakest channel  
reaction cross-section that can be  
measured over total cross section

# The $\gamma$ -ray spectroscopy dream

Cover the whole detection solid angle by germanium and track the path of the  $\gamma$  rays inside the detector medium



- segmented detectors
- digital electronics
- timestamping of events
- analysis of pulse shapes
- tracking of  $\gamma$ -rays



4 time more efficient than standard arrays, also for high  $\gamma$  multiplicity  
(28 %  $M_\gamma=30$ )

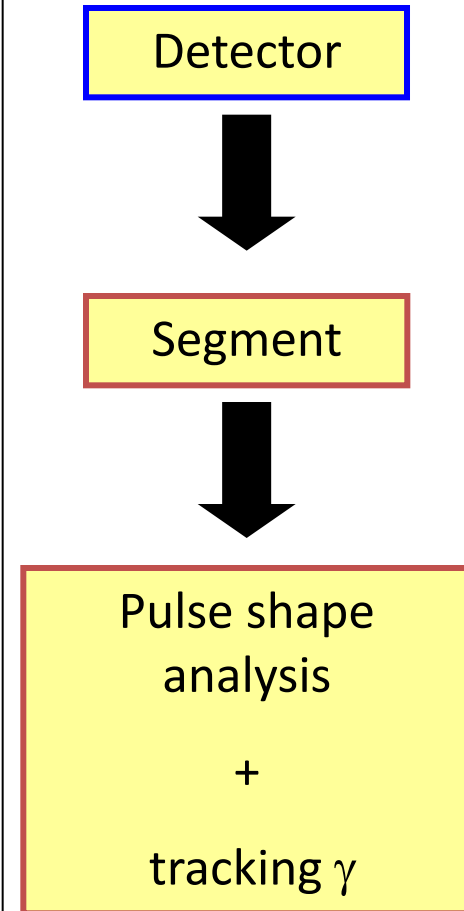
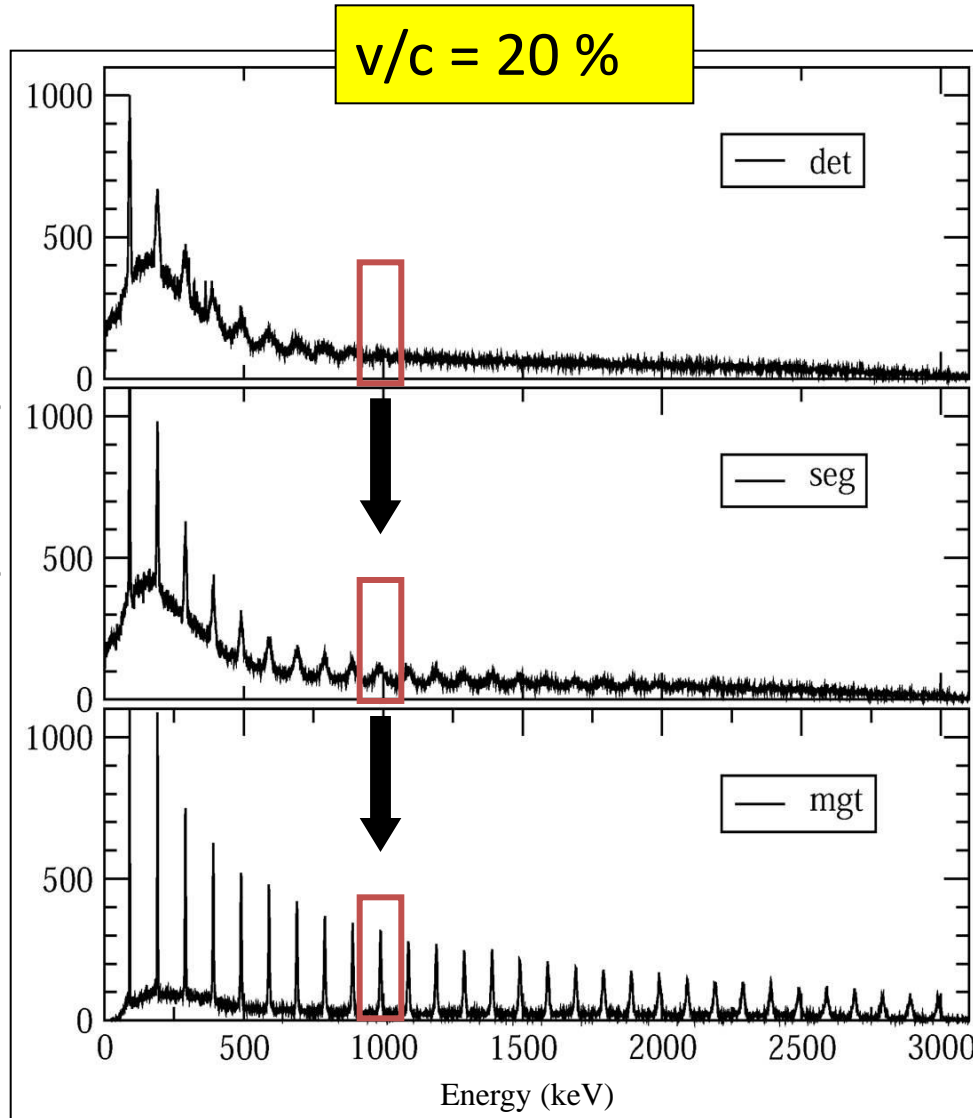
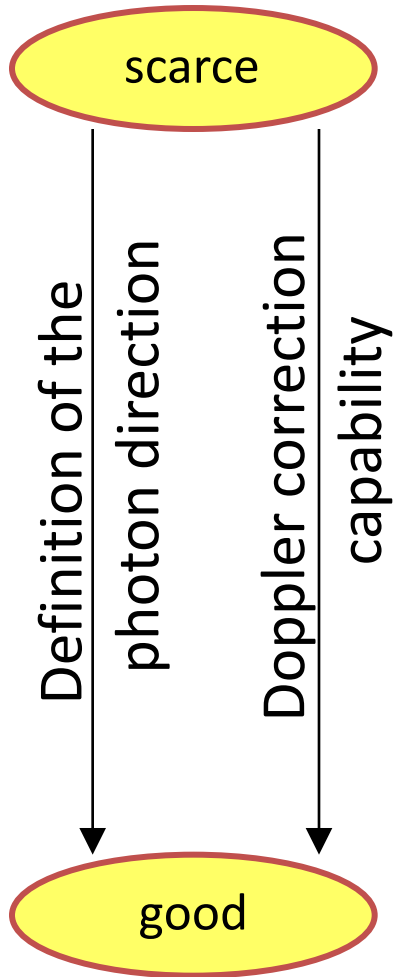
High count rate capabilities  
(100s KHz)

Study of nuclei in extreme conditions  
of angular momentum and  
neutron/proton asymmetry

“continuous” angular distributions of the  
 $\gamma$  interaction points ( $\theta \sim 1^\circ$ )

“perfect” Doppler correction  
(6 keV @ 1 MeV,  $\beta=50\%$ )  
new accuracy and sensitivity for  
nuclear level lifetimes  
 $\gamma$  linear polarization

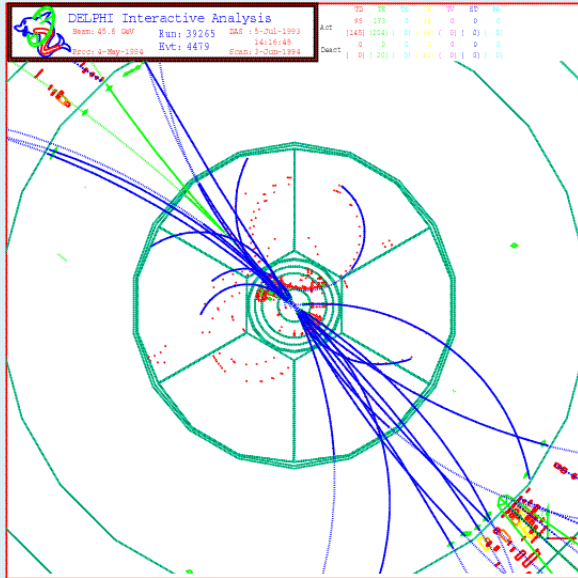
# Position resolution used to limit Doppler broadening of gammas emitted in flight -- Benefits of the $\gamma$ -ray tracking





# Tracking of radiation

in High Energy Physics

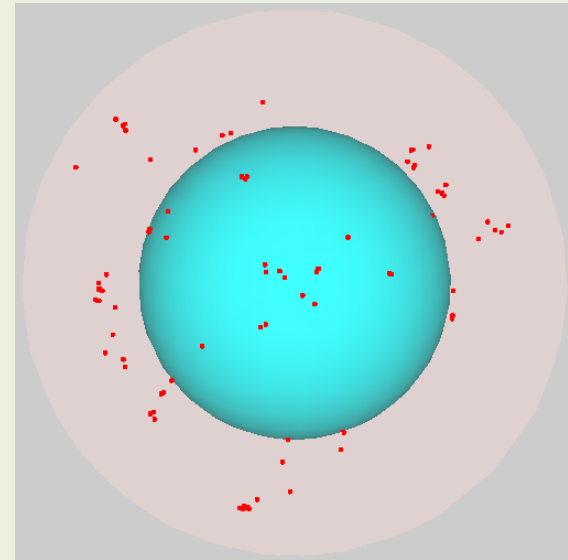


“continuous tracks” from very energetic particles

huge detectors for “one” experiment

Physics ← the study of “complete” events

in Nuclear Spectroscopy



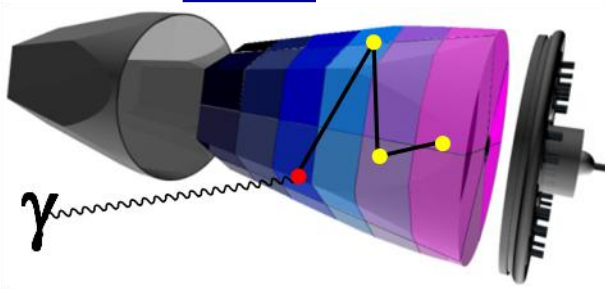
“many” low energy (0.01 -- 10 MeV) neutral transitions with low density of energy deposition

“general-purpose” detectors for a large variety of experiments

Physics ← large number of incomplete events

# Position-sensitive operation mode and $\gamma$ -ray tracking

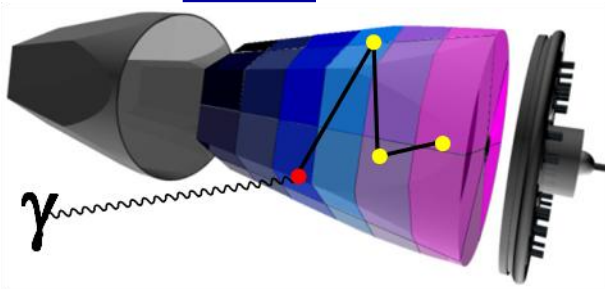
highly segmented  
HPGe detectors



Event by event:  
how many gammas,  
for each gamma: energy,  
first interaction point, path

# Position-sensitive operation mode and $\gamma$ -ray tracking

highly segmented  
HPGe detectors

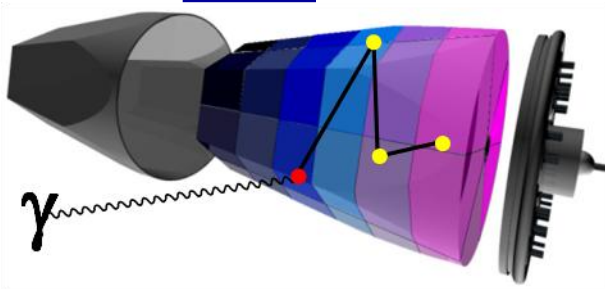


digital electronics to  
record sampled  
waveforms

Event by event:  
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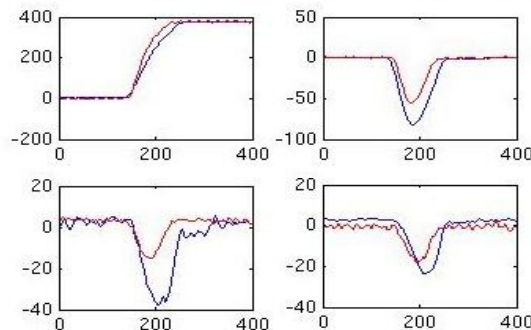
# Position-sensitive operation mode and $\gamma$ -ray tracking

highly segmented  
HPGe detectors



digital electronics to  
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waveforms

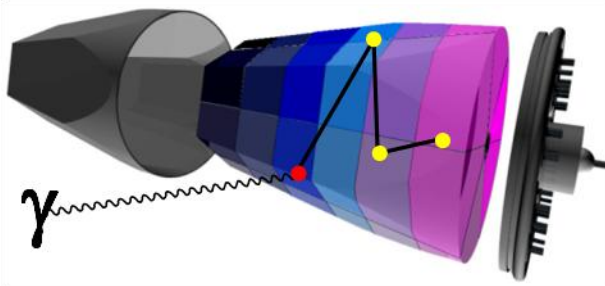
Pulse Shape Analysis  
of the recorded waves



Event by event:  
how many gammas,  
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first interaction point, path

# Position-sensitive operation mode and $\gamma$ -ray tracking

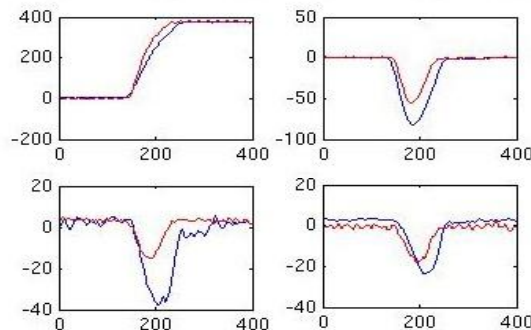
highly segmented  
HPGe detectors



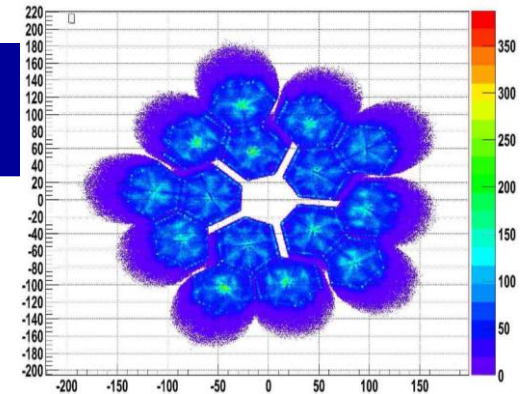
Identified  
interaction points  
(hits)

$(x,y,z,E,t)_i$

Pulse Shape Analysis  
of the recorded waves



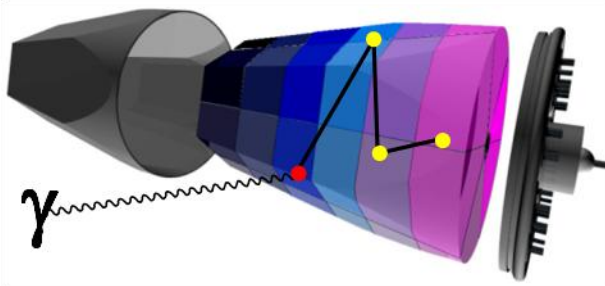
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HPGe detectors

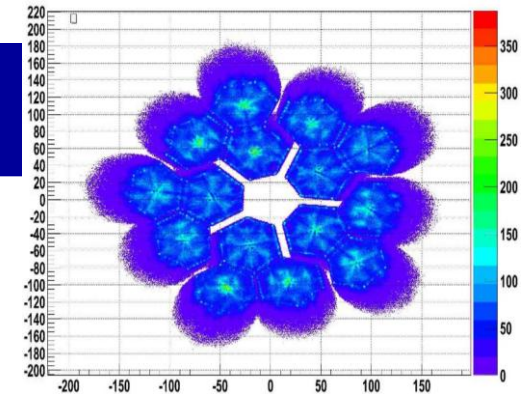
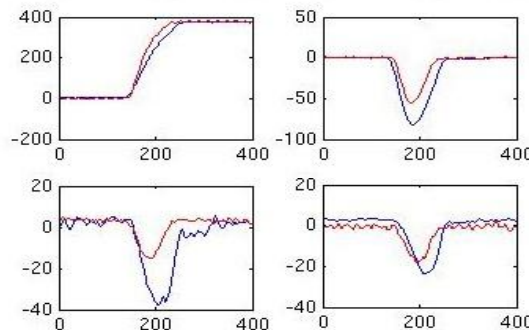


digital electronics to  
record sampled  
waveforms

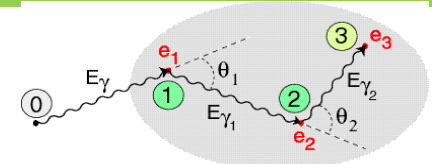
Identified  
interaction points  
(hits)

$(x, y, z, E, t)_i$

Pulse Shape Analysis  
of the recorded waves



reconstruction of  
 $\gamma$ -rays from the hits  
(tracking)

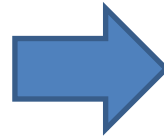


Event by event:  
how many gammas,  
for each gamma: energy,  
first interaction point, path

# Aim of gamma-ray tracking

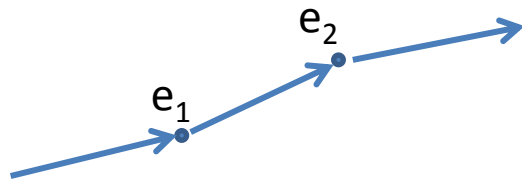
deposited energies and the positions of all the interactions points of an event in the detector

$e_1, x_1, y_1, z_1$   
 $e_2, x_2, y_2, z_2$   
.....  
 $e_n, x_n, y_n, z_n$



reconstruct individual photon trajectories and write out photon energies, incident and scattering directions

$E_1, (\theta, \phi)_{inc,1}, (\theta, \phi)_{sc,1} \dots$   
 $E_2, (\theta, \phi)_{inc,2}, (\theta, \phi)_{sc,2} \dots$   
.....  
 $E_i, (\theta, \phi)_{inc,i}, (\theta, \phi)_{sc,i}$

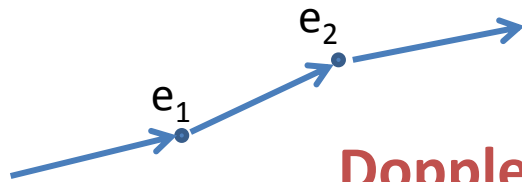


discard events corresponding to incomplete energy release

# Aim of gamma-ray tracking

deposited energies and the positions of all the interactions points of an event in the detector

$e_1, x_1, y_1, z_1$   
 $e_2, x_2, y_2, z_2$   
.....  
 $e_n, x_n, y_n, z_n$



**Doppler correction**

**Linear Polarization**

reconstruct individual photon trajectories and write out photon energies, incident and scattering directions

$E_1, (\theta, \phi)_{inc,1}, (\theta, \phi)_{sc,1} \dots$   
 $E_2, (\theta, \phi)_{inc,2}, (\theta, \phi)_{sc,2} \dots$   
.....  
 $E_i, (\theta, \phi)_{inc,i}, (\theta, \phi)_{sc,i}$

discard events corresponding to incomplete energy release

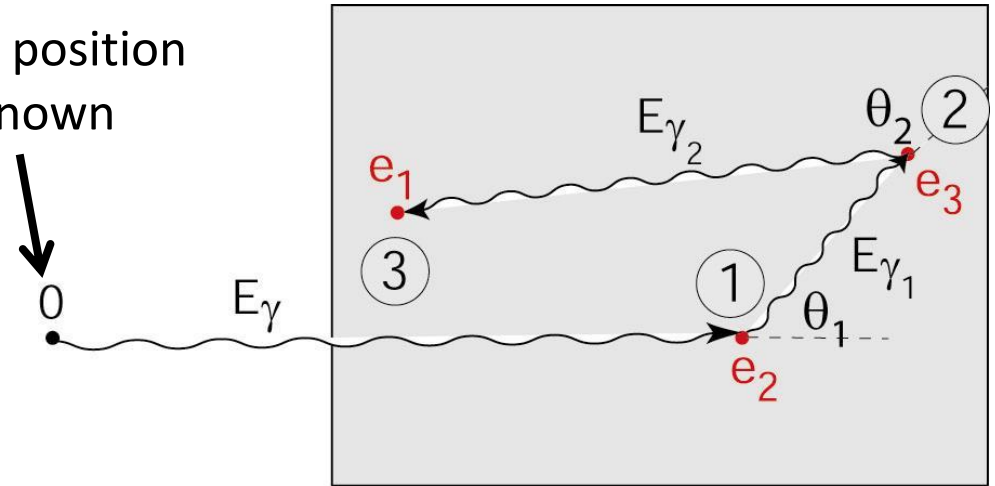


# Tracking of Compton Scattered Events

Questions :

- 1) Is the event complete?
- 2) What is the right sequence?

Source position  
is known

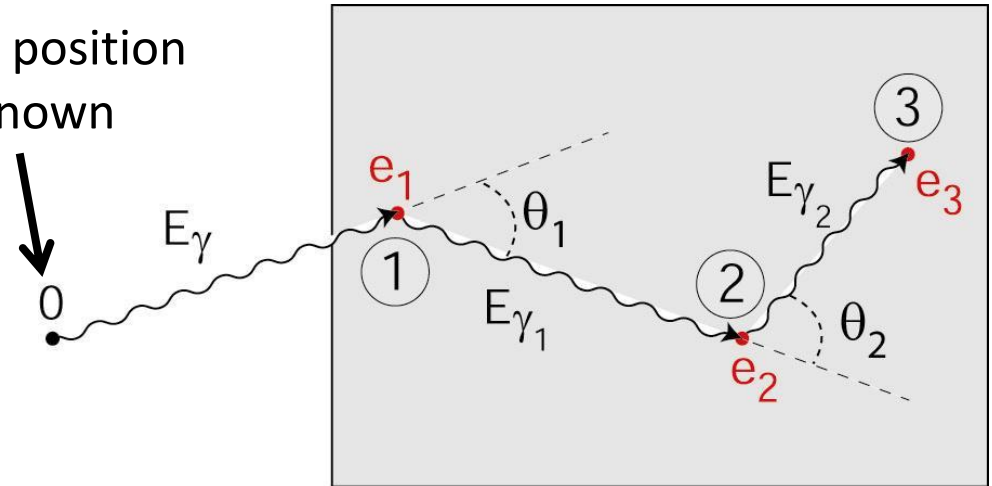


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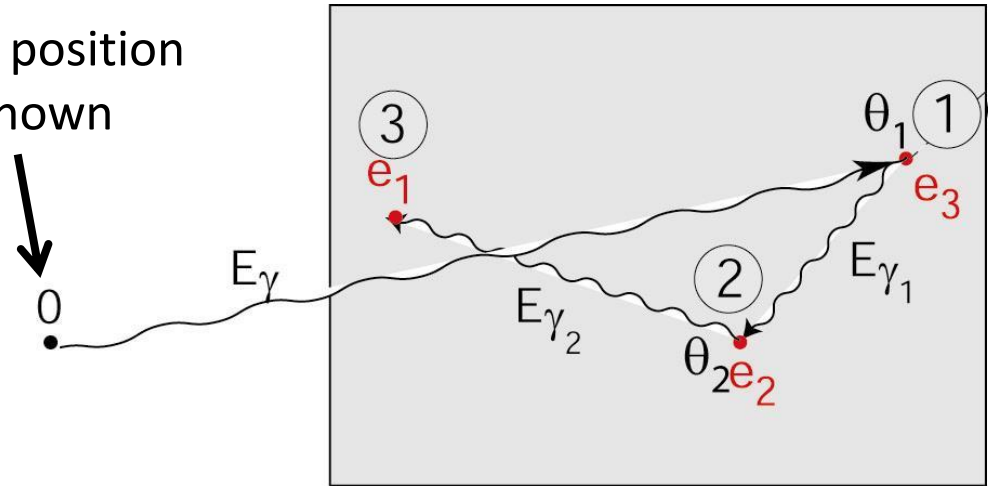


# Tracking of Compton Scattered Events

Questions :

- 1) Is the event complete?
- 2) What is the right sequence?

Source position  
is known



From energy deposition +  
incident energy

$$E_\gamma^E = \sum_{i=n}^{N-1} e_i$$

From source +  
interaction positions

$$\cos \theta^P = \frac{\vec{01} \cdot \vec{12}}{|\vec{01}| \cdot |\vec{12}|}$$

$$E_{\gamma'}^E = \sum_{i=n+1}^{N-1} e_i$$

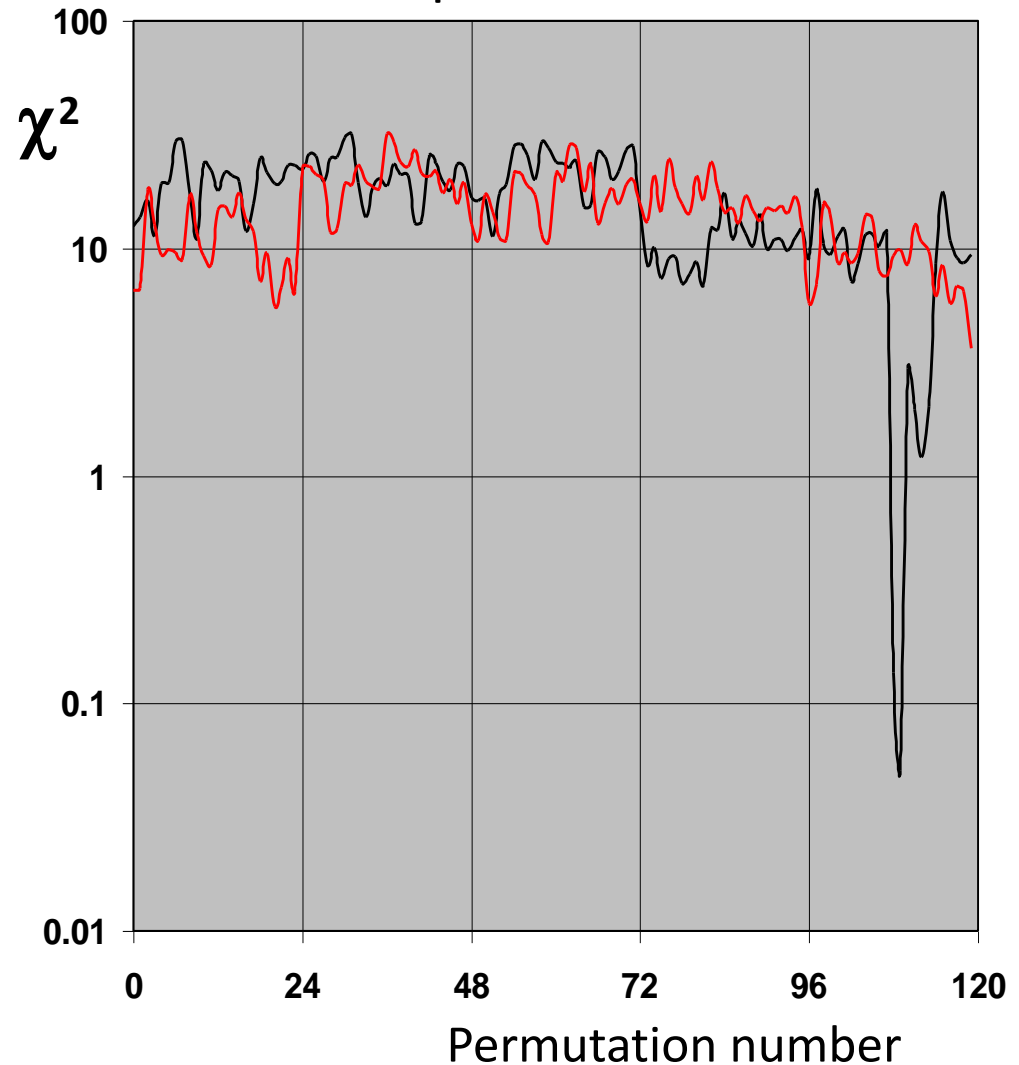
$$\Rightarrow E_{\gamma'}^P = \frac{E_\gamma^E}{1 + \frac{E_\gamma^E}{m_0 c^2} (1 - \cos \theta^P)}$$

Track order = permutation  
with best  $\chi^2$

$$\chi_n^2 = \left( \frac{E_{\gamma'}^E - E_{\gamma'}^P}{\sigma} \right)^2 \Rightarrow \chi^2 \approx \sum_{n=1}^{N-1} \chi_n^2$$

# Tracking of Compton Scattered Events

Two 5-point events



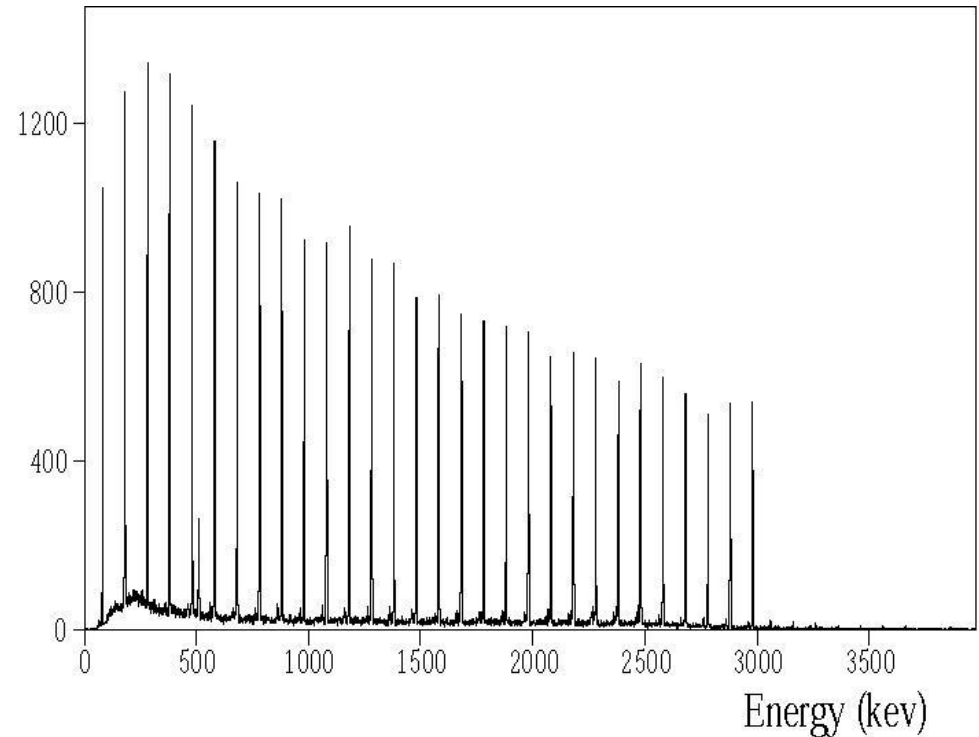
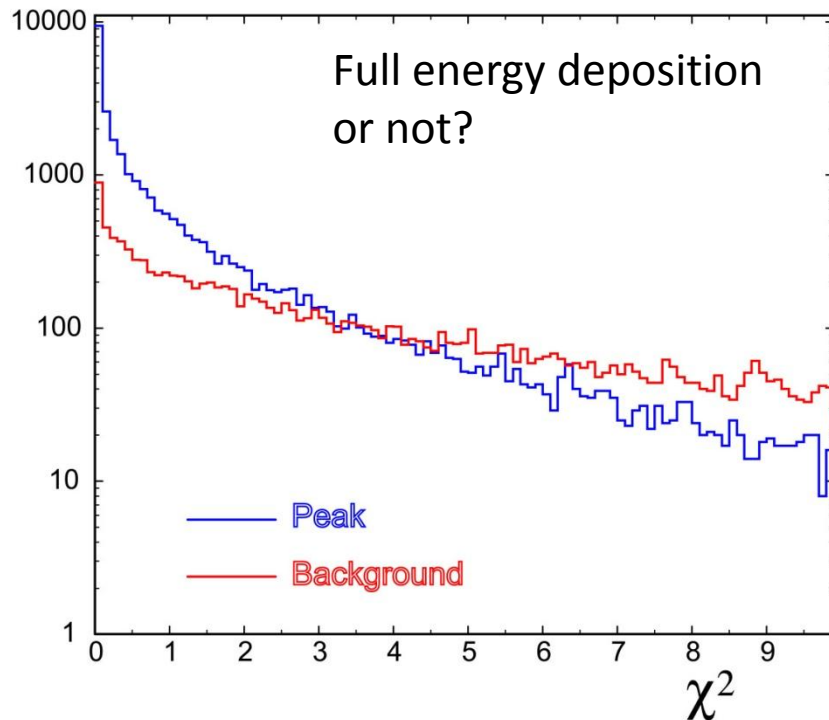
Find  $\chi^2$  for the  $N!$  permutations of the interaction points

Fit parameter is the permutation number

Accept the best permutation if its  $\chi^2$  is below a predefined value

# Identification is not 100% sure

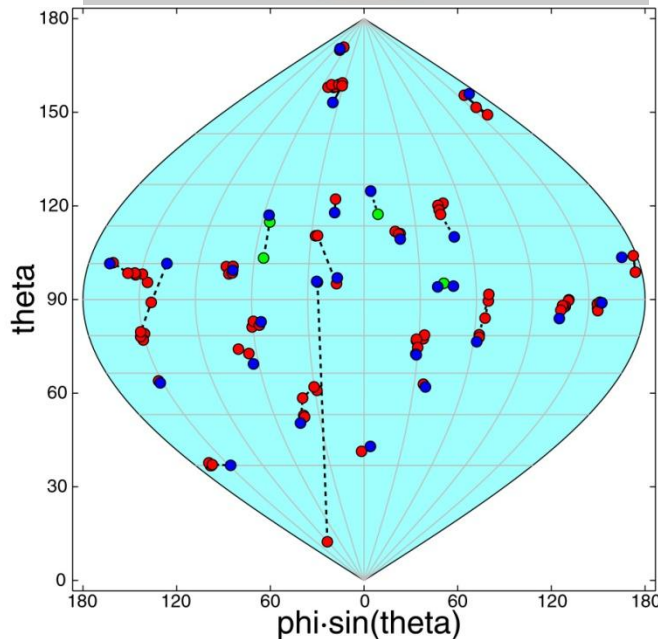
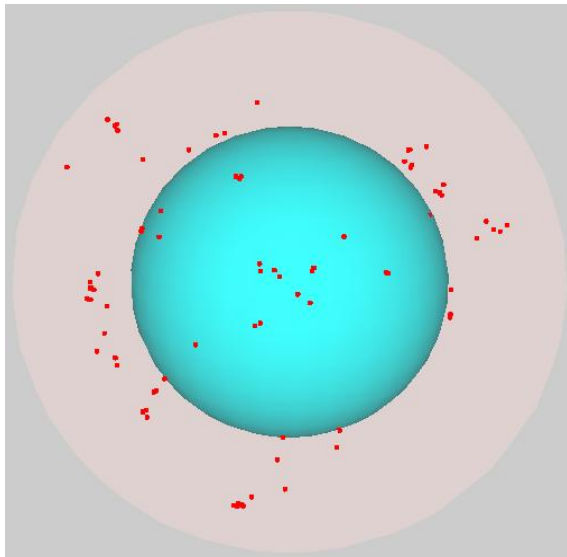
→ spectra will always contain background



The acceptance value determines the quality (P/T ratio) of the spectrum

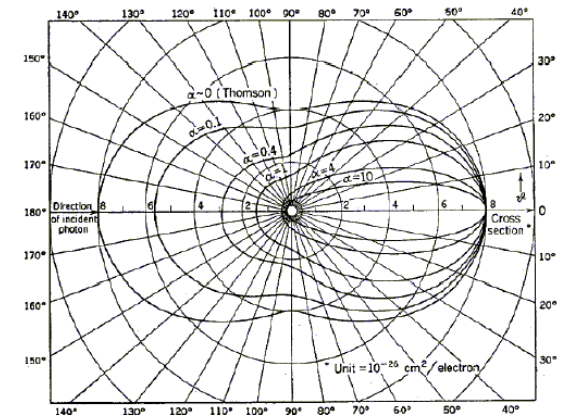
Often we use the **R = Efficiency • PT** to qualify the reconstructed spectra

# Reconstruction of multi-gamma events

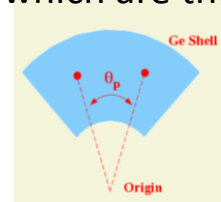


- Analysis of all partitions of measured hits is not feasible:  
Huge computational problem  
( $\sim 10^{23}$  partitions for 30 points)  
Figure of merit is ambiguous  $\rightarrow$  the total figure of merit of the “true” partition not necessarily the minimum
- Forward peaking of Compton scattering cross-section implies that the hits of one gamma tend to be localized along the emission direction

$$\frac{d\sigma_{KN}}{d\Omega} = Z \frac{r_0^2}{2} \left( \frac{E'}{E} \right)^2 \left[ \frac{E'}{E} + \frac{E}{E'} - \sin^2 \theta \right]$$



- The most used algorithm (G.Schmid et al. NIMA 430 1999, GRETA) starts by identifying **clusters** of points which are then analyzed as individual candidate gammas



# Forward tracking implemented for AGATA

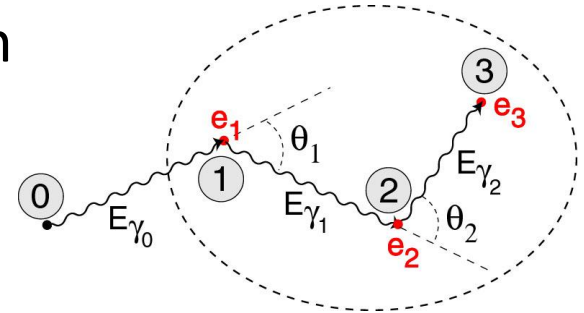
(D.Bazzacco, Padova - A. Lopez-Martens, Orsay [NIMA 533 (2004) 454])

1. Create cluster pool => for each cluster,  $E_{\gamma_0} = \sum$  depositions in the cluster

# Forward tracking implemented for AGATA

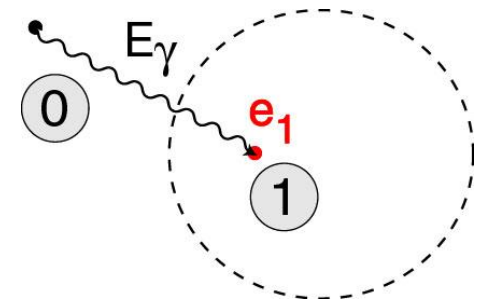
(D.Bazzacco, Padova - A. Lopez-Martens, Orsay [NIMA 533 (2004) 454])

1. Create cluster pool => for each cluster,  $E_{\gamma 0} = \sum$  depositions in the cluster
2. Find most probable sequence of interaction points, test the 3 mechanisms



1. do the interaction points satisfy the **Compton** scattering rules ?

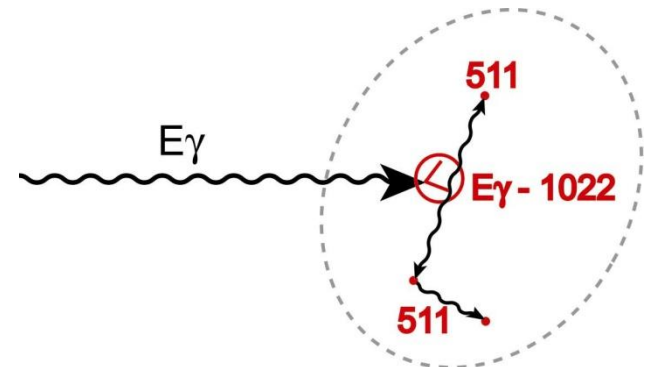
$$\chi^2 \approx \sum_{n=1}^{N-1} W_n \cdot \left( \frac{E_{\gamma'} - E_{\gamma'}^{\text{Pos}}}{E_{\gamma}} \right)_n^2$$



2. does the interaction satisfy **photoelectric** conditions  
( $e_1$ , depth, distance to other points) ?

3. do the interaction points correspond to a **pair production** event ?

$$E_{1st} = E_{\gamma} - 2 m_e c^2$$

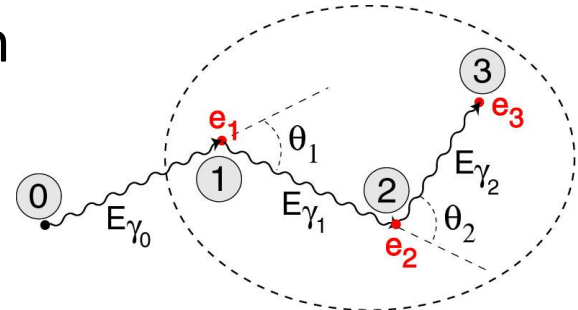




# Forward tracking implemented for AGATA

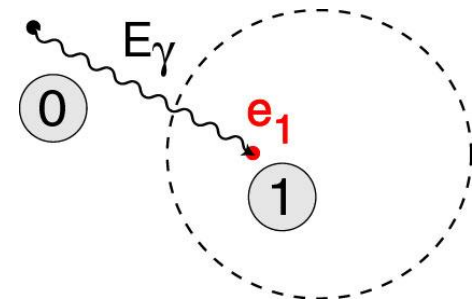
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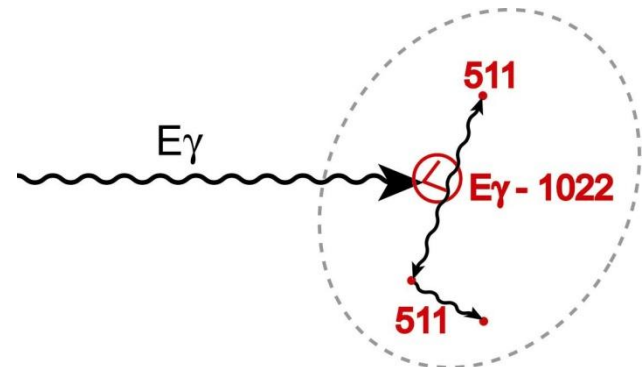
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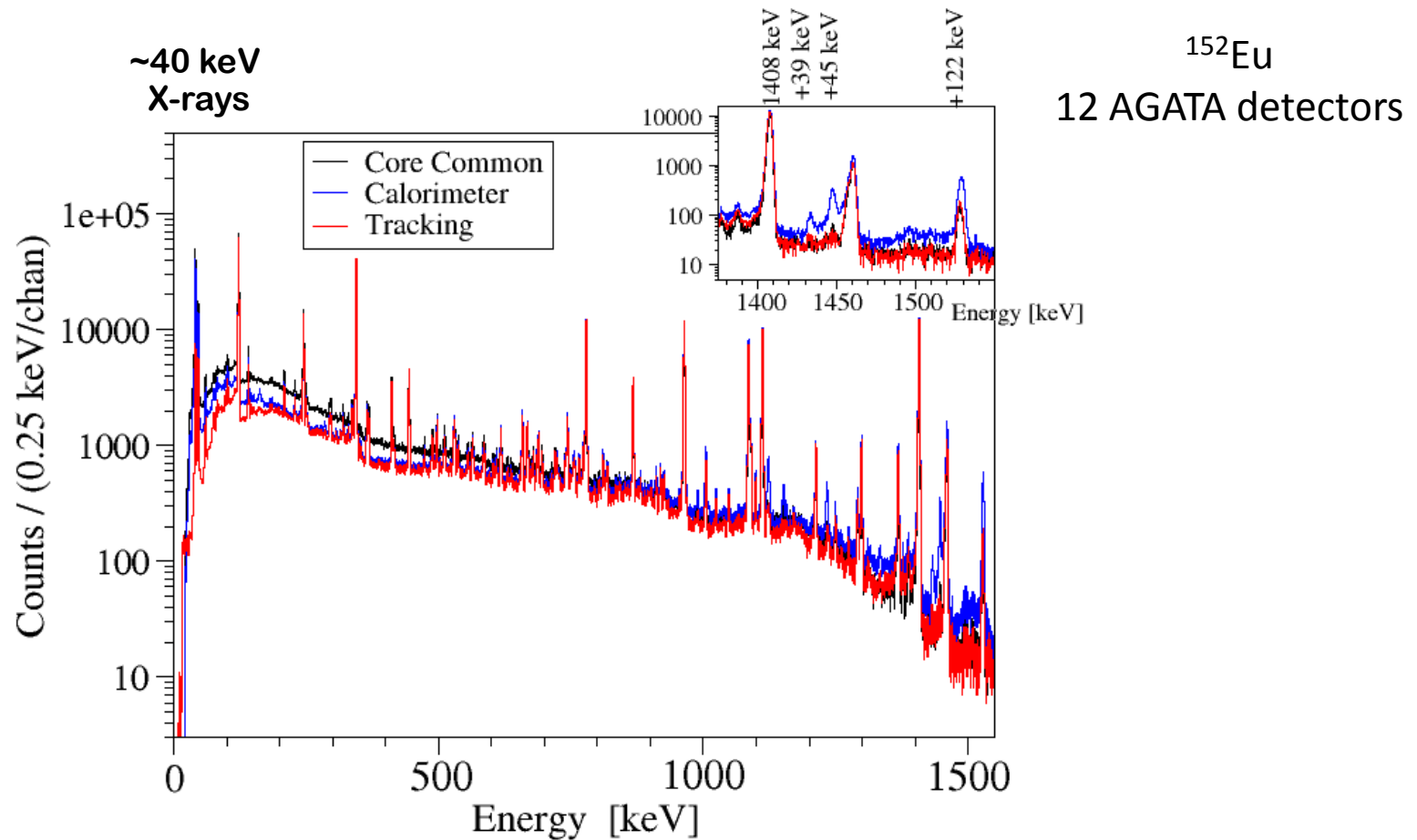
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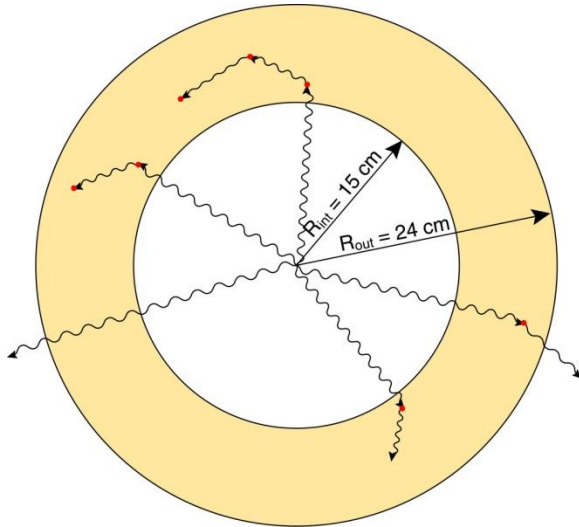
3. Select clusters based on  $\chi^2$

# Examples of tracked source spectra



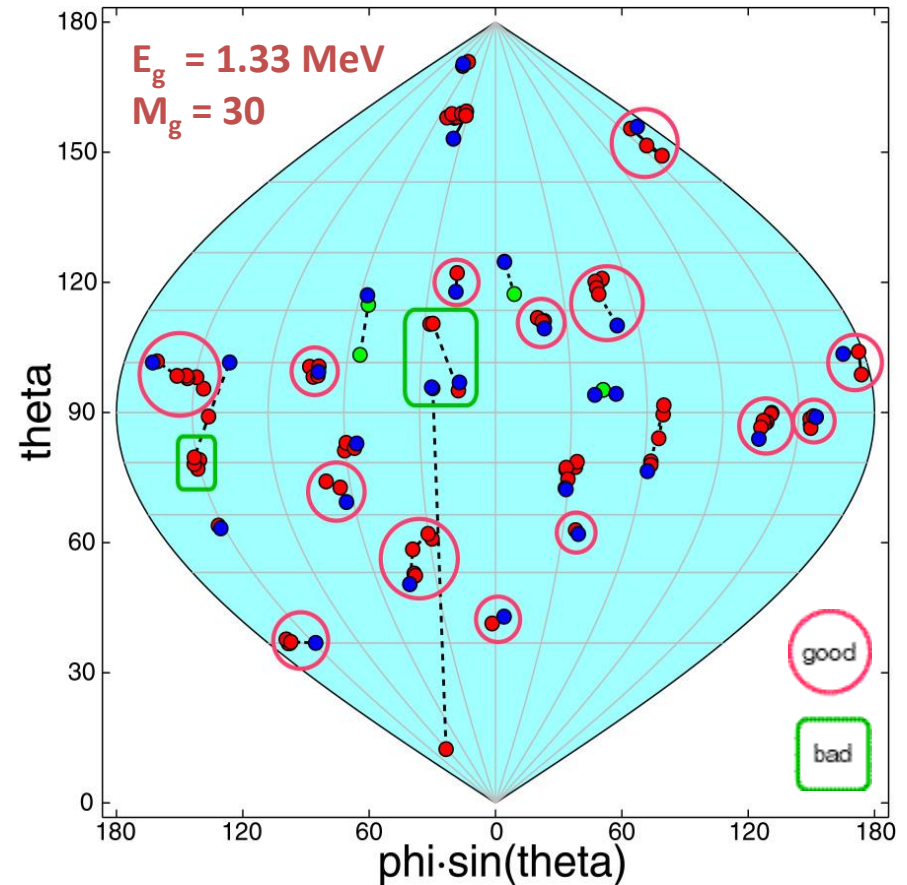
# Performance of the Germanium Shell

Idealized configuration to determine maximum attainable performance.



1.33 MeV	$M_\gamma = 1$	$M_\gamma = 30$
$\epsilon_{ph}$ (%)	65	36
P/T(%)	85	60

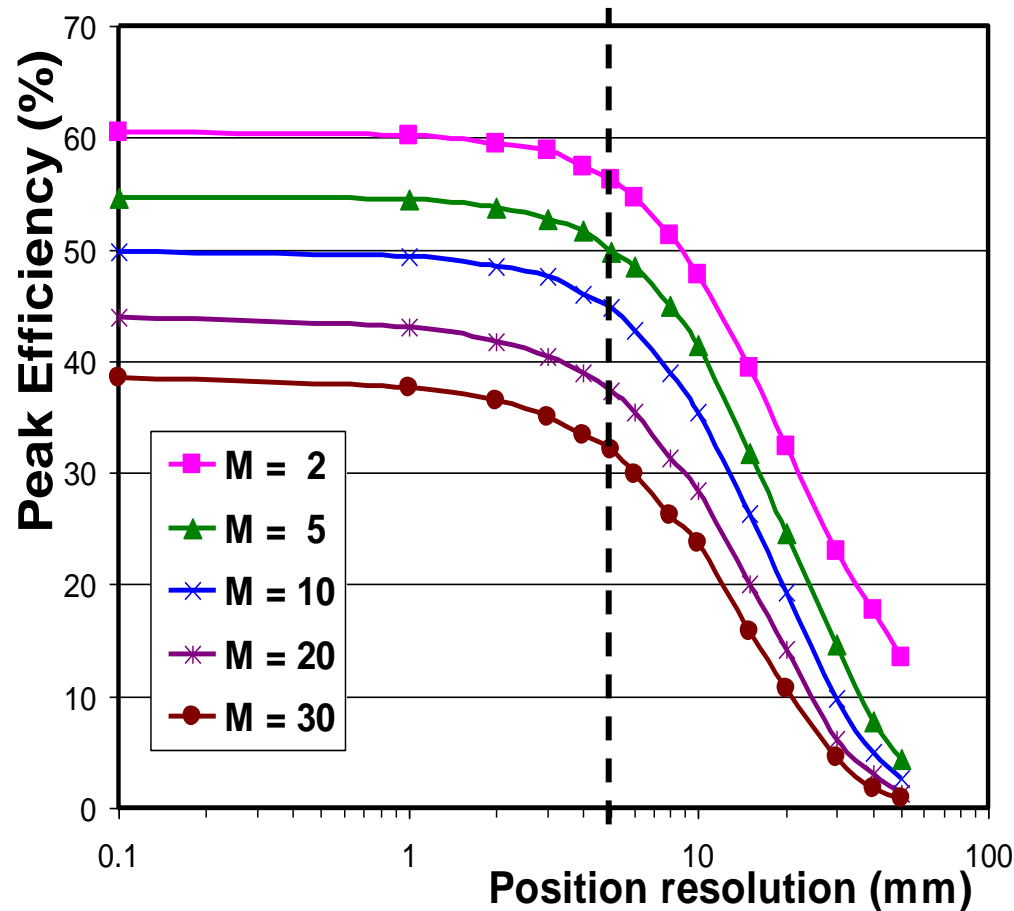
## A high multiplicity event



Reconstruction by Cluster-Tracking  
 Packing Distance: 5 mm  
 Position Resolution: 5 mm (at 100 keV)

27 gammas detected -- 23 in photopeak  
 16 reconstructed -- 14 in photopeak

# Efficiency of Standard Ge Shell vs. Position Resolution and $\gamma$ Multiplicity



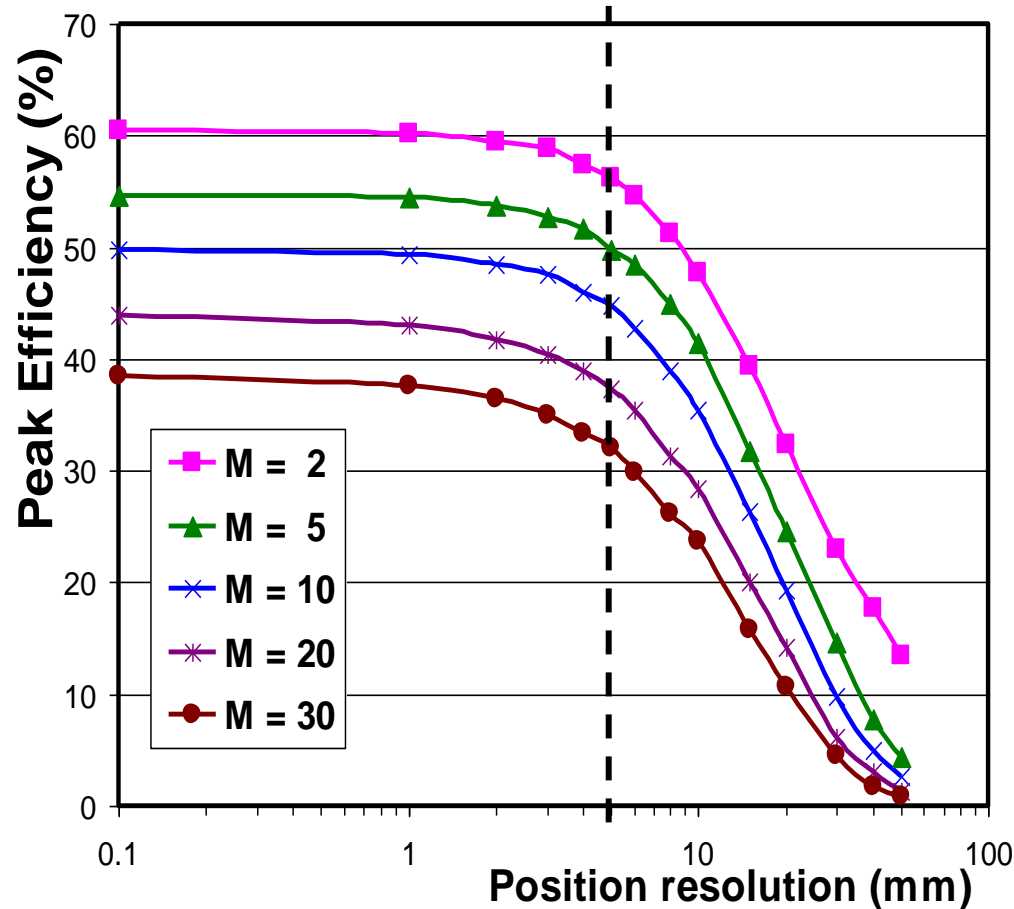
The biggest losses are due to multiplicity (mixing of points) not to bad position resolution

5 mm is the standard “realistic” packing and smearing assumption

If positions inside segments are not known, performance is a factor 2 worse

Standard shell;  $E_\gamma = 1.33$  MeV; Packing=Smearing;  
Energy independent smearing

# Efficiency of Standard Ge Shell vs. Position Resolution and $\gamma$ Multiplicity



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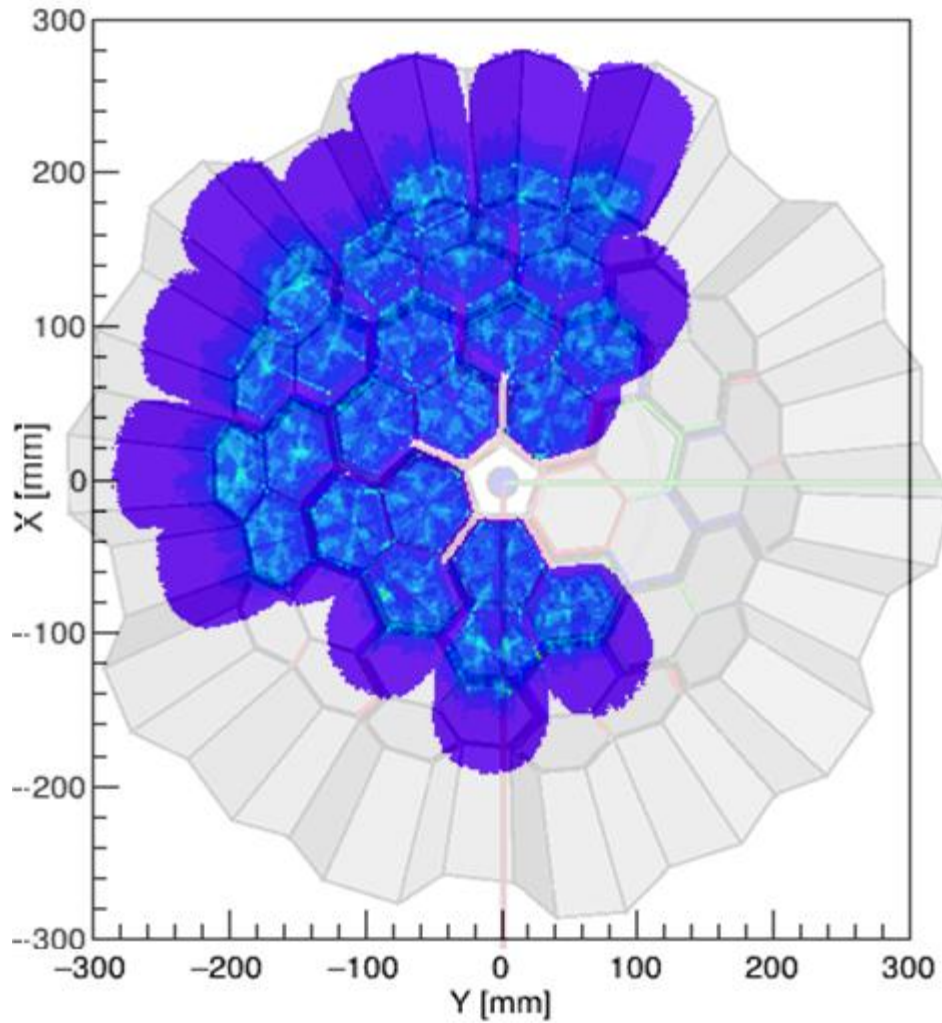
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Standard shell;  $E_\gamma = 1.33$  MeV; Packing=Smearing;  
Energy independent smearing

**Sub-segment position resolution is needed**

# Pulse Shape Analysis (PSA)



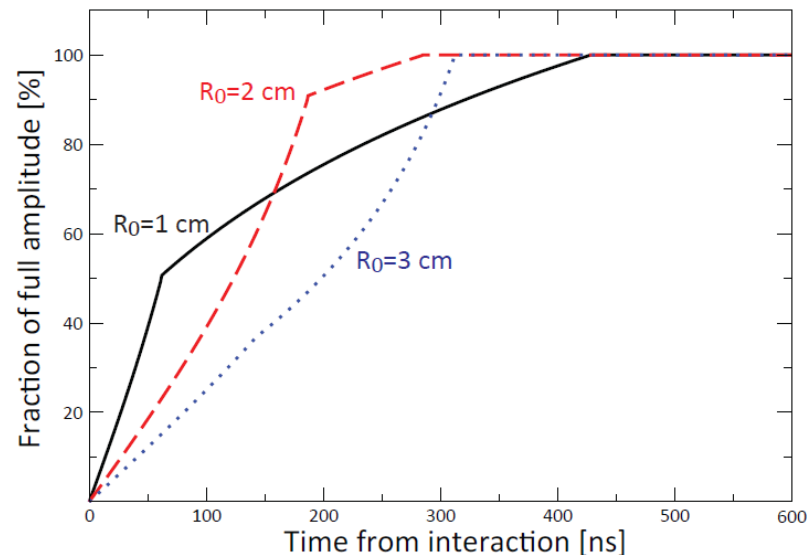
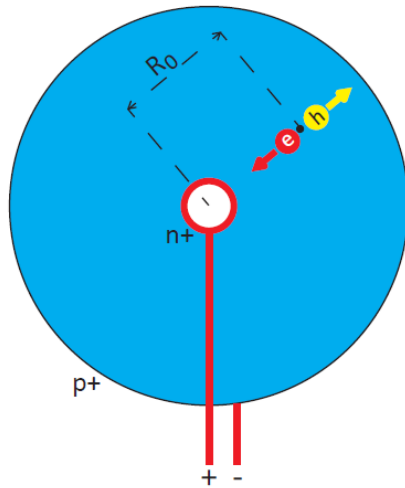
8 AGATA Triple Clusters  
(24 detectors)  
@ GANIL  
“captured” during an  
experiment

Reconstruction of the  
interaction points  
(hits)

# Pulse shapes in a coaxial Ge detector

Reverse bias (-HV on  $p^+$  contact) depletes bulk and generates high electric field

Radiation  $\rightarrow$  carriers in the bulk, swept out by electric field  $\rightarrow$  signal

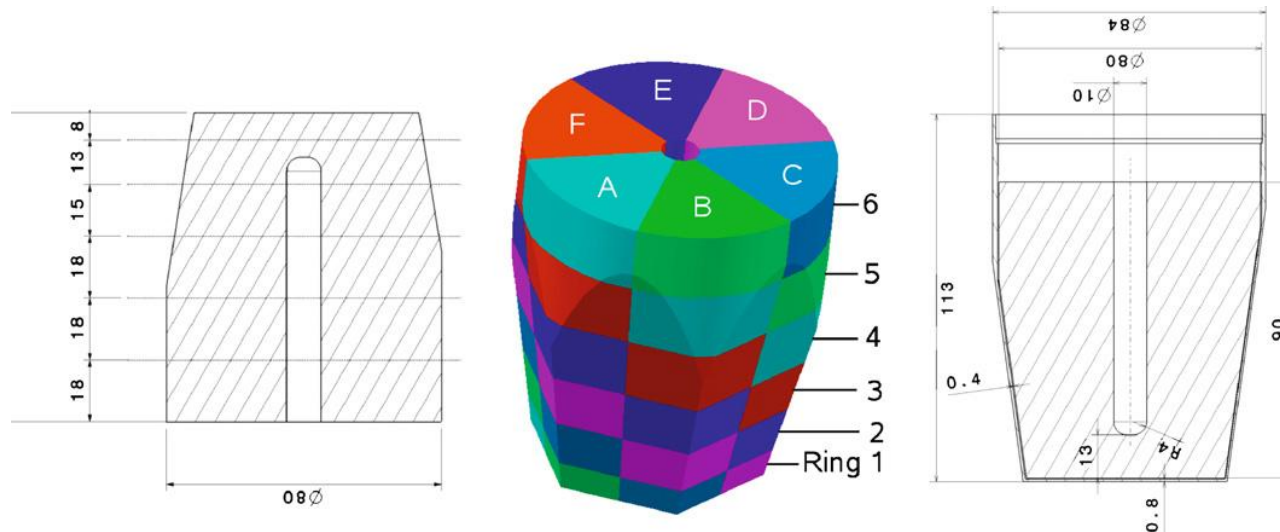


On “true” coaxial detectors, the shape depends on initial radius

# Segmented detectors

- When one of the electrodes is (electrically) segmented, the motion of charges within one segment induces a **transient** signal also in the neighboring electrodes
- Contrary to the segment where the interaction takes place (the charge is released), the total collected charge in the neighboring electrodes is null
- The amplitude of the induced transient signals provides a convenient way to locate the interaction with sub-segment precision

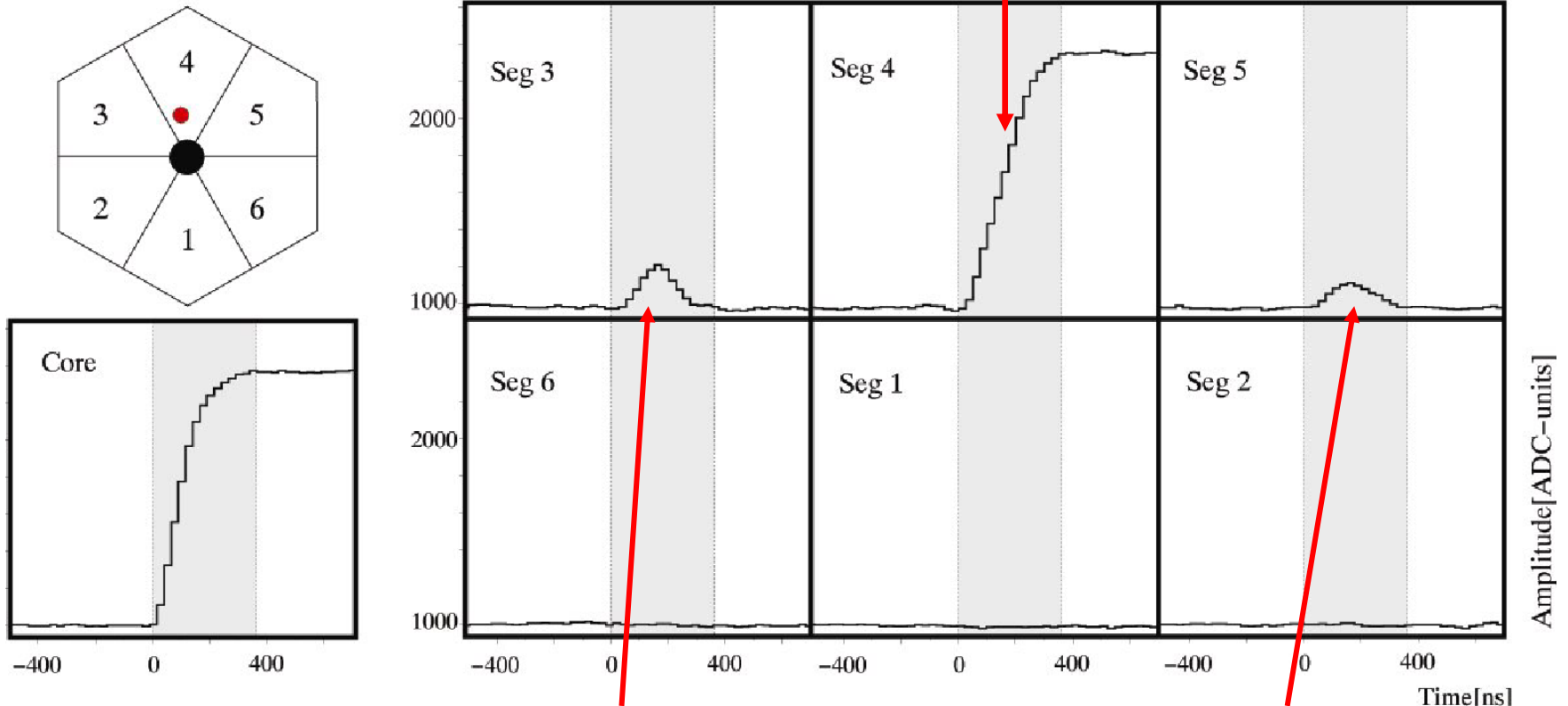
## Segmentation of an AGATA detector





# Pulse Shape Analysis concept

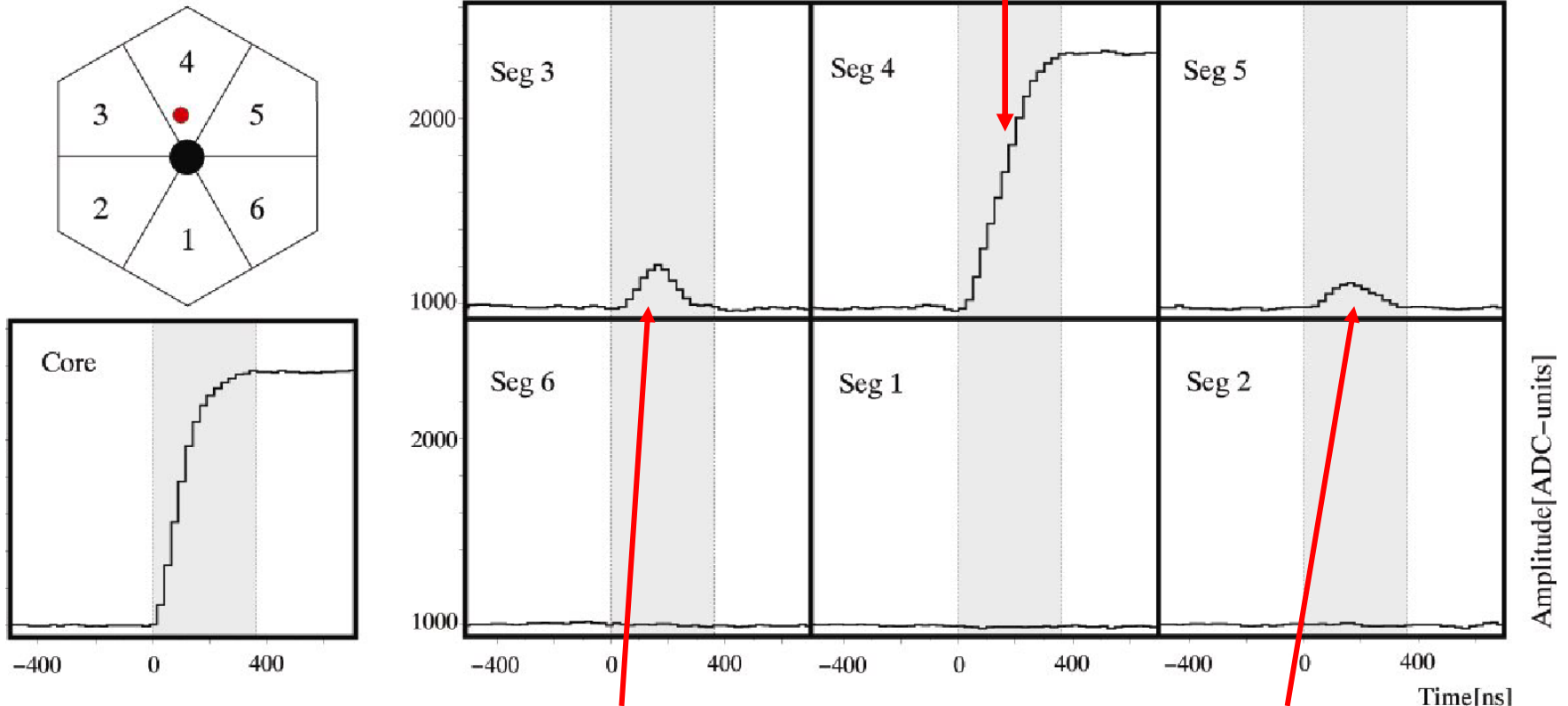
Interaction occurred in segment 4  
(net charge signal)



Interaction is closer to segment 3 (larger amplitude than segment 5)

# Pulse Shape Analysis concept

Interaction occurred in segment 4  
(net charge signal)

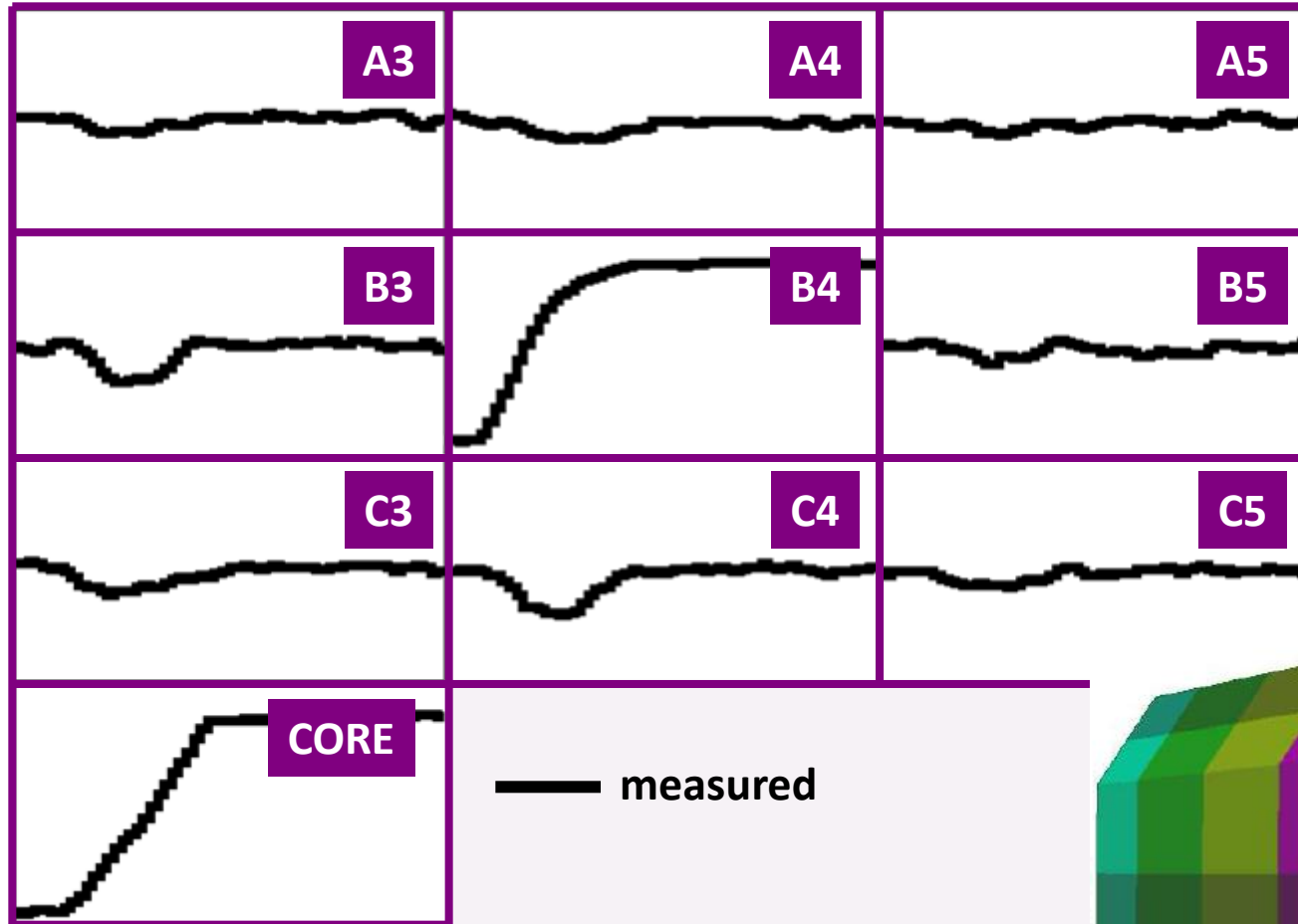


Interaction is closer to segment 3 (larger amplitude than segment 5)

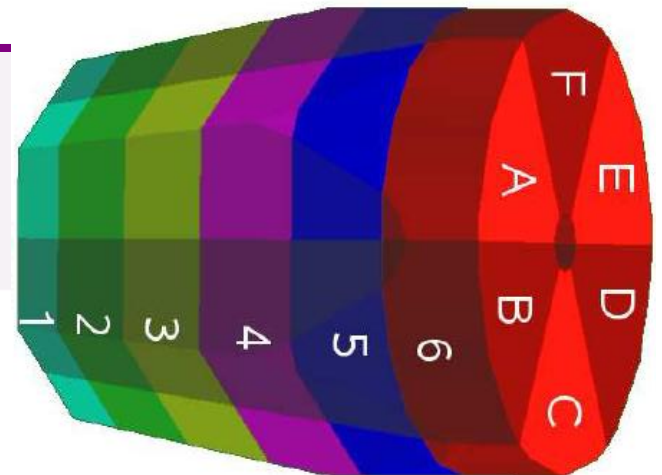
Sub-segment precision ... but not enough to efficiently perform tracking!

➔ Pulse Shape Analysis

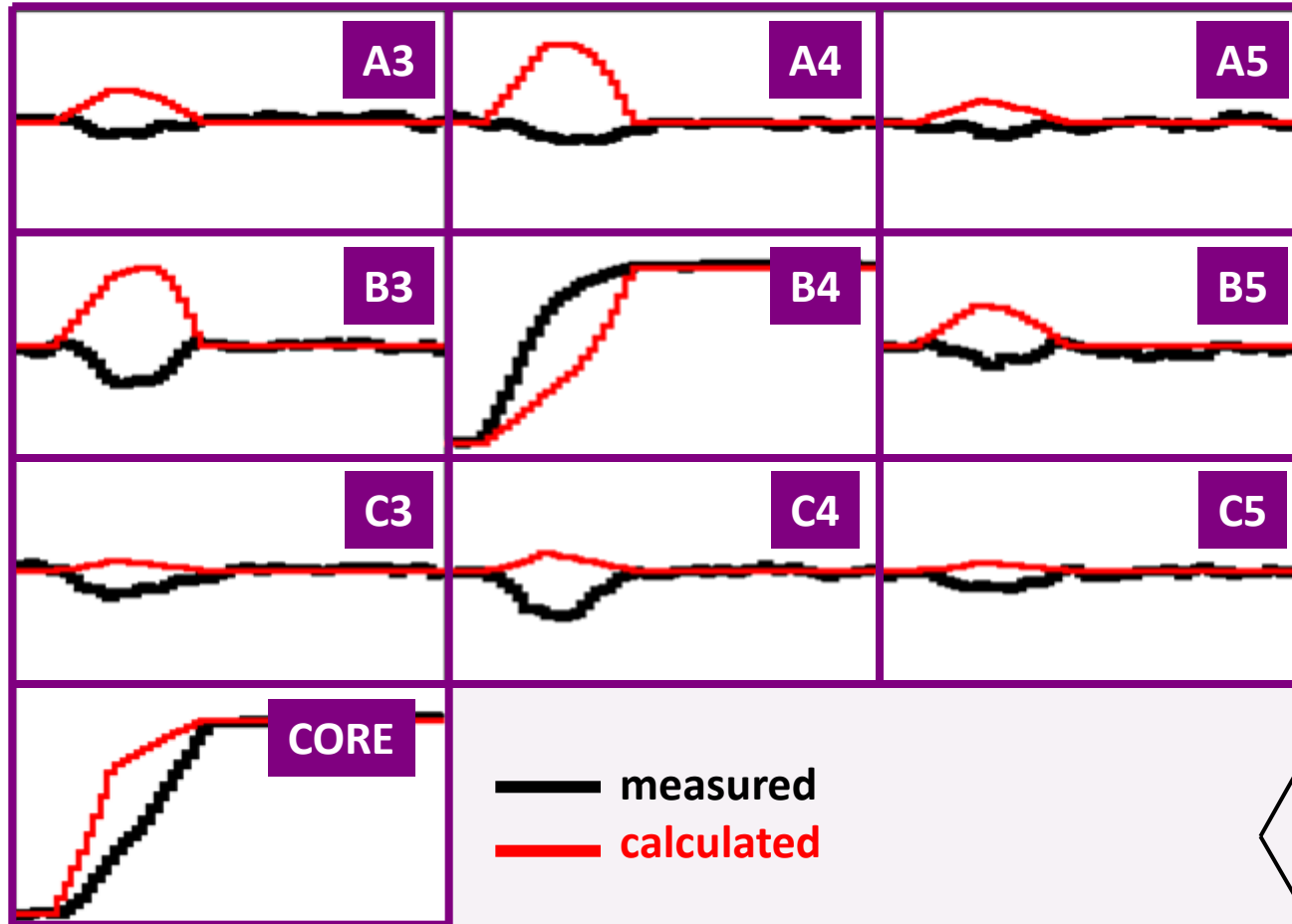
# Pulse Shape Analysis concept



791 keV deposited in segment B4

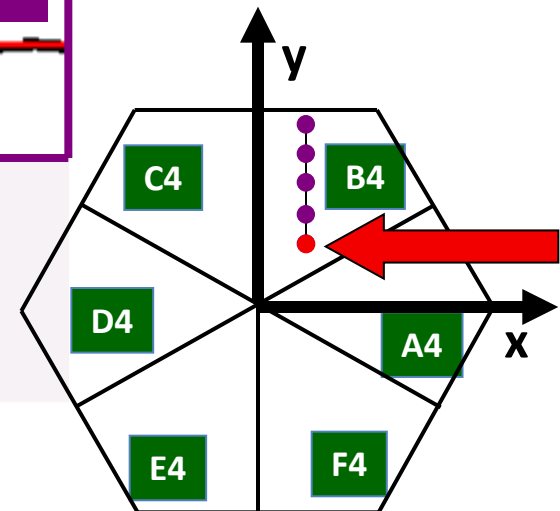


# Pulse Shape Analysis concept



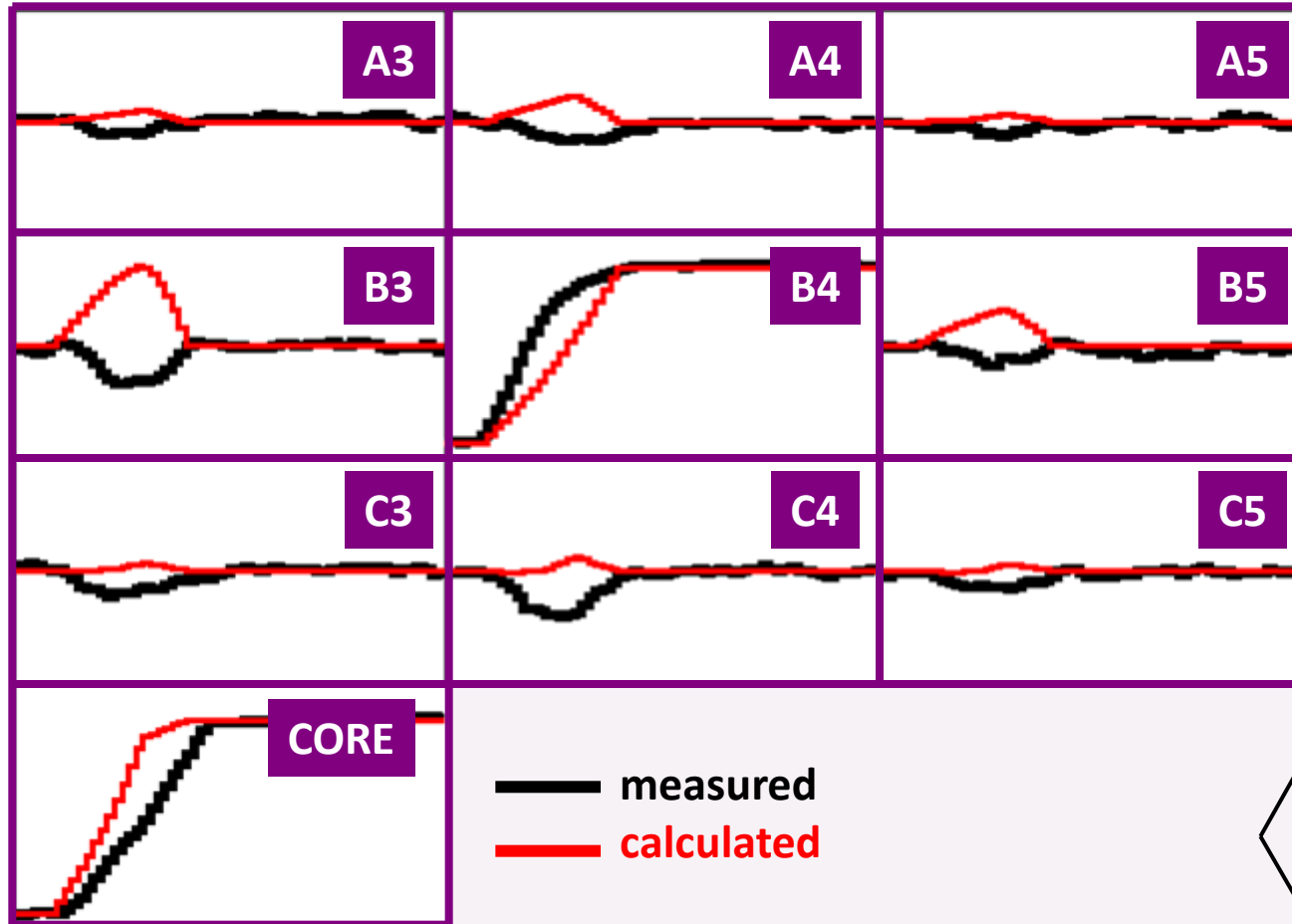
791 keV deposited in segment B4

(10, 10, 46)

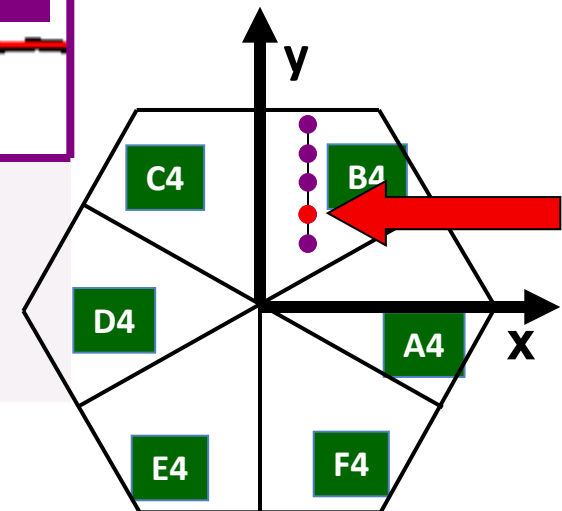


z = 46 mm

# Pulse Shape Analysis concept



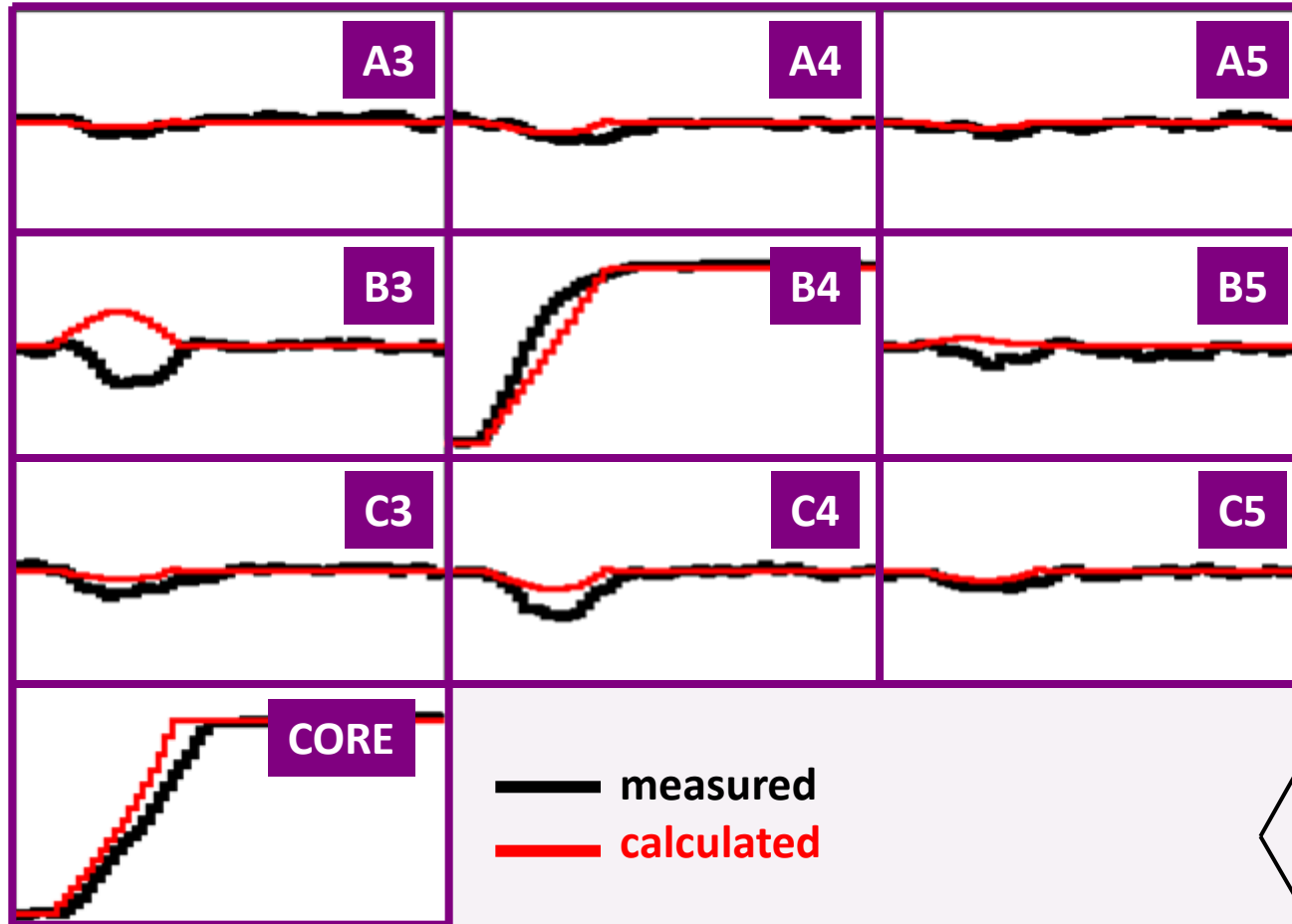
(10, 15, 46)



z = 46 mm

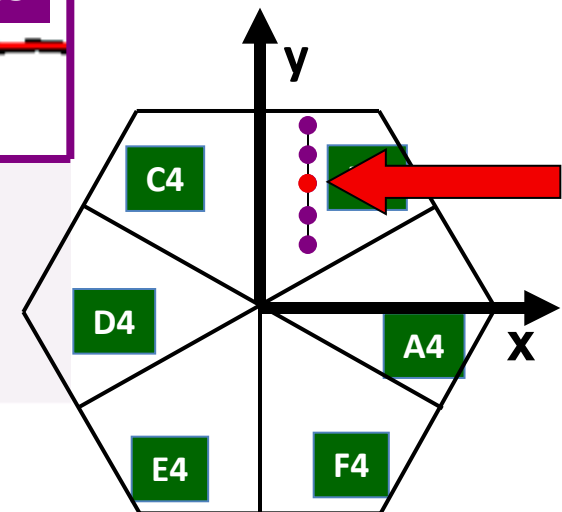
791 keV deposited in segment B4

# Pulse Shape Analysis concept



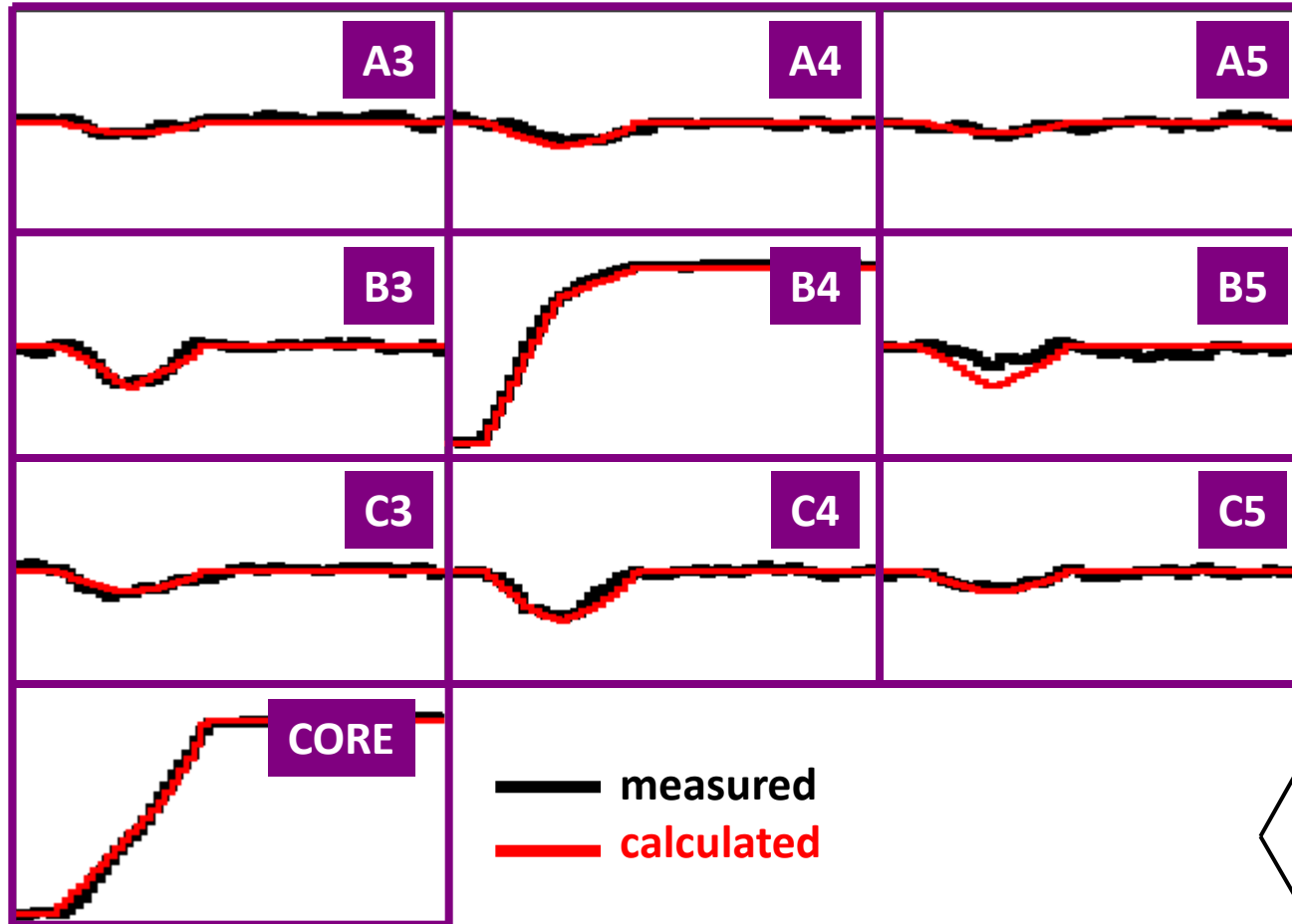
791 keV deposited in segment B4

(10, 20, 46)

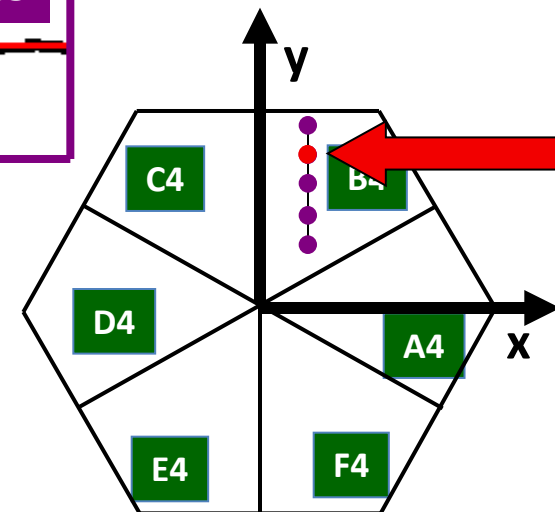


z = 46 mm

# Pulse Shape Analysis concept



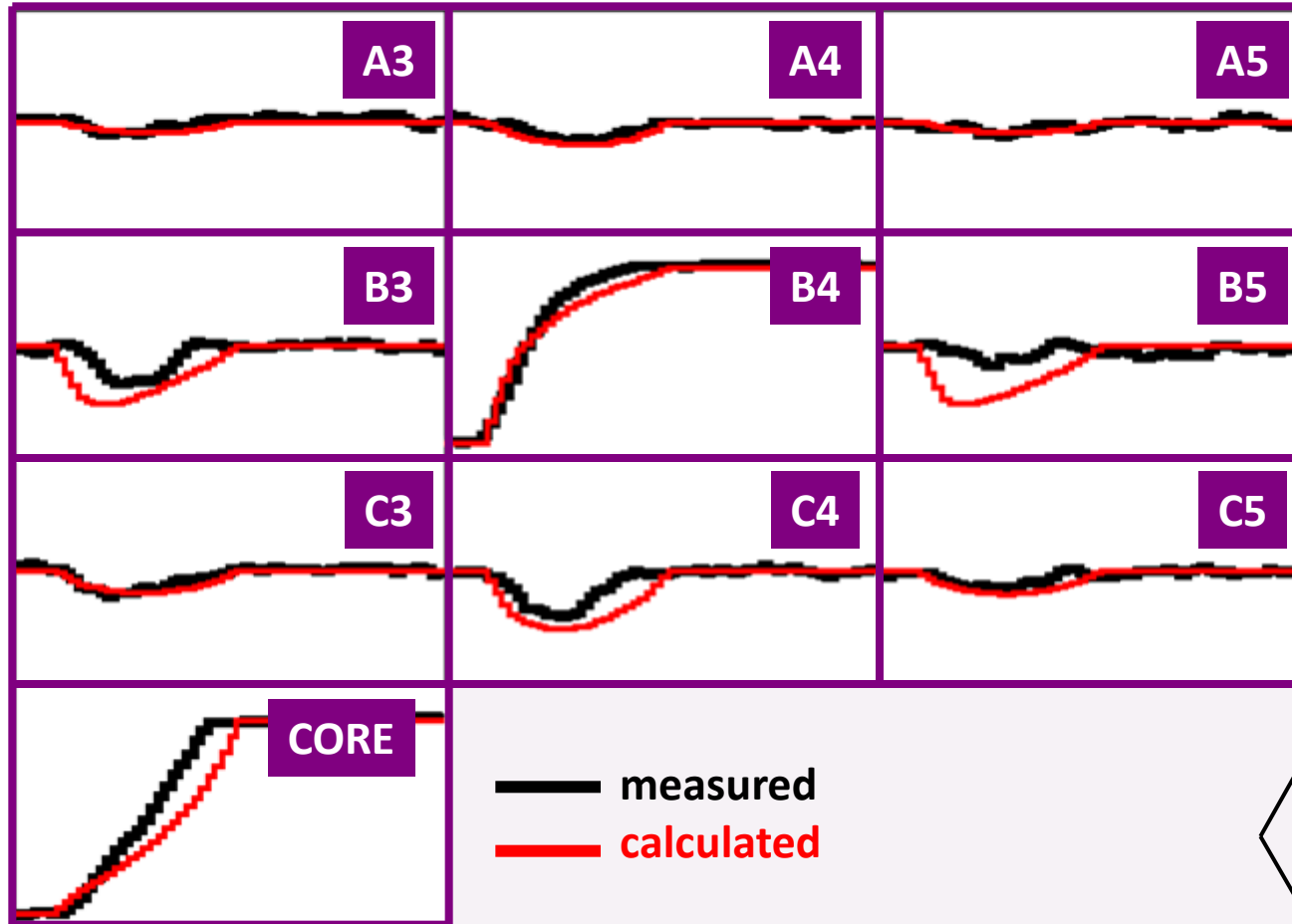
(10,25,46)



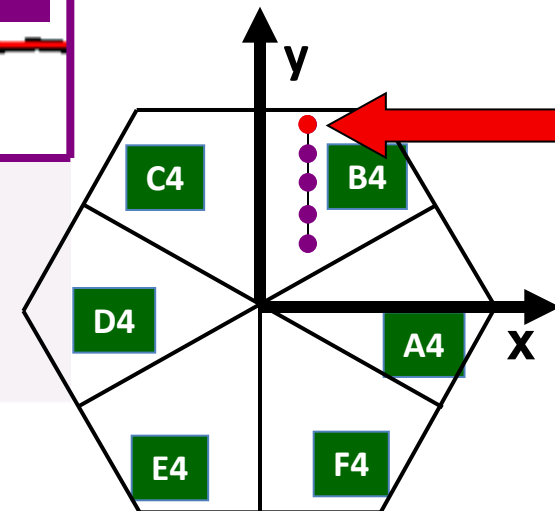
791 keV deposited in segment B4

z = 46 mm

# Pulse Shape Analysis concept



(10, 30, 46)

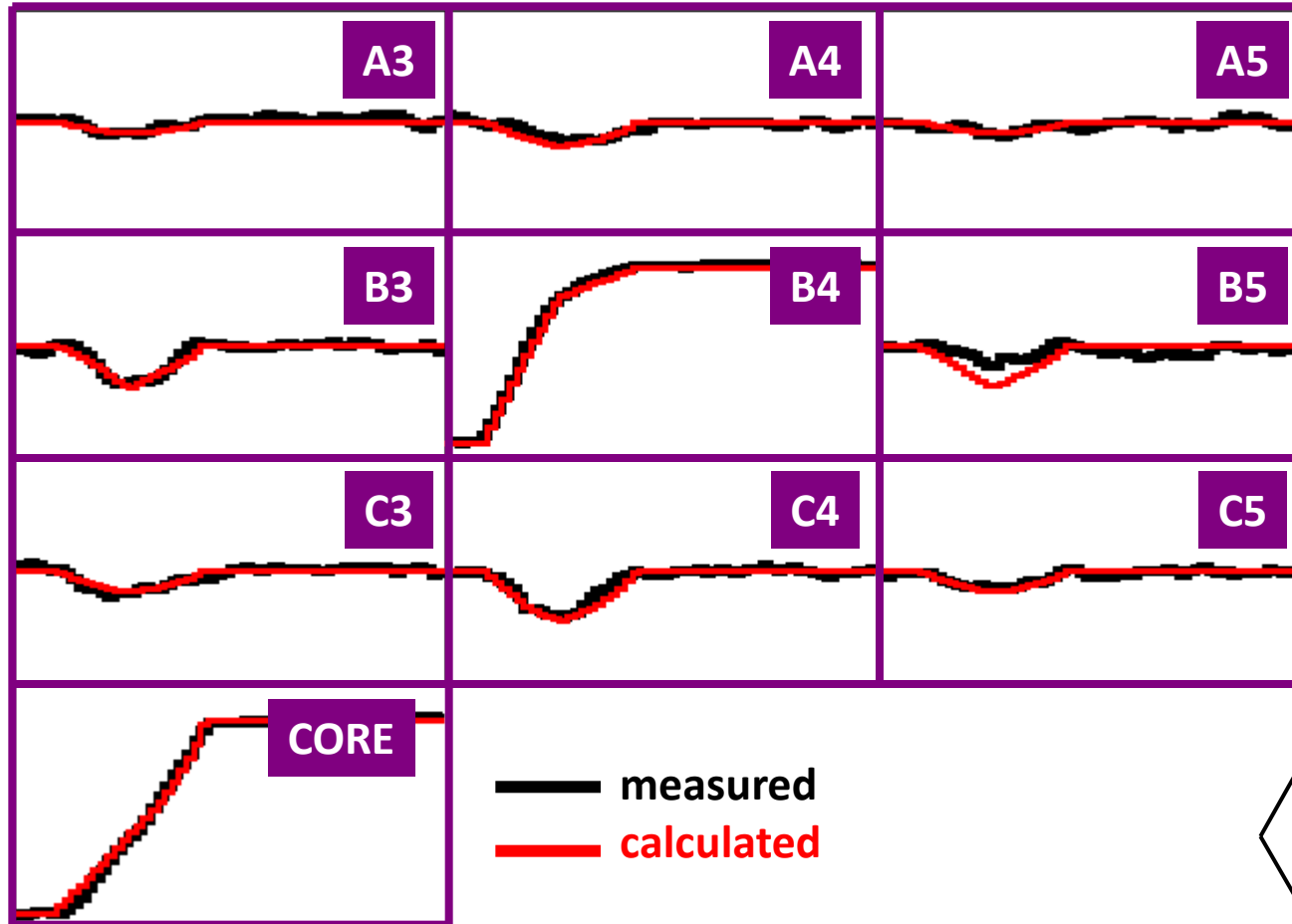


z = 46 mm

791 keV deposited in segment B4

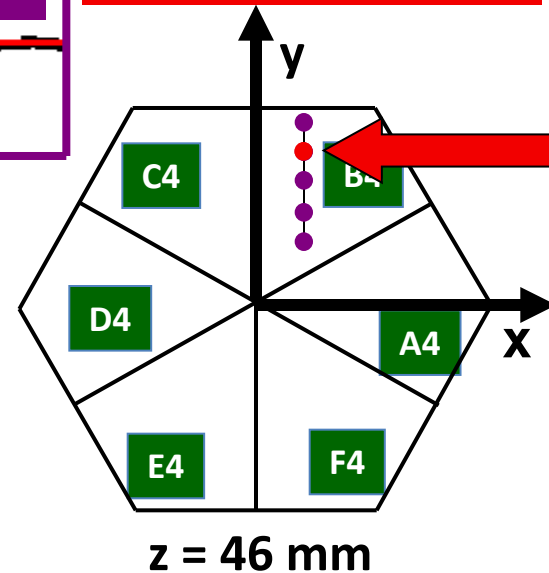


# Pulse Shape Analysis concept



Result of  
*Grid Search*  
Algorithm  
**(10,25,46)**

791 keV deposited in segment B4

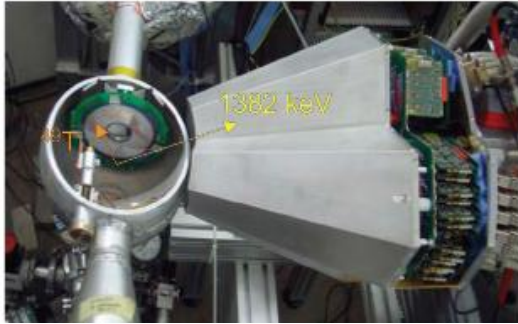


# Position resolution of AGATA

Method = Doppler correction capability  
in an in-beam experiment

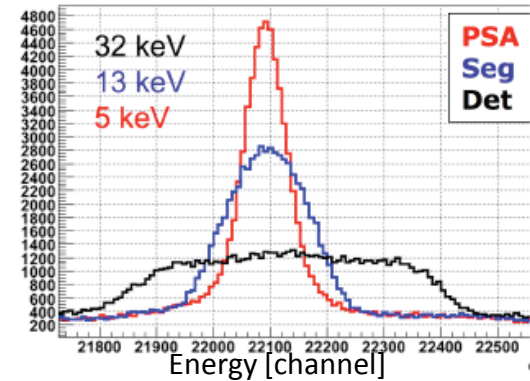
*F. Recchia et al., NIMA 604 (2009) 555*

*P-A. Soederstroem et al., NIMA 638 (2011) 96*

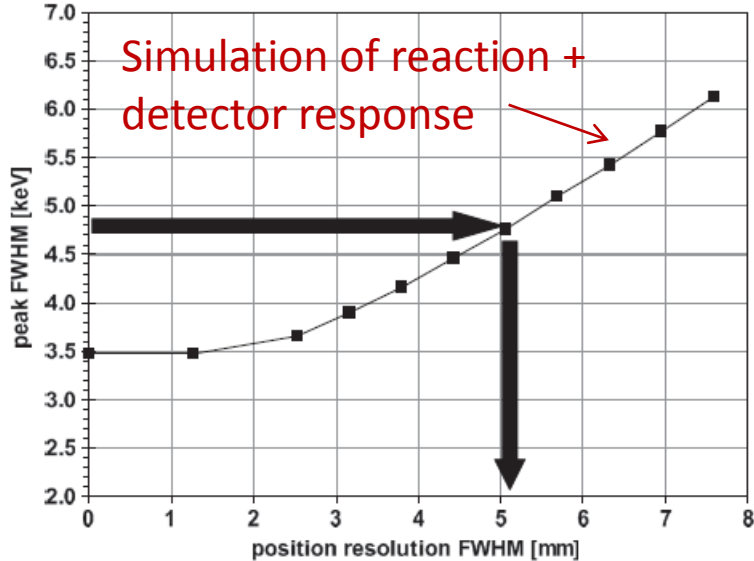


REACTION CHANNEL:  $^{48}\text{Ti}(d,p)^{49}\text{Ti}$

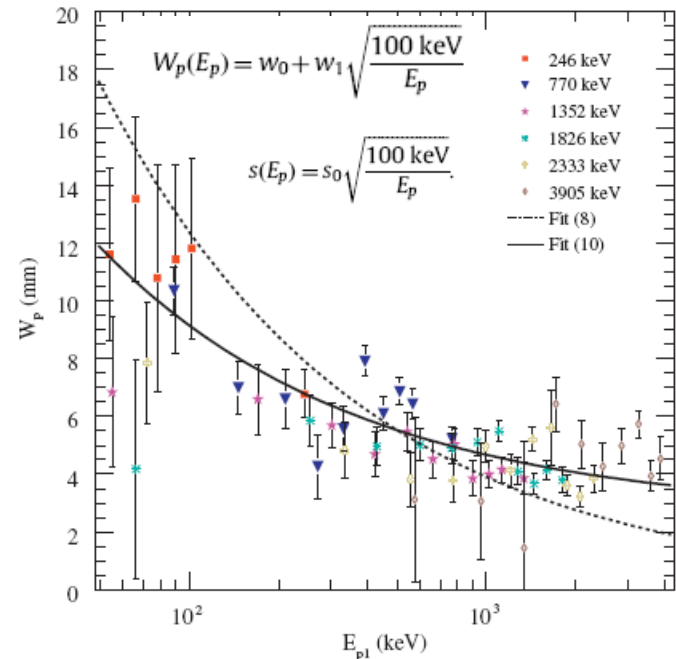
beam	$^{48}\text{Ti}$	100 MeV
target	$^{48}\text{Ti} + ^2\text{H}$	220 $\mu\text{g}/\text{cm}^2$
Si detector	thickness	300 $\mu\text{m}$
	segmentation	32 rings, 64 sectors
AGATA triple symmetric cluster		



*F. Recchia et al., NIMA 604 (2009) 555*



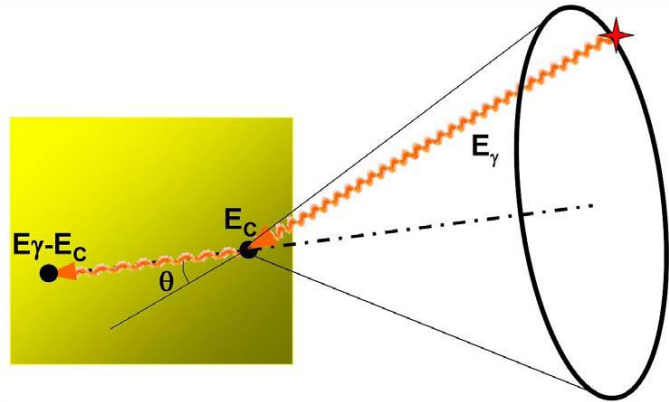
**Fig. 10.** Width of the simulated 1382 keV peak as a function of the position smearing for the full triple cluster. Individual crystal energy resolution have been considered. All of the segment multiplicities are taken into account. The horizontal arrow indicates the experimental width.



*P-A. Soederstroem et al., NIMA 638 (2011) 96*

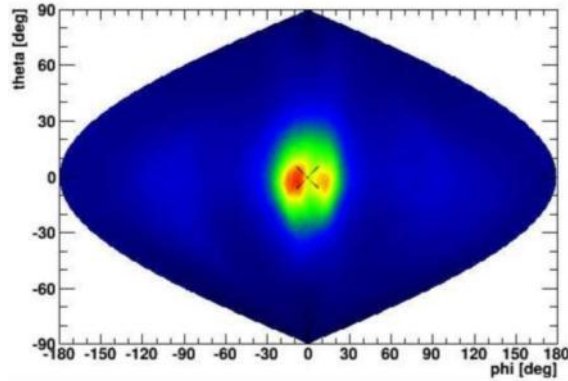
# Imaging of $E_\gamma=1332$ keV gamma rays

AGATA used as a big and expensive Compton Camera

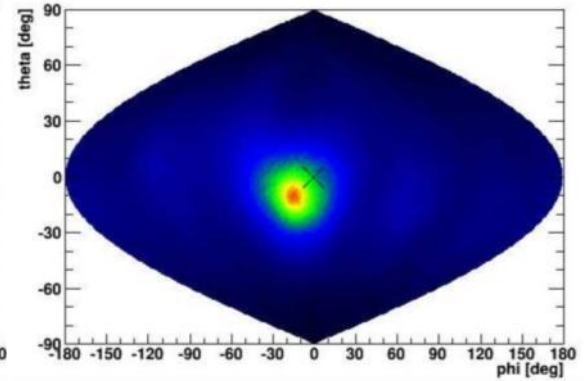


$$\cos \theta = 1 + \left( \frac{1}{E_\gamma} - \frac{1}{E'_\gamma} \right) m_0 c^2$$

Far Field Backprojection

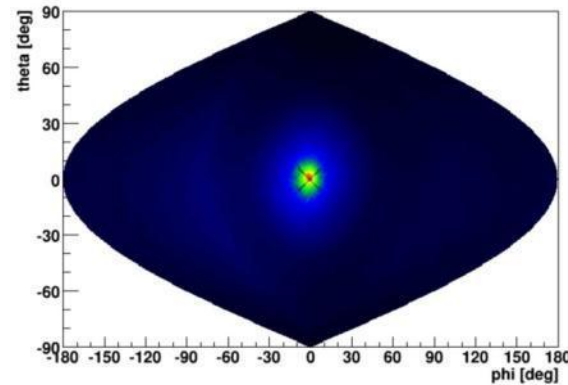


All 9 detectors

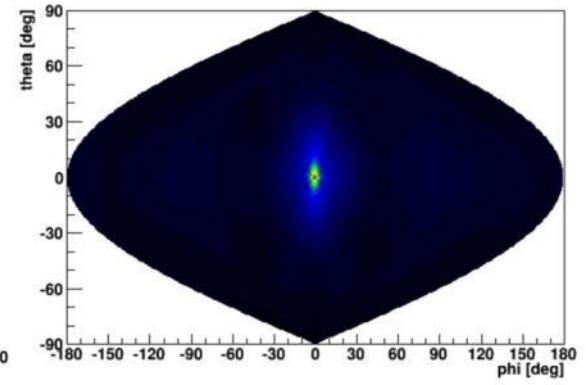


One detector

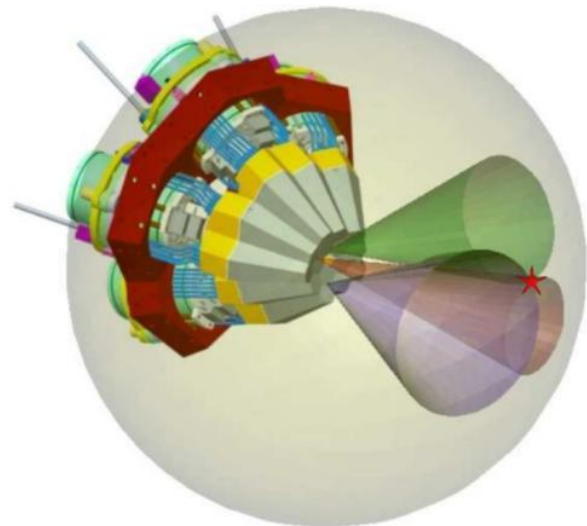
Near Field Backprojection



All 9 detectors



One detector



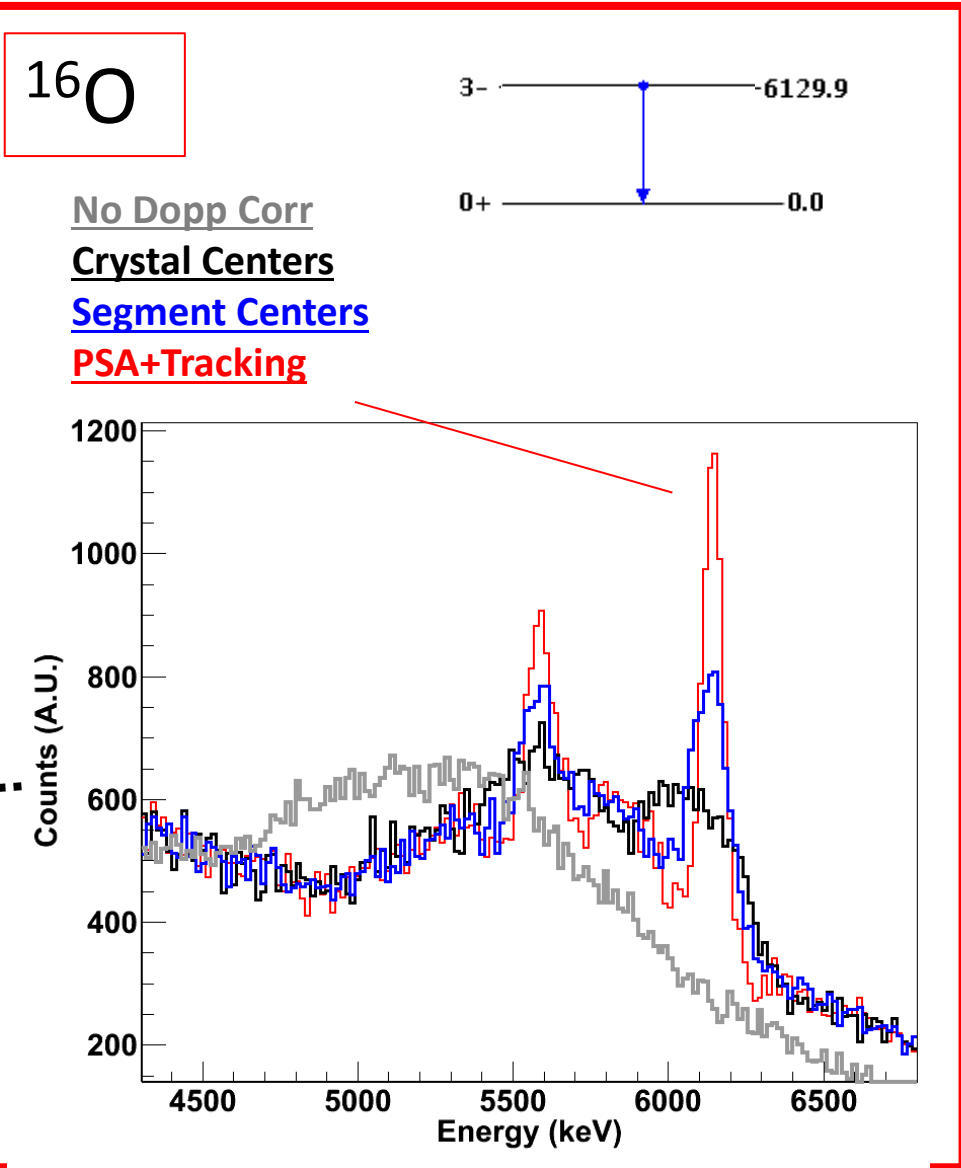
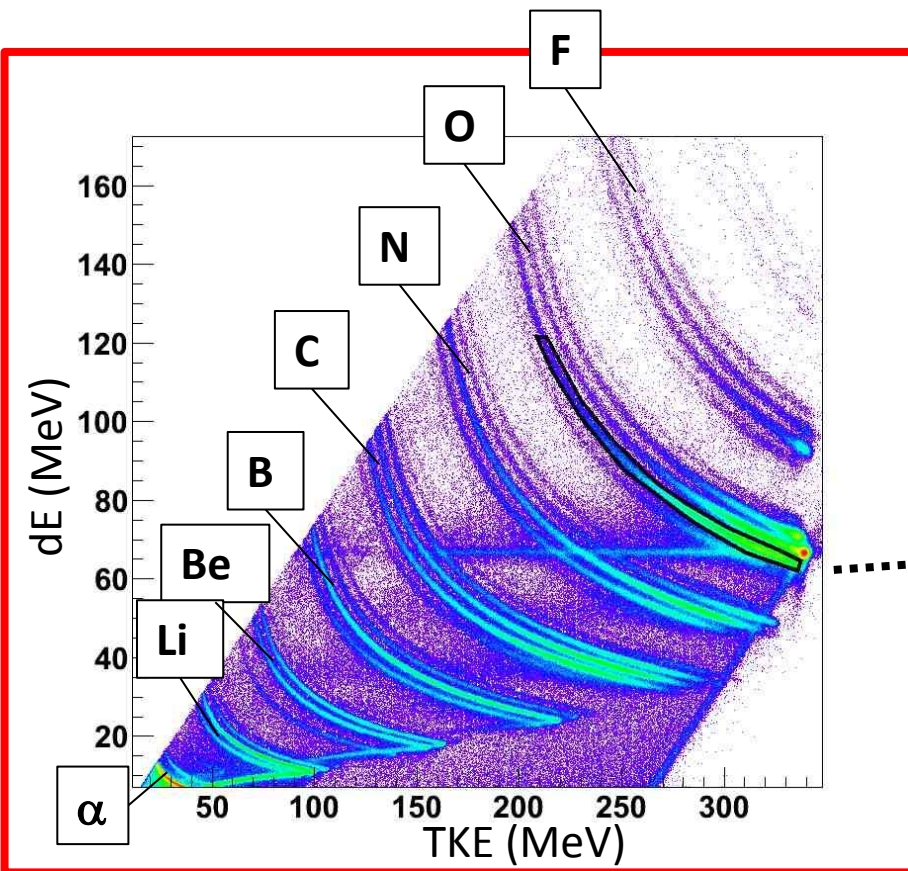
Source at 51 cm →  $D_x \sim D_y \sim 2$  mm  $D_z \sim 2$  cm

# Doppler correction capabilities

AGATA Demonstrator at LNL

Inelastic scattering

$^{17}\text{O}$  @ 20 MeV/u on  $^{208}\text{Pb}$



F.Crespi, Milano

# Outline

*PART 2 (September 29<sup>th</sup> 2015)*

## **Pulse Shape Analysis (PSA)**

1. Signal bases calculation
2. Signal decomposition

**Some results from Ge position sensitive mode operation and  $\gamma$ -ray tracking**

## **The AGATA array of segmented HPGe detectors**

1. Implementation of Pulse Shape Analysis and Tracking concepts
2. The AGATA detectors and preamplifiers
3. The structure of electronics and data acquisition
4. Digital signal processing (at high counting rate)
5. (AGATA data processing)

**AGATA+VAMOS (magnetic spectrometer) at GANIL**

*(be aware ... personal 😊selection of topics!)*